Genetic Algorithms and Ant Colony Optimisation

Introduction: Optimisation

- Optimisation : find an extremum
- Extrema can be local / global
- In Rⁿ (real numbers): methods with and without gradients

Local :

- □ With derivative (ok : space = Rⁿ) → gradient (possibly: first degree or even more)
- Without derivative : select a point, explore the neighborood, take the best, do it again. (type hill climber, local search)
- Global :
 - I = local with different initial conditions.
 - Method without derivatives \rightarrow GA

- Combinatorial optimisation problems.
- Deterministic algorithms : Explore too much and take too much time
 meta-heuristiques : find rapidly a satisfactory solution
- Example : Scheduling problem, packing or ordering problems
- The classics of the classics : TSP
 - The travelling salesman problem
 - N cities
 - □ Find the shortest path going through each city only once
 - Benchmarking problems
 - Problems NP-complete (the time to find grows exponentially with the size of the problem (N! ~ N^(N+1/2)))

Genetic Algorithms: Introduction

- Evolutionary computing
- 1975 : John Holland \rightarrow Genetic algorithms
- 1992 : John Koza → Genetic programming

Genetic algorithms

- Darwinian inspiration
- Evolution = optimisation:

Reproduction

- 2 genetic operators:
 - Cross-over (recombination)
 - Mutation

Fitness

The standard algorithm

- Generate random population
- Repeat
- \Box Evaluate fitness *f*(*x*) for each individual of the population
- Create a new population (to repeat until a stopping critetion)
 - Selection (according to fitness)
 - Crossover (according to probability of crossover)
 - Mutation (according to probability of mutation)
 - evaluate the new individuals in the population (replacement)
- Replace the old population by the new (better) ones

Until stop condition; return the best solution of the current population

The GA lingo





Chromosones encoding

Can be influenced by the problem to solve

Examples:

- Binary encoding
- Permutation encoding (ordening problems) e.g. TSP problem)
- Real value encoding (evolutionary strategies)
- Tree encoding (genetic programming)

Binary Encoding

Chromosome A101100101100101011100101Chromosome B111111100000110000011111

 Binary encoding is the most common, mainly because first works about GA used this type of encoding. In binary encoding every chromosome is a string of bits, 0 or 1.

Example of Problem: Knapsack problem

The problem: There are things with given value and size. The knapsack has
given capacity. Select things to maximize the value of things in knapsack, but do
notnotextendknapsackcapacity.Encoding: Each bit says, if the corresponding thing is in knapsack.

Permutation Encoding

Chromosome A	1	5	3	2	6	4	7	9	8
Chromosome B	8	5	6	7	2	3	1	4	9

- In permutation encoding, every chromosome is a string of numbers, which represents number in a sequence.
- **Example of Problem:** Traveling salesman problem (TSP)

The problem: There are cities and given distances between them.Travelling salesman has to visit all of them, but he does not to travel very much. Find a sequence of cities to minimize travelled distance. **Encoding:** Chromosome says order of cities, in which salesman will visit them.

Value Encoding

Chromosome A1.23245.32430.45562.32932.4545Chromosome BABDJEIFJDHDIERJFDLDFLFEGTChromosome C(back), (back), (right), (forward), (left)

- In value encoding, every chromosome is a string of some values. Values can be anything connected to problem, form numbers, real numbers or chars to some complicated objects.
- **Example of Problem:** Finding weights for neural network

The problem: There is some neural network with given architecture. Find weights for inputs of neurons to train the network for wanted output.

Encoding: Real values in chromosomes represent corresponding weights for inputs.



- In tree encoding every chromosome is a tree of some objects, such as functions or commands in programming language.Used in genetic programming
- **Example of Problem:** Finding a function from given values

The problem: Some input and output values are given. Task is to find a function, which will give the best (closest to wanted) output to all inputs.

Encoding: Chromosome are functions represented in a tree.

Crossover - Recombination

- C1: 1011|10001
- C2: 0110|11100
- → D1: 1011|11100
- → D2: 0110|10001
- Variants, many points of crossover

Crossover – Binary Encoding

- Single Point Crossover
 □ 11001011 et 10011111→11001111
 Two Point Crossover
 - □ 11001011 et 10011111 \rightarrow 11011111
- Uniform Crossover
 - □ 11001011 et 10011111 \rightarrow 11011111
- Difference operators:
 - □ 11001011 AND 10011111 → 10001011

Crossover - variants

- Permutation encoding
 - Single Point Crossover
 - (123456789) et (453689721) →(123459768)
- Tree encoding



Mutation

- D1: 101111100
- D2: 011010001
- →M1: 100111100
- →M2: 001010101
- variants

Mutation - Variants

- Binary Encoding
 - □ Bit inversion 101111100→11111100
- Permutation Encoding
 - □ Order changing (123456897)→(183456297)
- Value Encoding
 - □ +/- one number (1.29 5.68 2.86 4.11 5.55) → (1.29 5.68 2.73 4.22 5.55)
- Tree Encoding: (ex)-change nodes

Selection

- By roulette wheel
- By rank
- By tournement
- Steady-State

Roulette wheel

Selection according to fitness



Selection by rank

Sorting of the population $(n \rightarrow 1)$



Selection by tournament

Size *k*

- Take randomly k individuals
- Make them compete and select the best



➡ → Elitism: copy the single or many bests in the population then construct the remaining ones by genetic operations

So many parameters

- Crossover probability
- Mutation probability
- Population size

Ant Colony

In biology:



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Ant Colony

Adaptivity



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Ants Foraging Behavior Example: The Double Bridge Experiment

Goss et al., 1989, Deneubourg et al., 1990





Simple bridge

% of ant passages on the two branches

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Ant Colony

Navigation

- -At first: random
- -Using pheromones as previous search experience

Recruitment (communication) – Indirect via the environment

Ants Trail

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Ant System Applied to the TSP

Ant System is the ancestor of all Ant Colony Optimization algorithms Dorigo, Maniezzo, Colorni, 1991 Dorigo & Gambardella, 1996

Pheromone trail depositing



Probabilistic rule to choose the path

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Ant Algorithms



Ant Algorithms

For all iterations For all ants choose and perform action (i.e. choose next node to visit) Update pheromone

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Ant System (AS): Some Results



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