

---

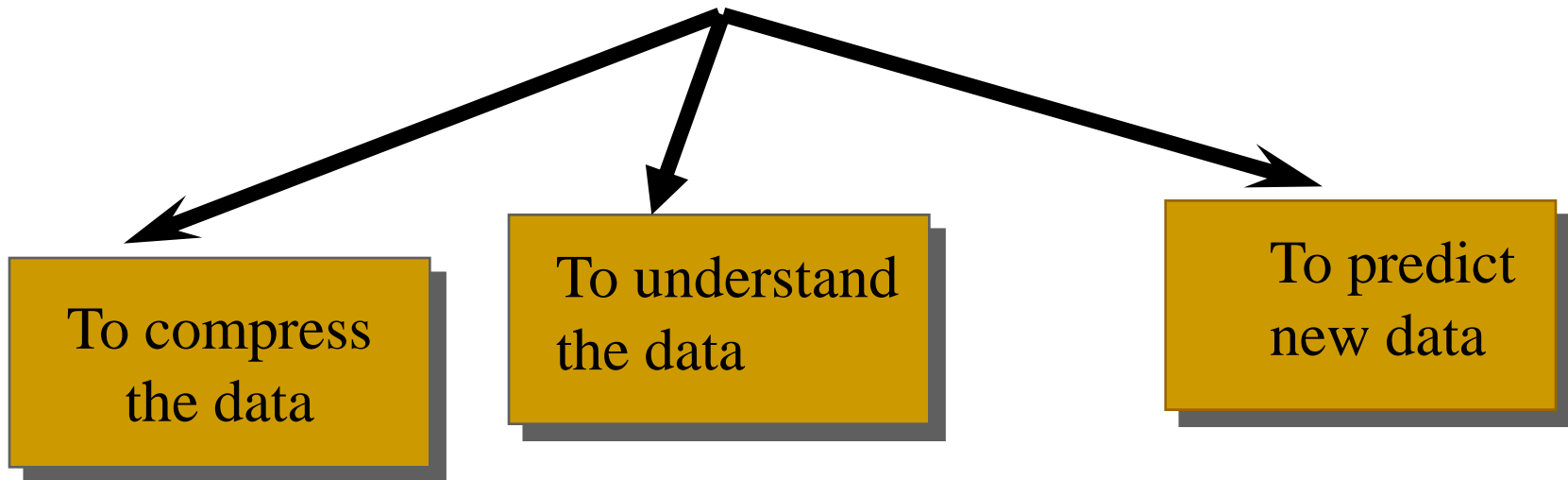
# Data Mining in a complex world

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Hugues Bersini  
IRIDIA/CODE

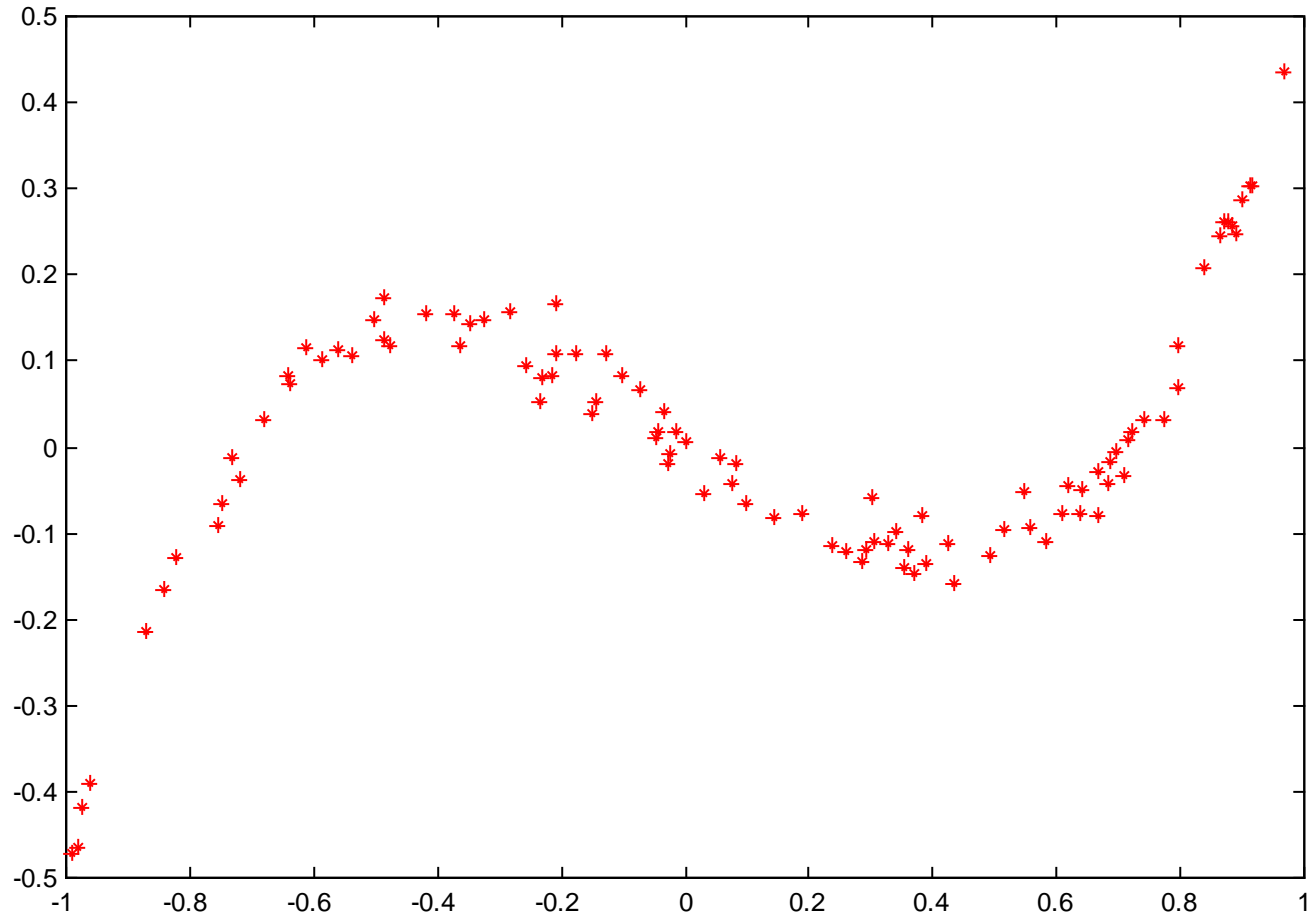
# Modelling the data: WHY ??

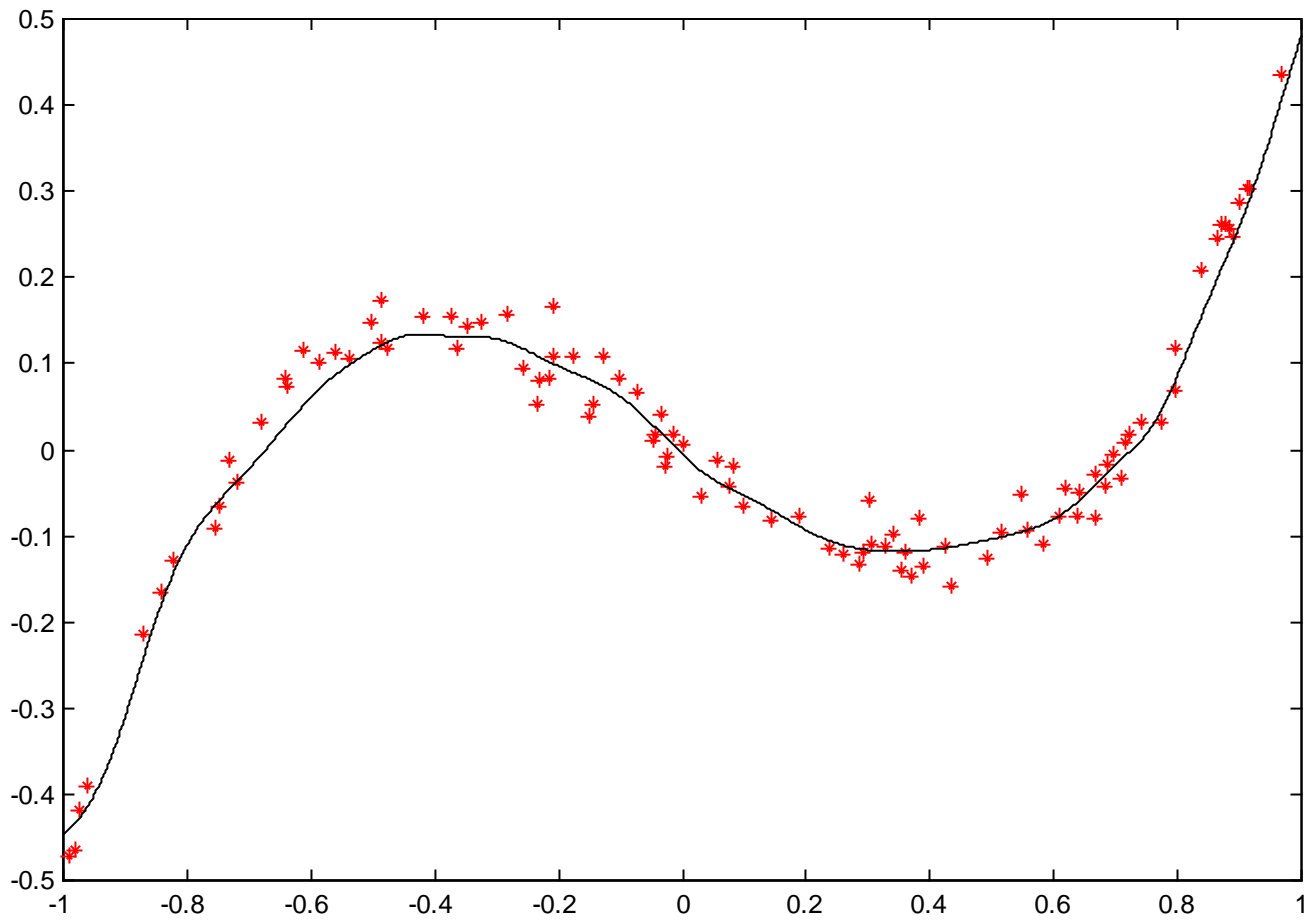
only if structure and regularities in the data  
data contains the needed information in a hidden form !!



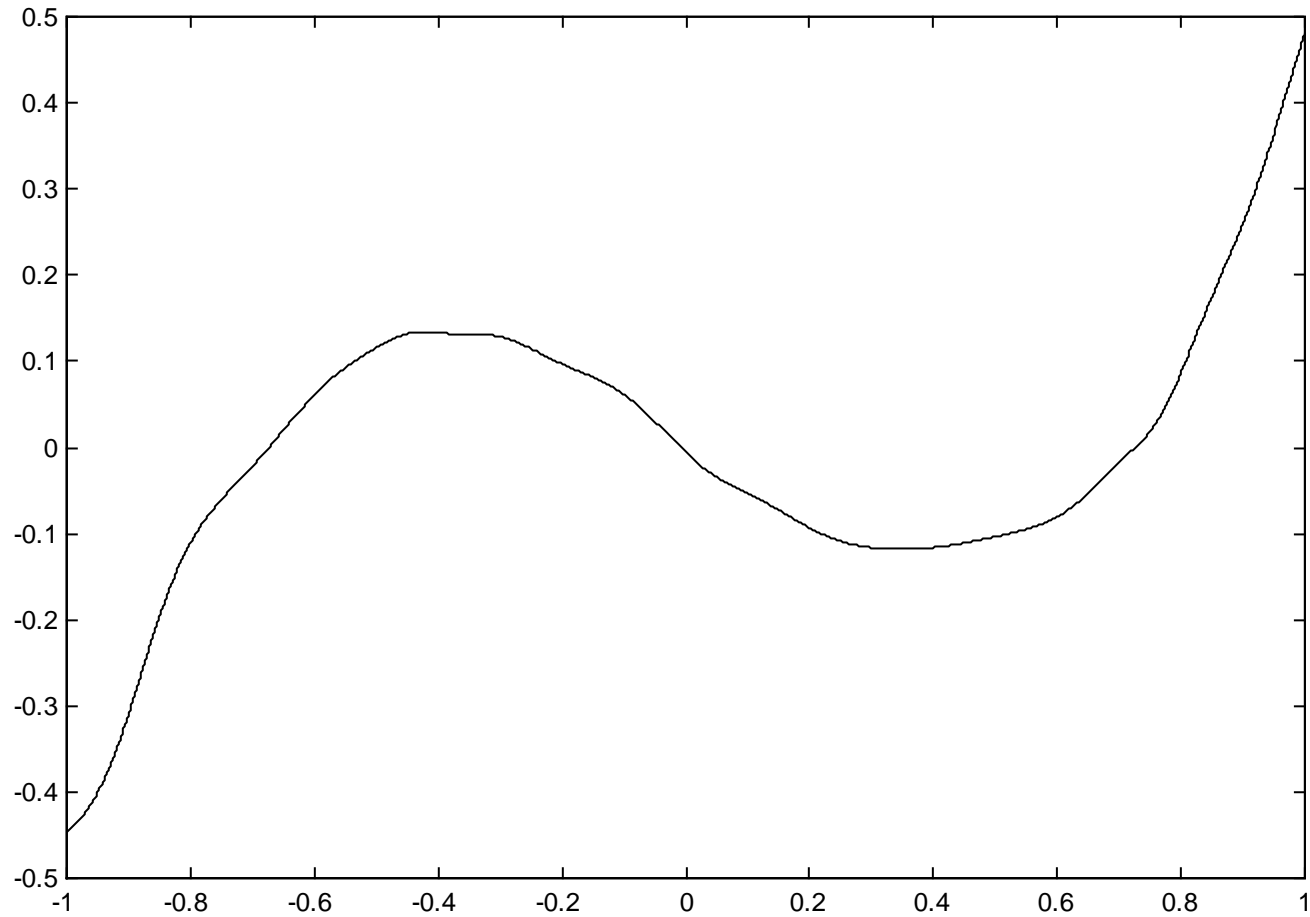
They might be antagonistic objectives

Training set

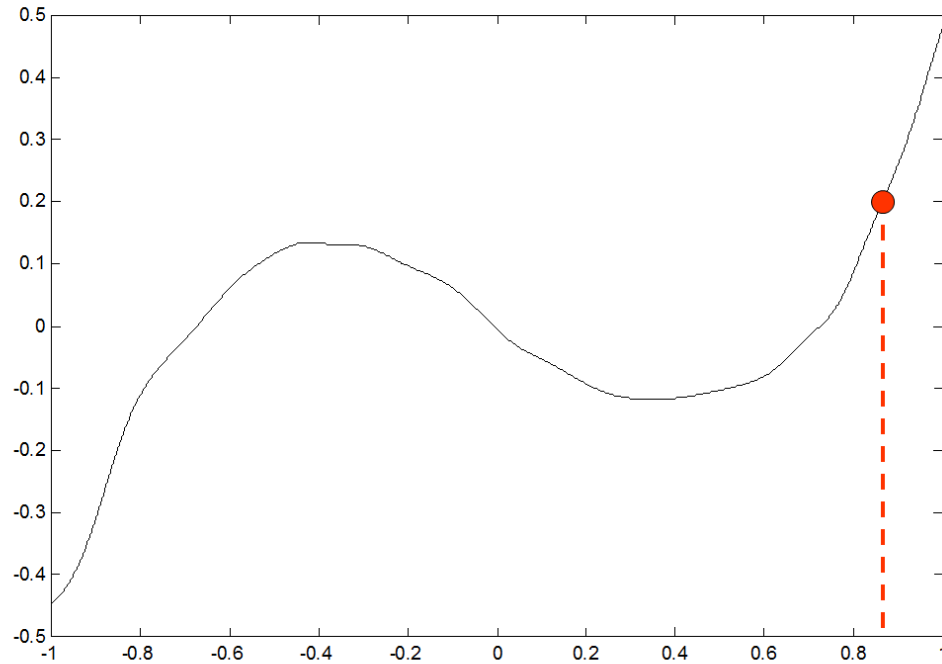




## A compressed model with predictive power



# Prediction with global models



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# The main techniques of data-mining

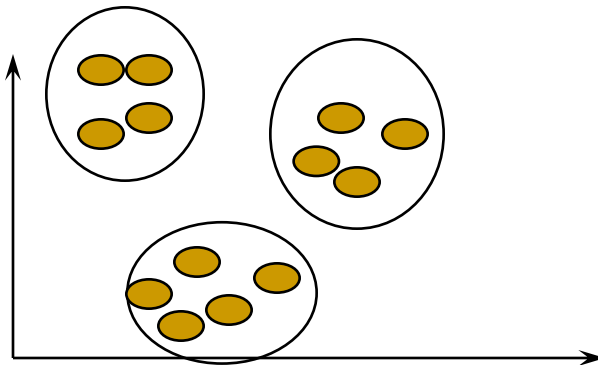
- Clustering
  - Classification
  - Outlier detection
  - Association analysis
  - Regression
  - Forecasting
  - Why in business: personalized business, improved prediction, targeted marketing
-

# Data Classification: to understand and/or to predict

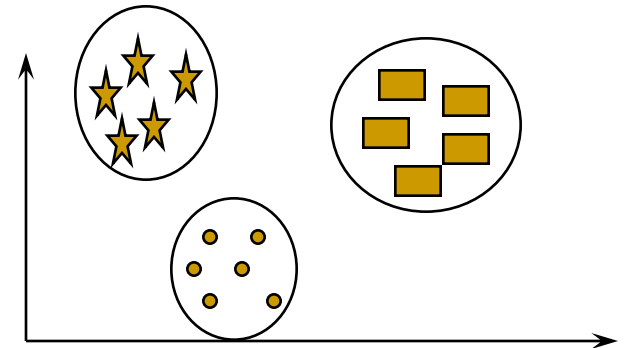
Clustering

Classification

discovering structure in data

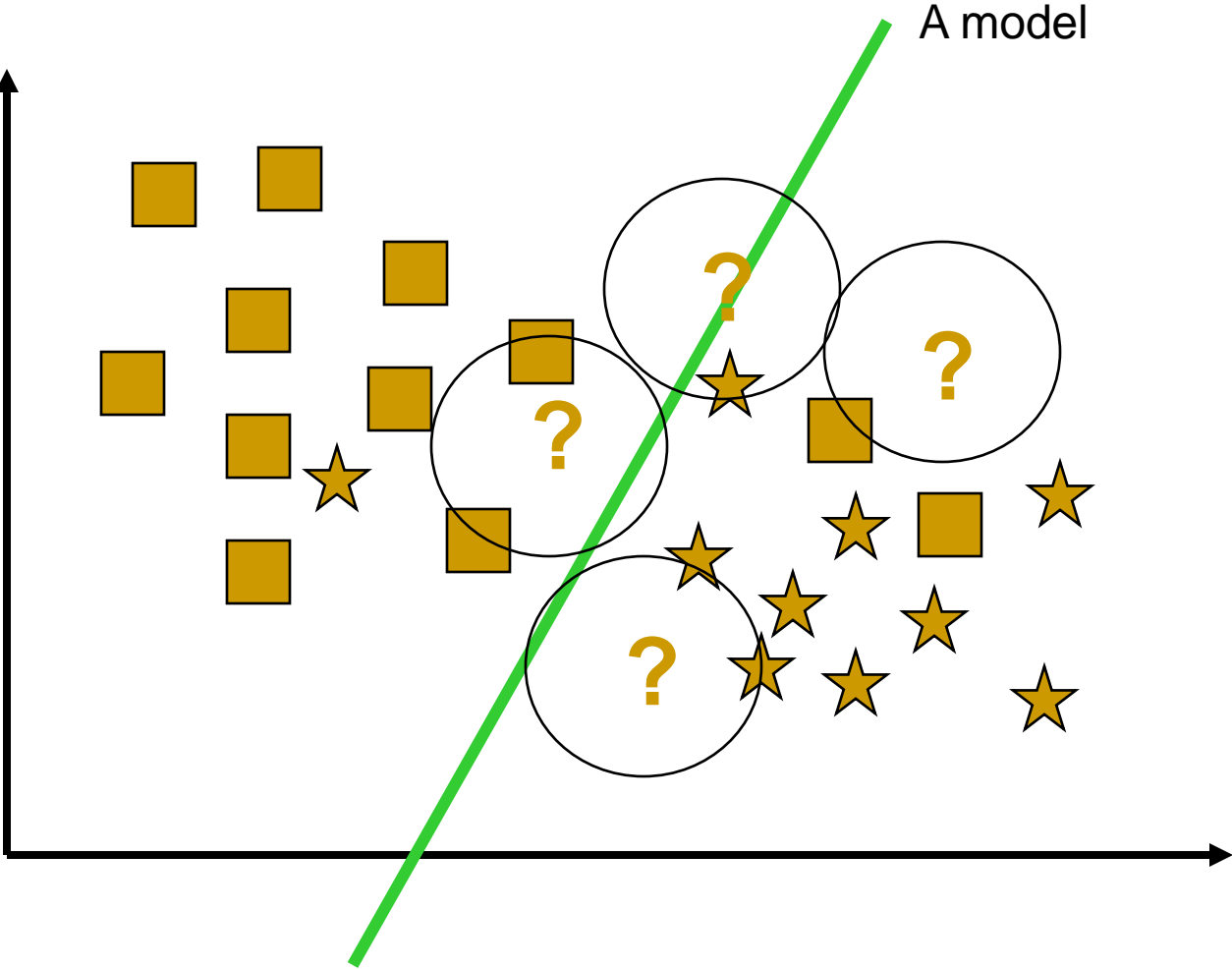


discovering I/O relationship in data

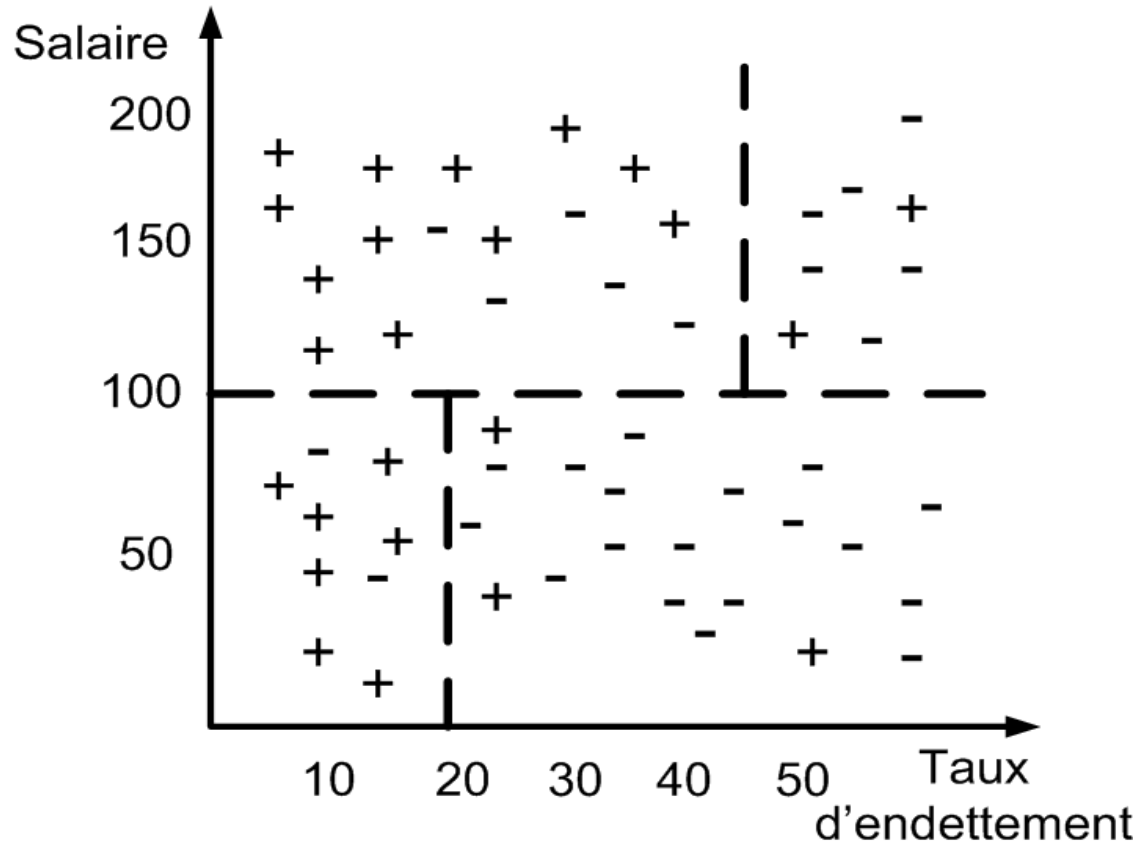


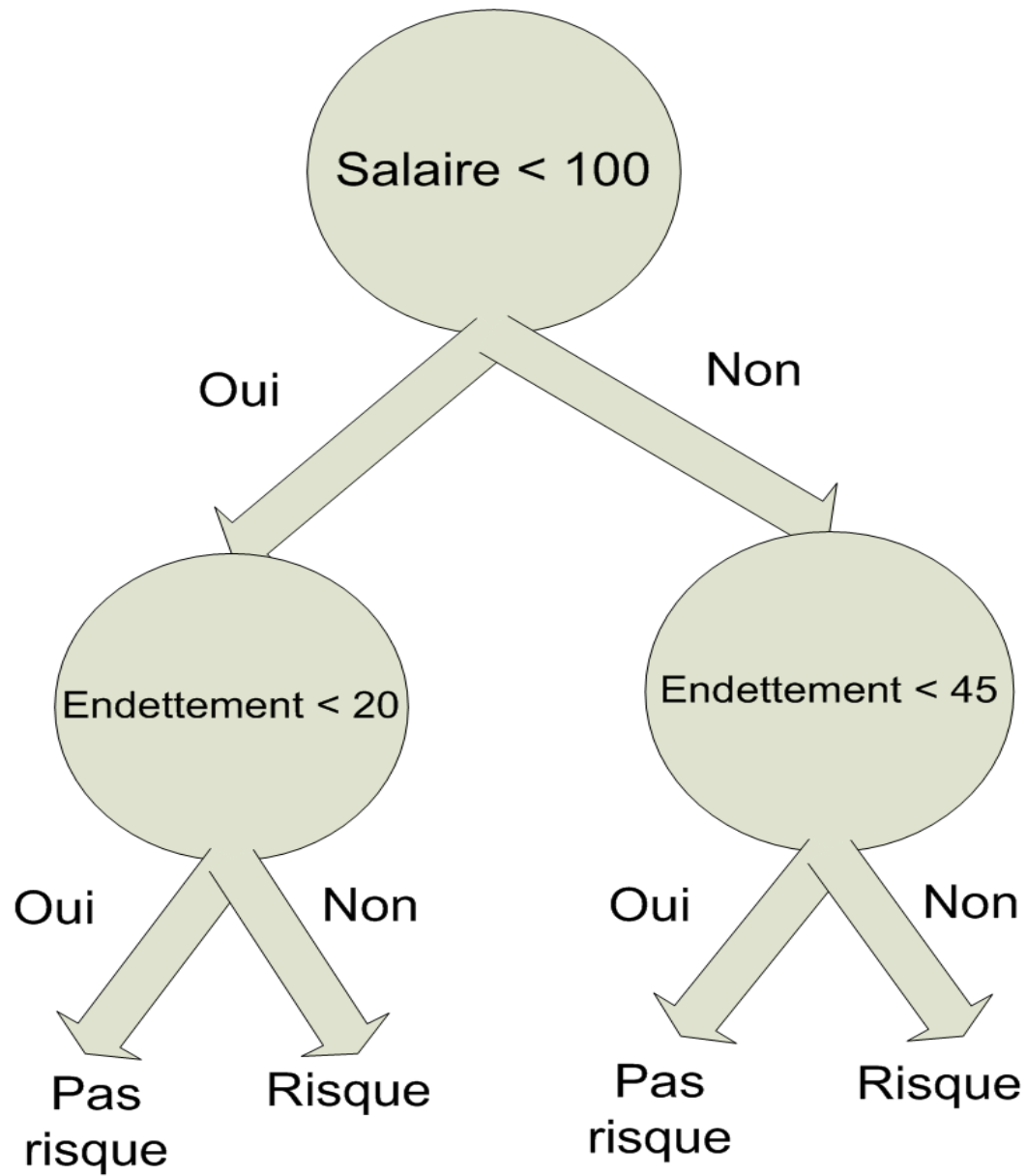


# CLASSIFICATION



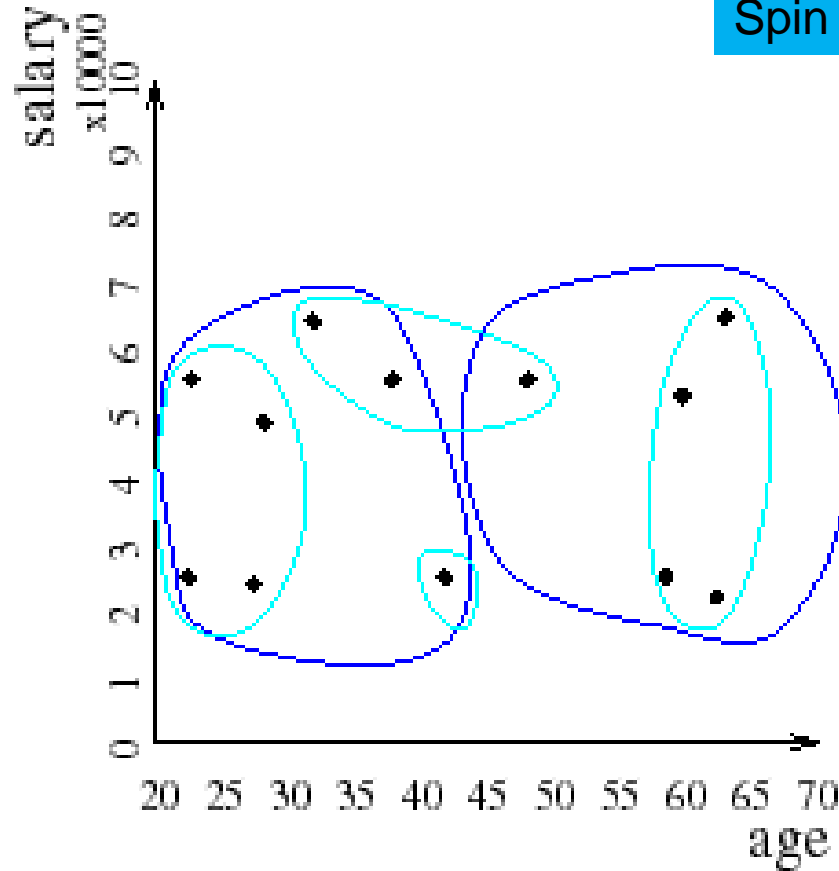
# Exemple de classification: Decision tree





# Clustering and outlier

Spin off : VADIS



Intéressant petit coco

# Market Basket Analysis: Association analysis

Quantity bought

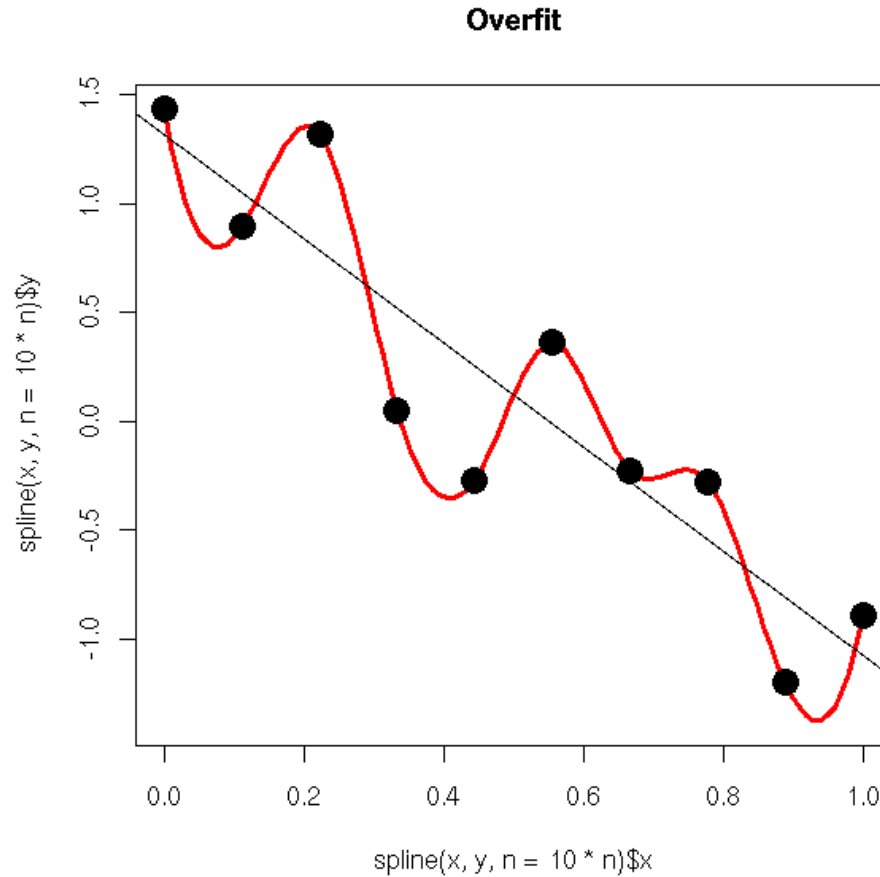
Transn.	Juice	Tea	Coffee	Milk	Sugar	Pop
1	0	0	0	0	0	0
2	0	2	2	4	3	0
3	1	0	0	0	0	0
4	0	1	0	0	0	0
5	1	2	1	1	0	0
6	0	2	1	3	2	0
7	0	0	0	0	0	6
8	0	0	0	0	0	0
9	4	0	0	0	0	0
10	0	0	1	1	0	0
11	0	0	0	0	0	6
12	0	0	1	1	0	0
13	0	0	0	0	0	5
14	0	0	0	0	0	0
15	1	2	0	2	0	0
16	0	1	1	1	2	1
17	1	0	1	0	0	0
18	2	0	0	0	0	0
19	0	0	0	0	0	2
20	3	0	0	0	0	3

# Calcul of Improvement

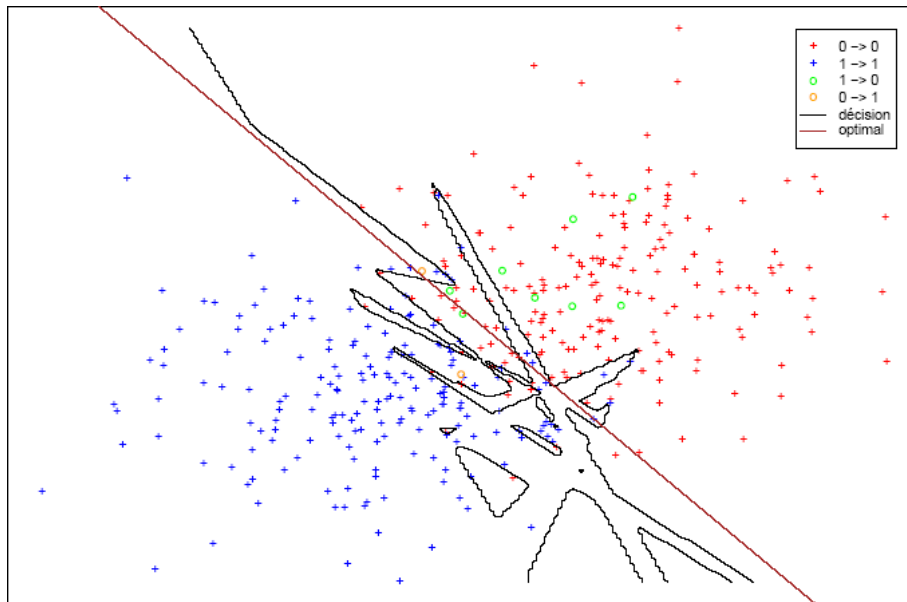
$$\text{IMPROVEMENT} = (N * x_{ij}) / (n_i * n_j)$$

Improvement	Juice	Tea	Coffee	Milk	Sugar	Pop
Juice	0	0,95	0,82	0,82	0	0,17
Tea	0.95	0	1,9	2.38	3,33	0.56
Coffee	0.82	1,9				
Milk	0,82					
Sugar	0	3,33				
Pop	0,17					

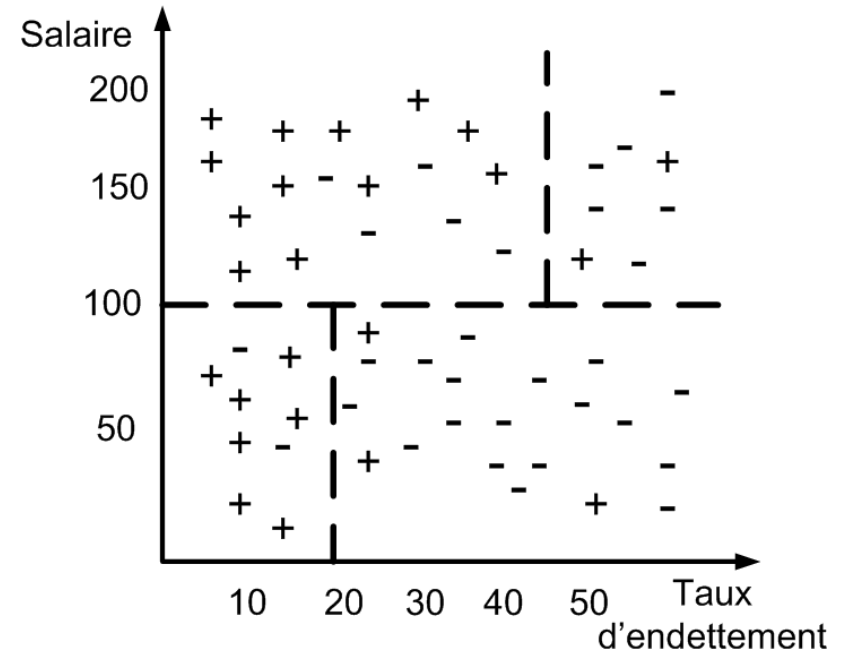
# Data Regression and Prediction



# Understand or predict



Neural networks



Decision tree

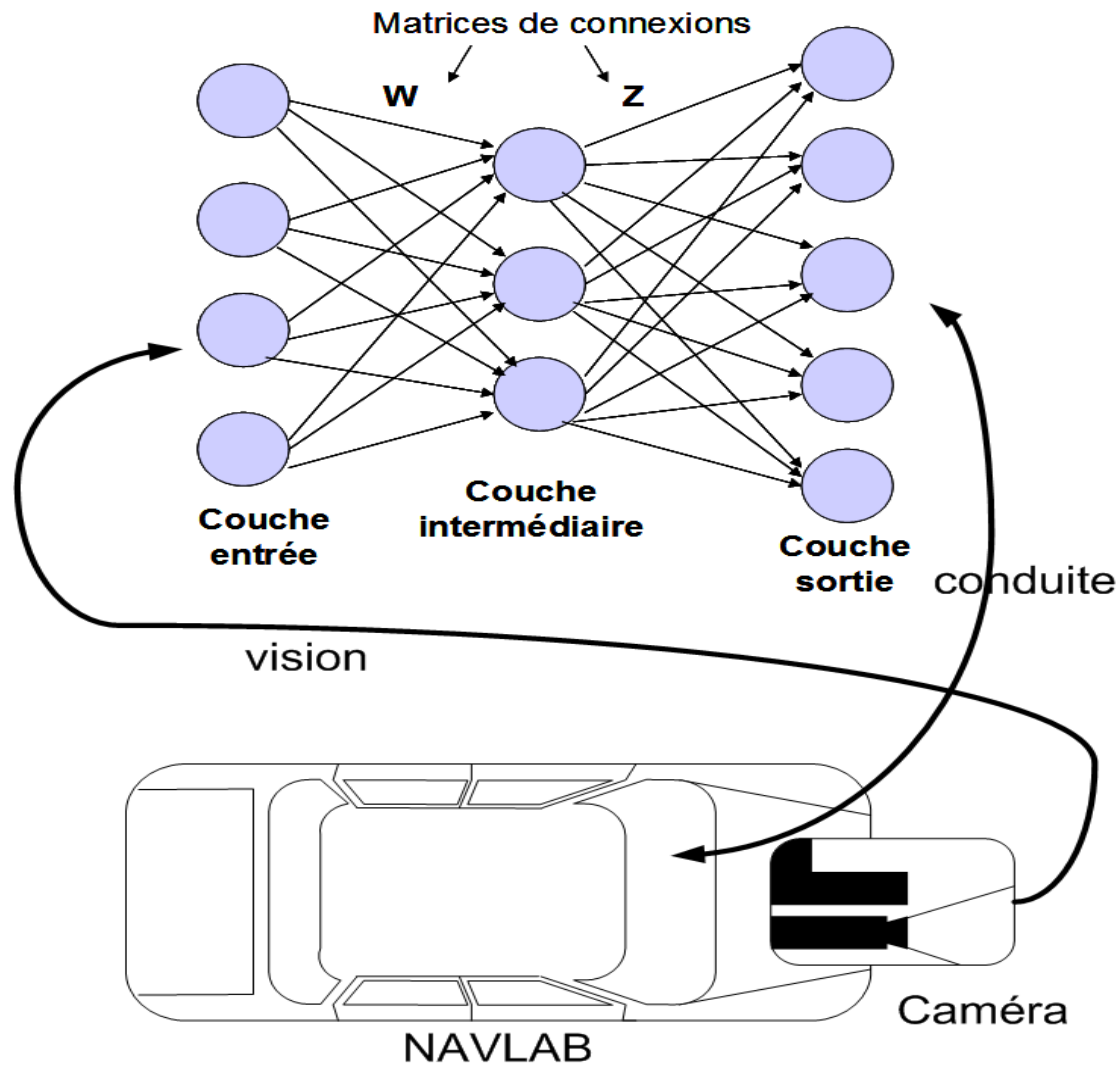


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# Important emblematic achievements

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# 1) A new engineering approach



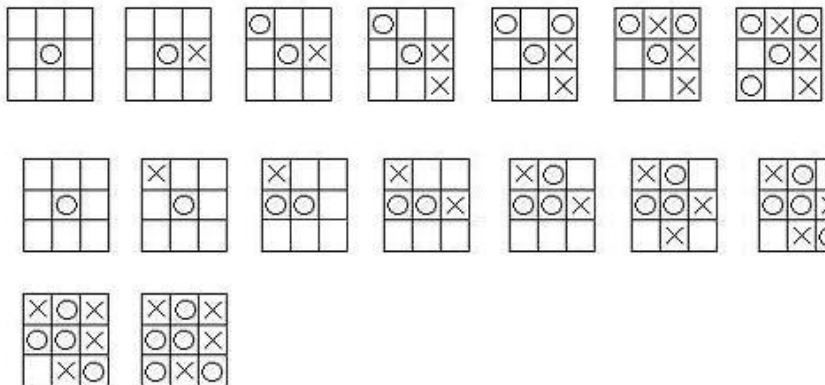
# The Darpa Challenge



# Games

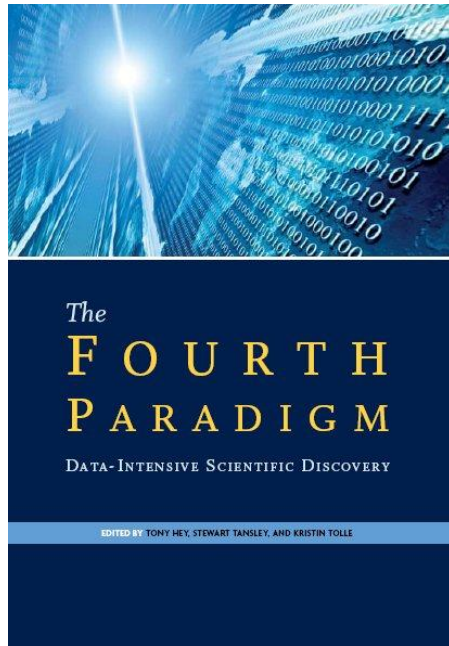


Min-max



Data mining

## 2) A new scientific Paradigm: The fourth : Microsoft

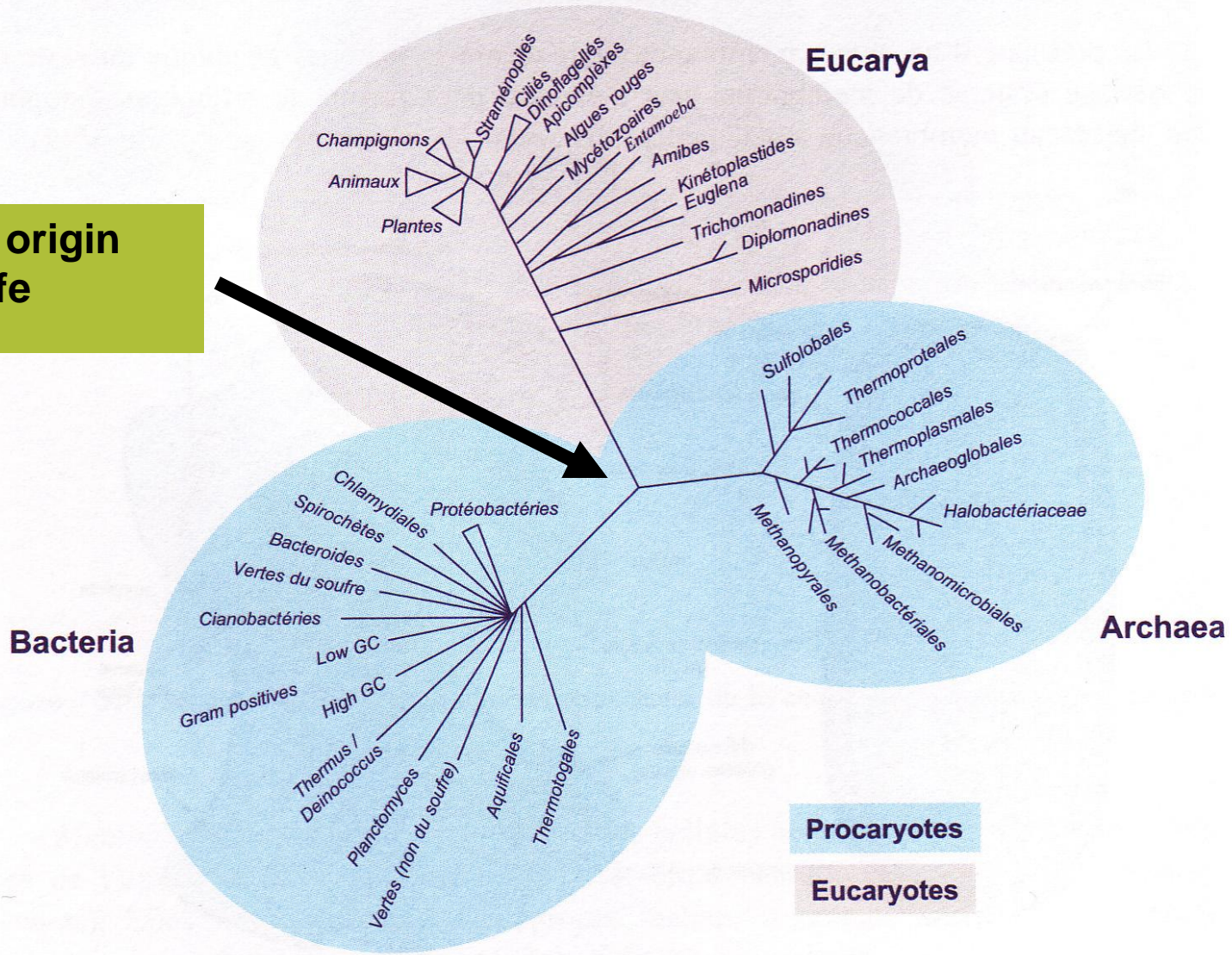


Increasingly, scientific breakthroughs will be powered by advanced computing capabilities that help researchers manipulate and explore massive datasets. The speed at which any given scientific discipline advances will depend on how well its researchers collaborate with one another, and with technologists, in areas of eScience such as databases, workflow management, visualization, and cloud computing technologies.

.



The origin of life



# CLIMATE FORECASTING

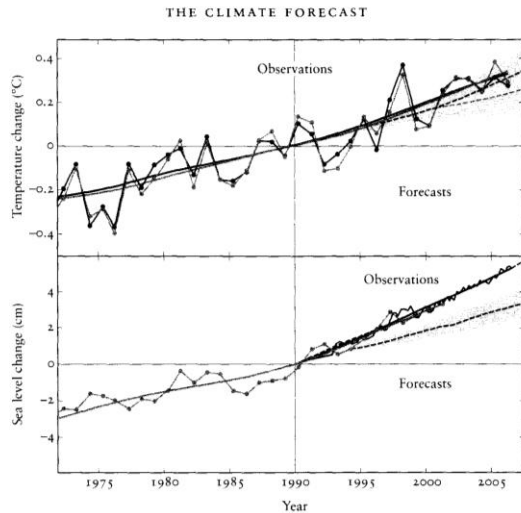


Figure 1. Upper panel: comparison of observations of global mean temperature (joined points) with model forecasts (grey zone and dotted lines). Lower panel: comparison of observed sea level (joined points) and model forecasts (grey zone and dotted lines). Both panels cover the years 1970 to 2007.



James Lovelock

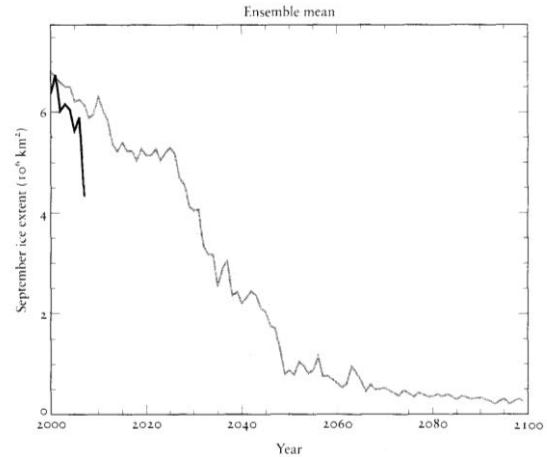
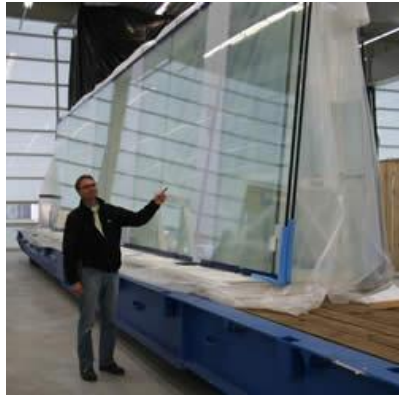


Figure 2. The IPCC model predictions of the extent of ice covering the summer Arctic Ocean (grey zone with a solid line representing the average in its centre) and the observed ice cover (solid line to the left of the figure).



### 3) A huge market of business opportunities: IRIDIA's CV

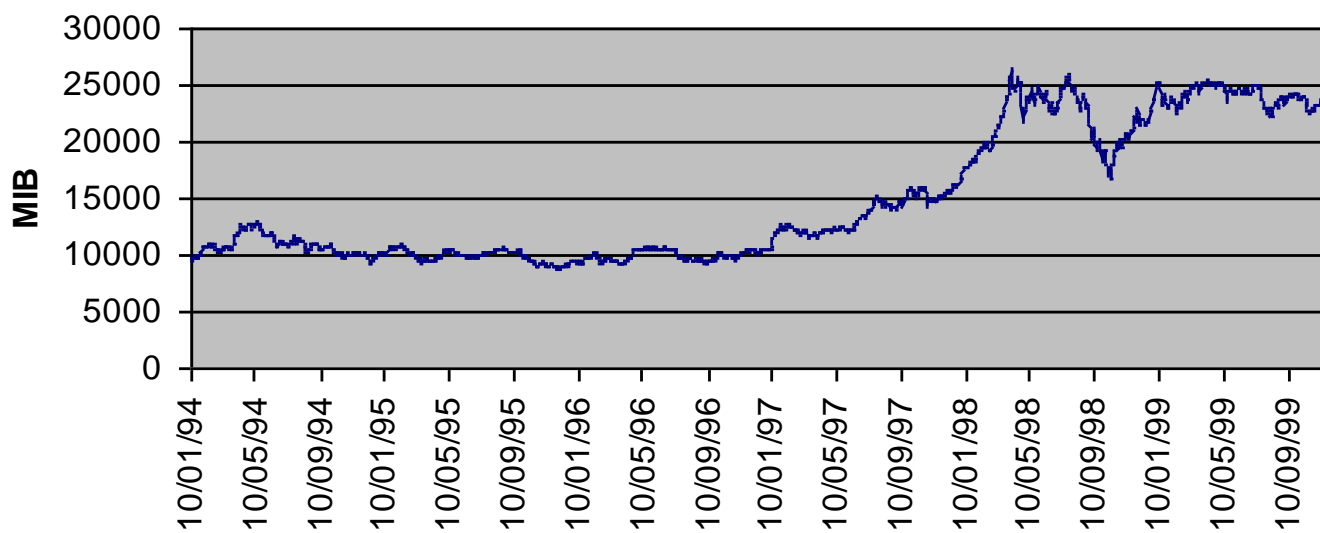
Automatic glass defect recognition



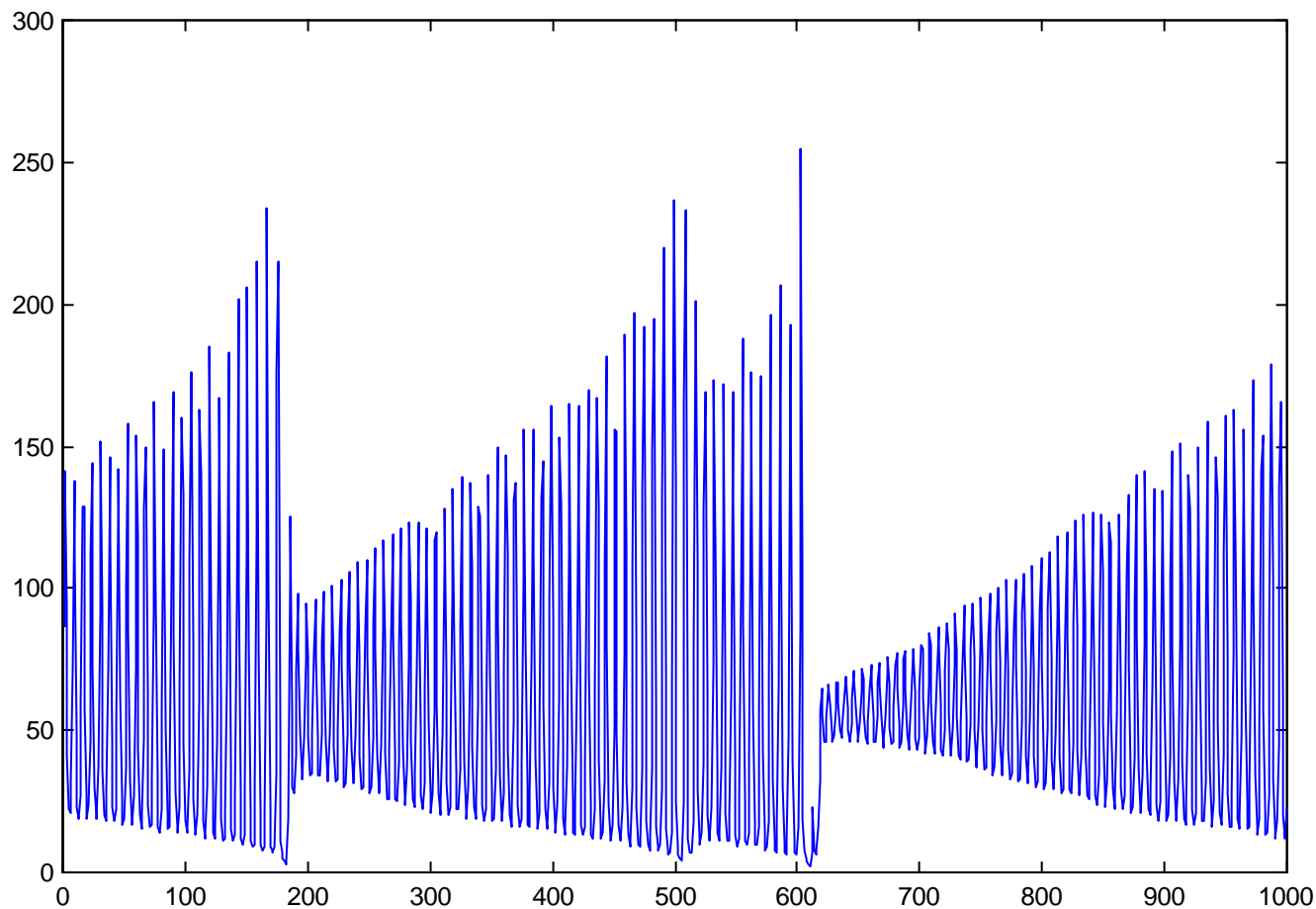


# Financial prediction

daily stock market index

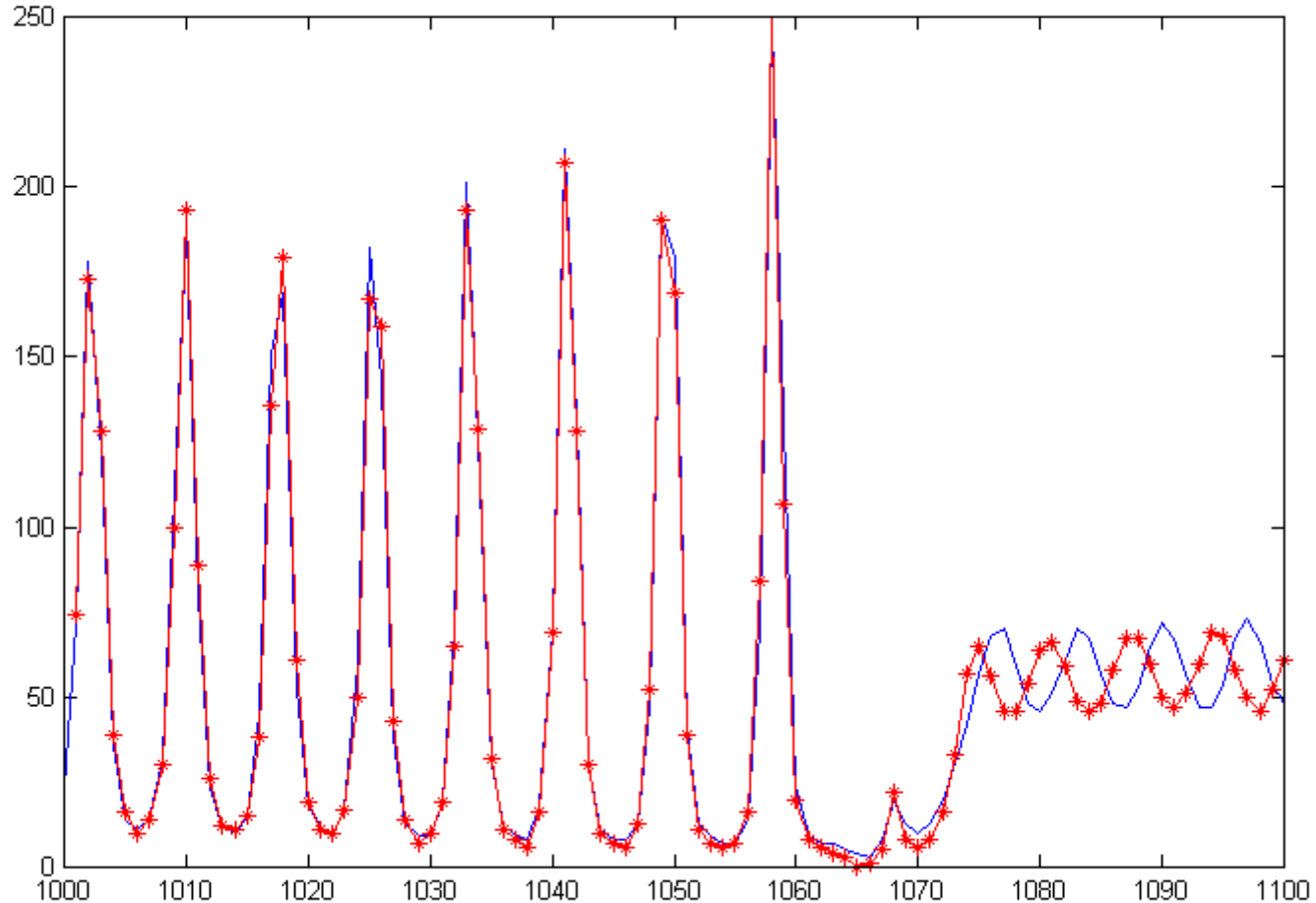


# Santa Fe time series



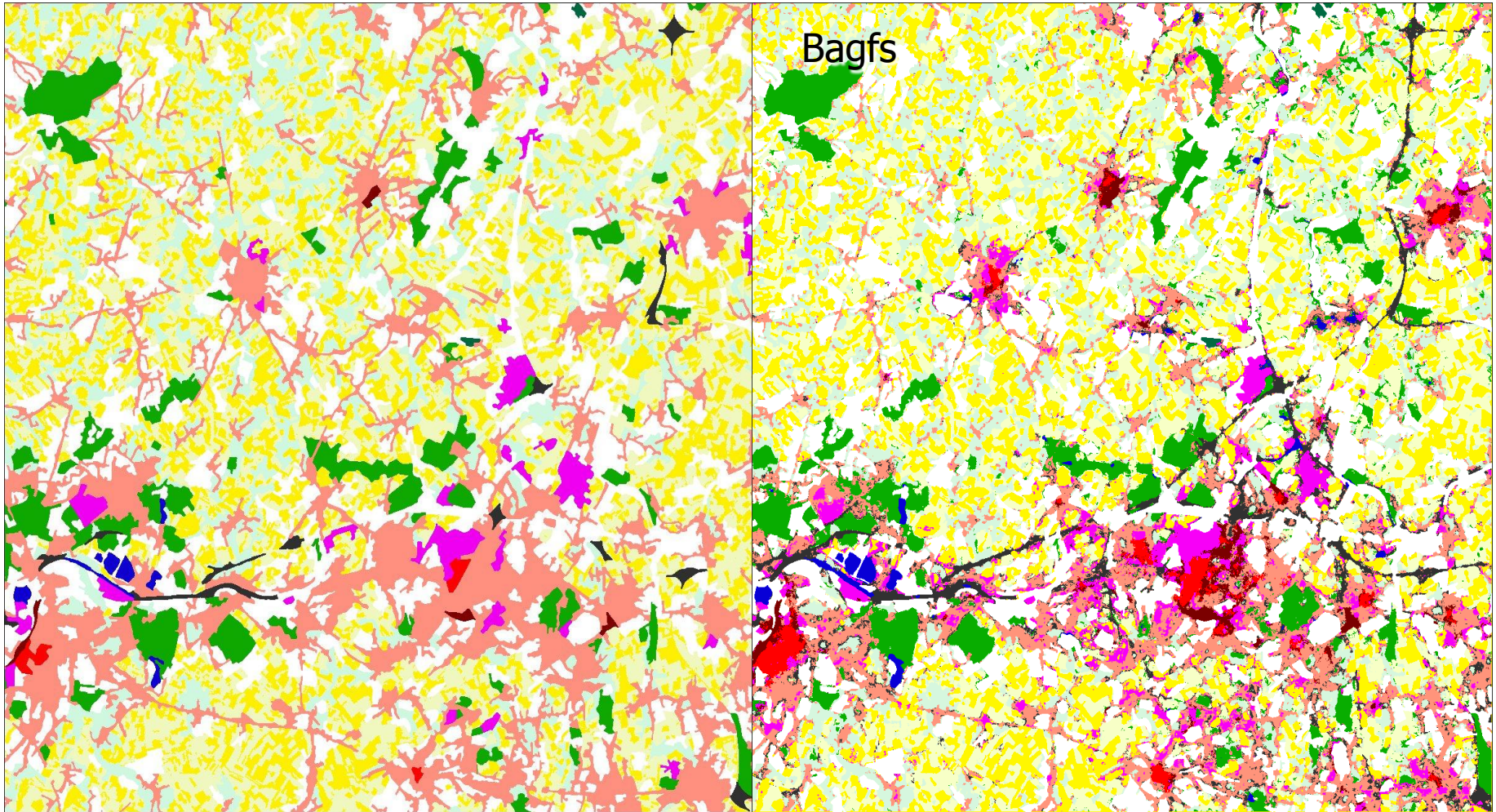
**Task:** predict the continuation of the series for the next 100 steps.

# Lazy Learning prediction



LL is able to predict the abrupt change around  $t = 1060$  !

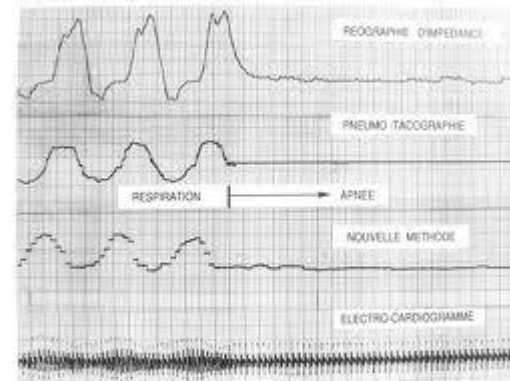
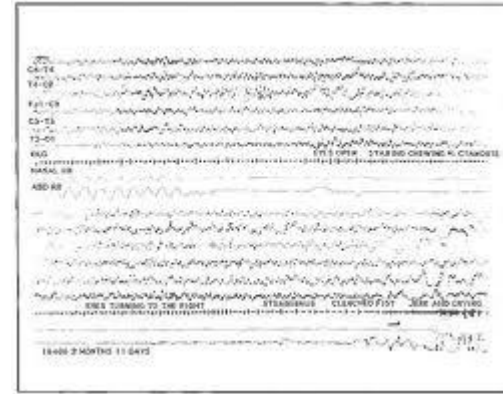
# Automatic image labelling



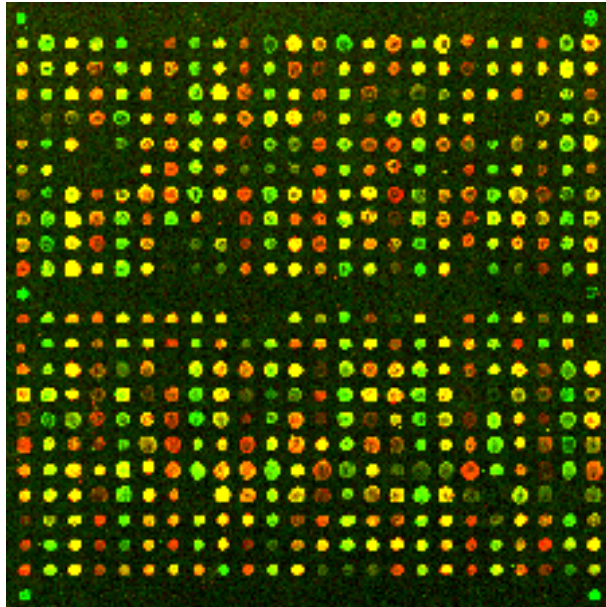




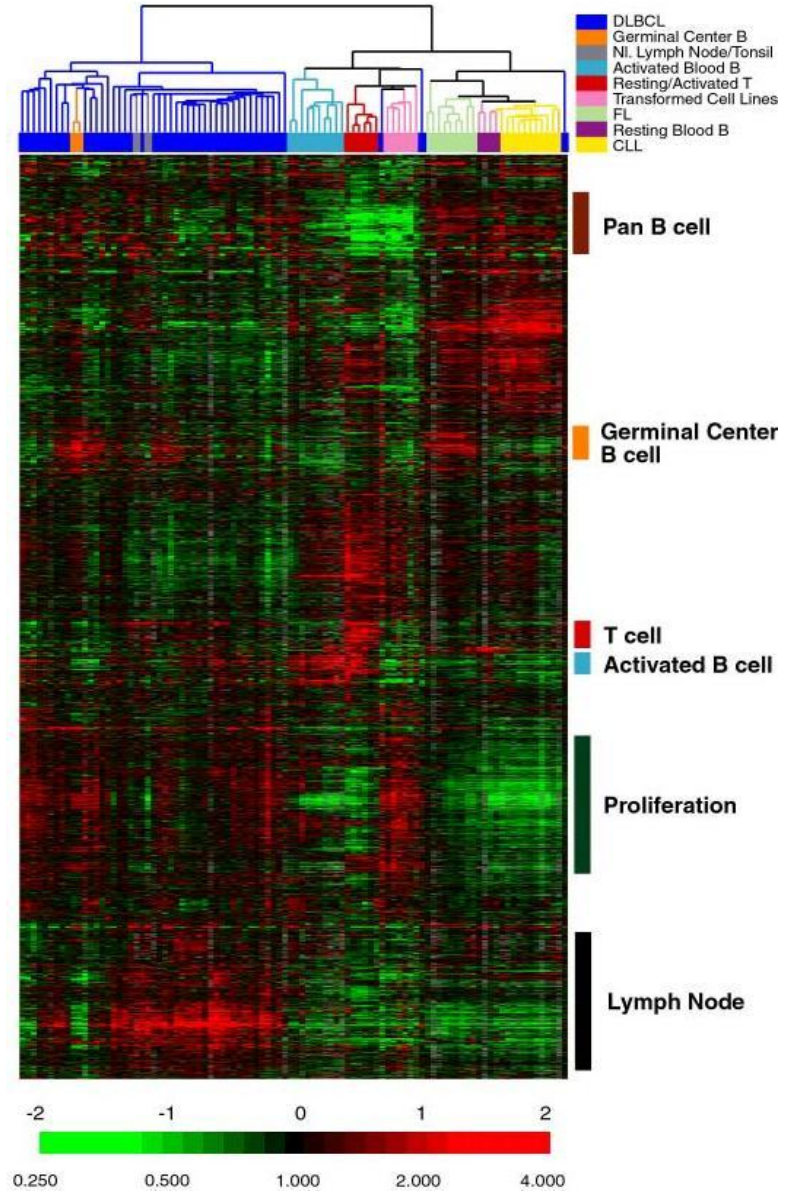
# Sudden infant death syndrome



# Microarrays



Microarray chip



# In Silico project: Integration with visualisation and analysis tools

**GenePattern**

Curated biological  
Smoker

	No	Yes	Description
	Red	Yellow	
	Blue	Red	angiogenin, ribonuclease, RNase A
	Blue	Red	melanoma antigen family D, 1
	Blue	Red	NAD(P)H dehydrogenase
	Blue	Red	CAP, adenylate cyclase
	Blue	Red	WAP four-disulfide core domain
	Blue	Red	histone cluster H1
	Blue	Red	homogentisate 1,2-dioxygenase
	Blue	Red	pirin (iron-binding protein)
	Blue	Red	family with sequence similarity to claudin 10
	Blue	Red	claudin 10
	Blue	Red	transcobalamin II
	Blue	Red	carboxyl dehydrogenase
	Blue	Red	polase do
	Blue	Red	related
	Blue	Red	Inha (gl

**Excel**

NUMBER	SUB-ARRAY	GENE	log ratio	mean (log)	D.F.	S.D.	T-TEST	P-VALUE
1	1	pooled me	-0.30767	0.182282	3	0.707056	0.515608	0.64
2	1	pooled me	-0.43044	0.081927	3	0.492659	0.332591	0.76
3	1	salmon sp	na	na	na	na	na	na
4	1	luciferase	na	na	na	na	na	na
5	1	salmon sp	na	na	na	na	na	na
6	1	salmon sp	na	na	na	na	na	na
7	1	salmon sp	na	na	na	na	na	na
8	1	salmon sp	na	na	na	na	na	na
9	1	salmon sp	na	na	na	na	na	na
10	1	salmon sp	na	na	na	na	na	na
11	1	salmon sp	na	na	na	na	na	na
12	1	salmon sp	na	na	na	na	na	na
13	1	salmon sp	na	na	na	na	na	na
14	1	salmon sp	na	na	na	na	na	na
15	1	salmon sp	na	na	na	na	na	na
16	1	salmon sp	na	na	na	na	na	na
17	1	salmon sp	na	na	na	na	na	na
18	1	salmon sp	na	na	na	na	na	na
19	1	salmon sp	na	na	na	na	na	na
20	1	salmon sp	na	na	na	na	na	na

**IGV**

**Integr. Gen. View**

**R/Bioconductor**

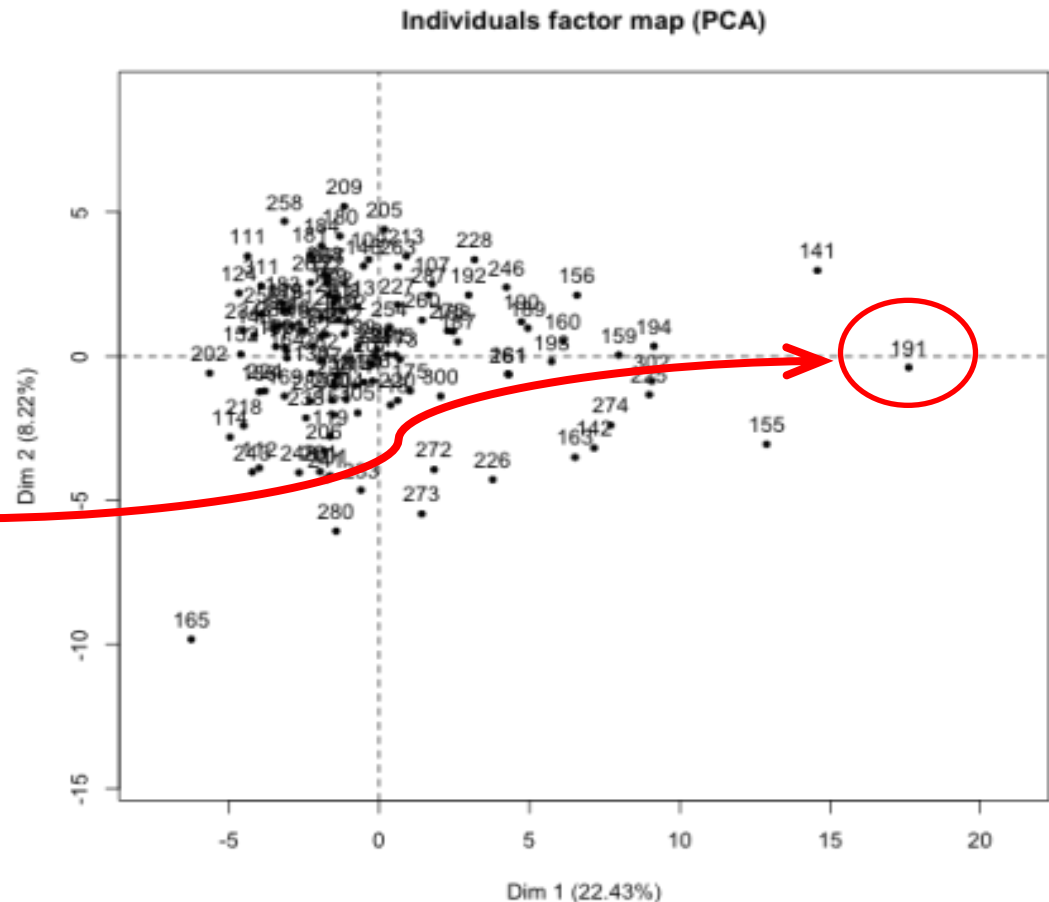
**Bioconductor**  
OPEN SOURCE SOFTWARE FOR BIOINFORMATICS

**2591 tracks loaded** **89M of 101M**



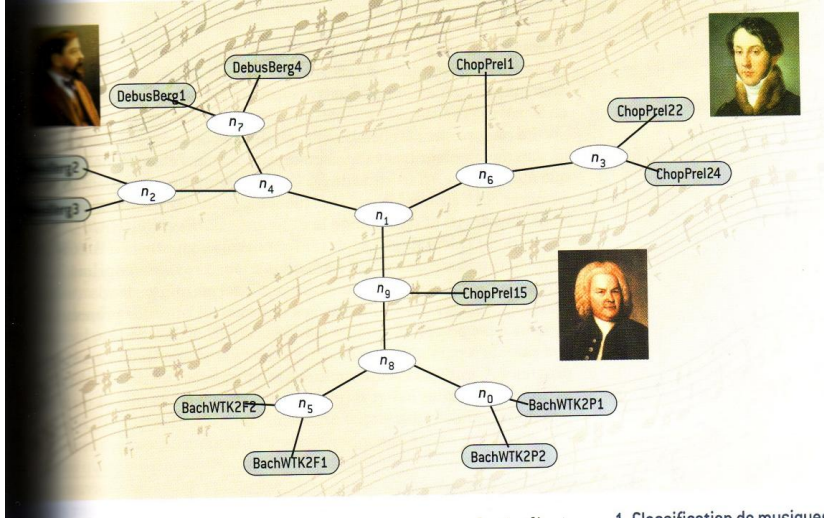
# SMART : detection of outlier clinical site

- Real example
  - Known fraud in center 191
- SMART analysis
  - 191 is an outlier
- Other centers?
  - 141, 155, 165?
  - Most frauds are undetected by current methods



Summary through PCA of a SMART analysis

# The future of it: More and more free documents with various contents and various own structuration



## Art Mining:

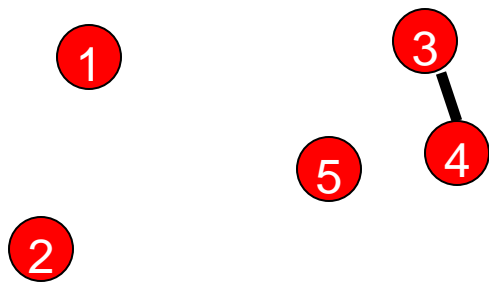
- images
- musics
- movies



# Exemple of clustering: hierarchical clustering

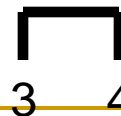
## Algorithm

- • *Join the two closest elements.*
- Update the distance matrix.



Closest : 3 et 4

	1	2	3	4	5
1	0	10	15	18	12
2		0	23	22	13
3			0	4	6
4				0	5

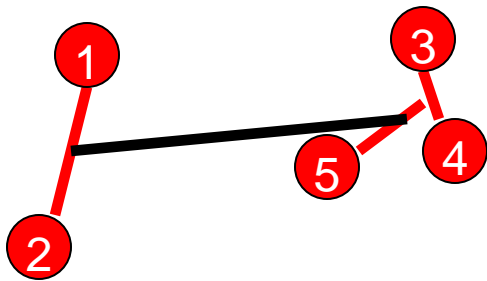


Distance matrix

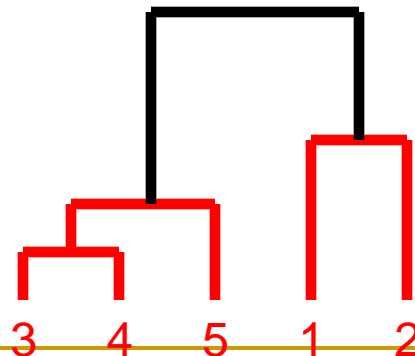
# Hierarchical clustering

## Algorithm

- • *Join the two closest elements.*
- Update the distance matrix.



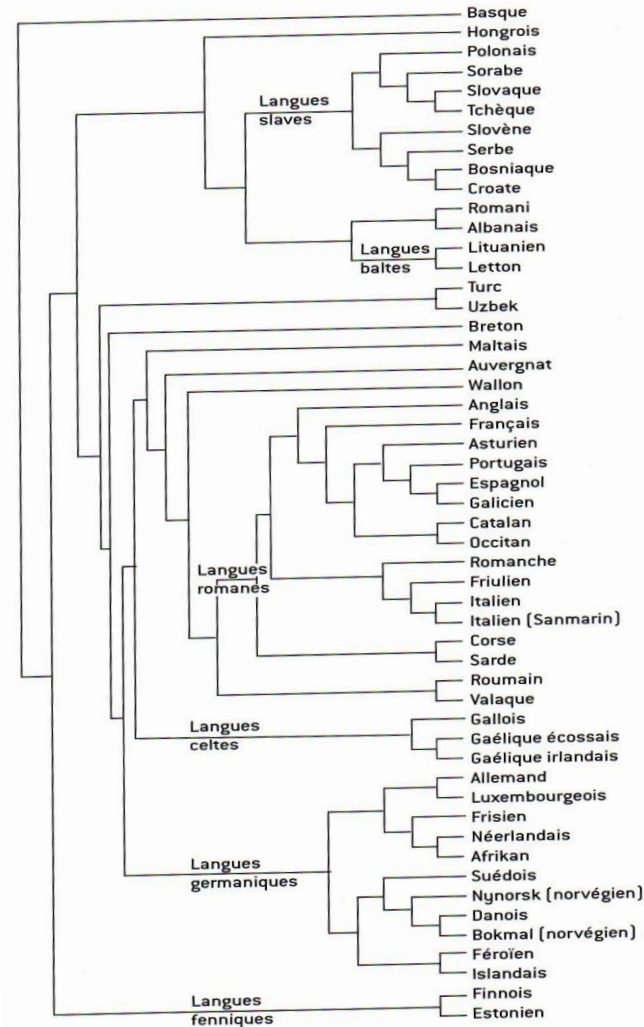
Closest : (1,2) et (3,4,5)



# Similarity based on compression algorithm

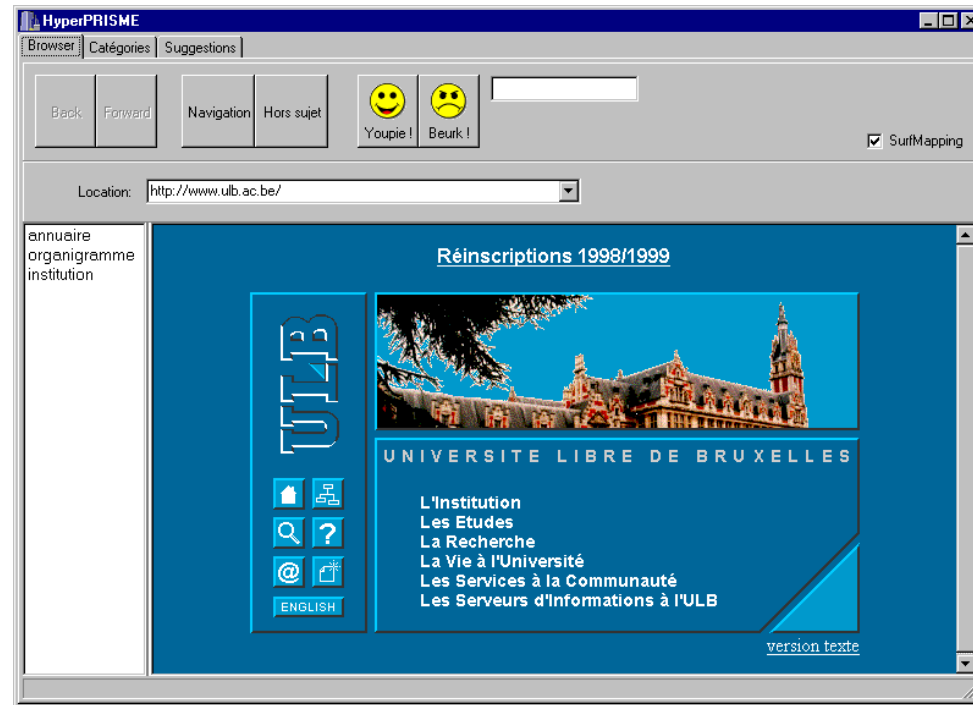
- Suppose two documents A and B
- Compute length of compressing A:  $C(A)$
- Compute length of compressing B:  $C(B)$
- Compute length of compressing AB:  $C(AB)$
- Similarity  $(A,B) = 1 - [C(A) + C(B) - C(AB)] / C(A)$   
if  $C(A) \geq C(B)$

# Similarity between natural languages



# Web Mining

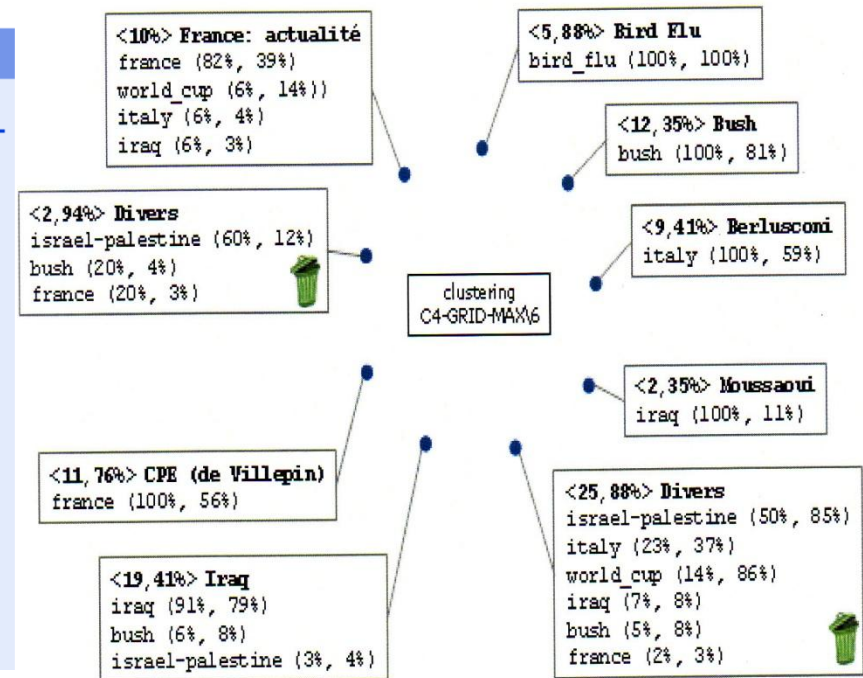
- The Hyperprisme project
- Spy the user and mine his clickstream
- Automatic profiling of users
  - Key words: positif, negatif,...
- Automatic grouping of users on the basis of their profiles



# Text Mining: still a lot of possible improvements

Table III Term-document matrix

Term	Doc1	Doc2	Doc3	Doc4	Doc5	Doc6
Passenger traffic volume	1	1	0	5	2	0
Decrease	1	2	1	0	0	0
Increase	0	2	0	0	0	0
Passengers carried	5	1	0	0	0	0
Personal traffic tools	1	0	0	0	0	0
Grow up	4	1	6	0	0	0
Million	4	1	0	0	0	0
Hundred	0	0	0	0	1	0
FAST rapid transit system	0	2	0	0	0	0
Finished	0	1	0	0	0	0
A1 station	0	0	0	5	4	4
B1 station	0	0	0	1	5	0
C1 station	0	0	0	1	0	0
D1 station	0	0	0	1	0	1
E1 station	0	0	0	1	0	2
Passenger-Kilometers	0	1	7	0	0	0
Columniation	0	0	0	0	2	0
Check the number	0	0	0	0	2	0
Ticket Revenues	0	0	0	0	0	7



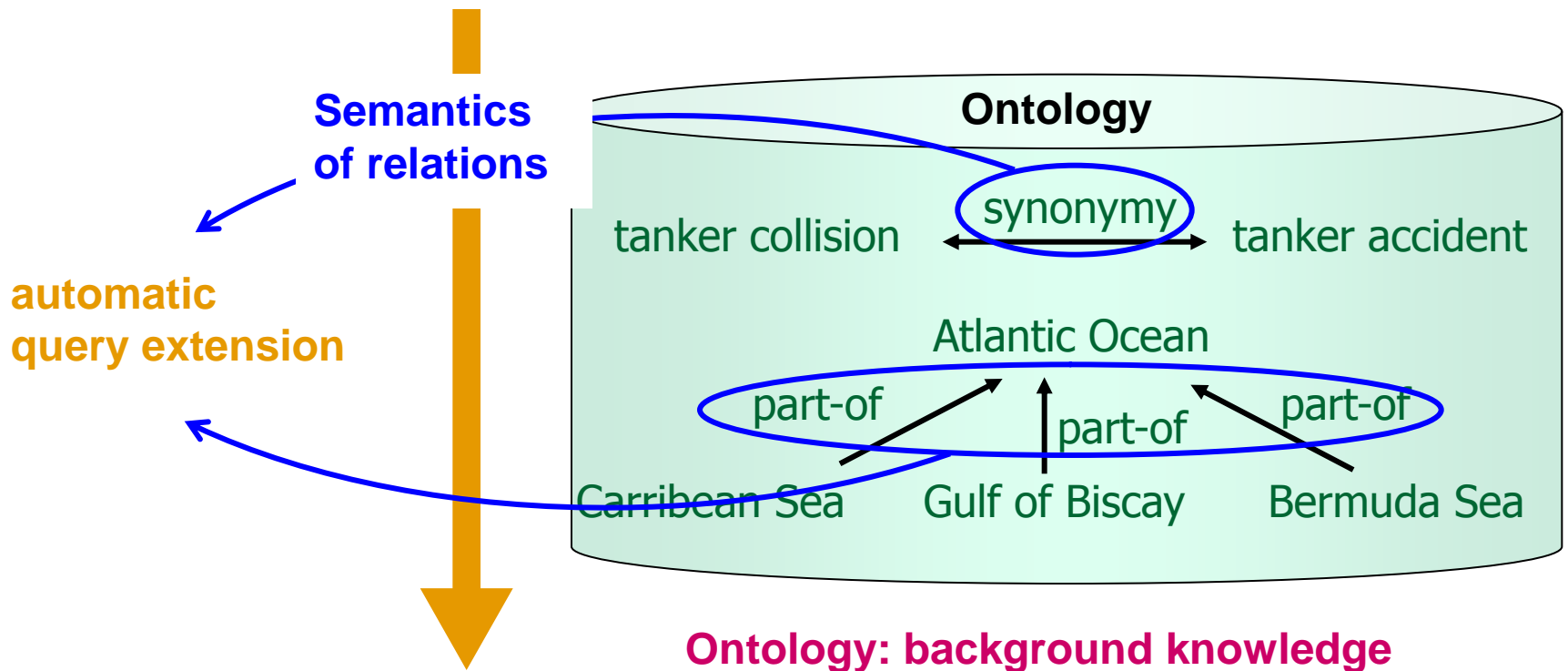


# Semantic enrichment

Using background knowledge to extend query

“tanker accident” atlantic

Search



(tanker collision OR tanker accident) AND

(Atlantic Ocean OR Carribean Sea OR Bermuda Sea OR ...)

---

# Exploit the structure of the documents

Like for XML for instance

```
<Course>
```

```
  <title> Software technologies </title>
```

```
  <teacher> Bersini </teacher>
```

```
  <themes>
```

```
    <name> programming technique </name>
```

```
    <name> data representation </name>
```

```
    <name> data mining </name>
```

```
  </themes>
```

```
</Course>
```

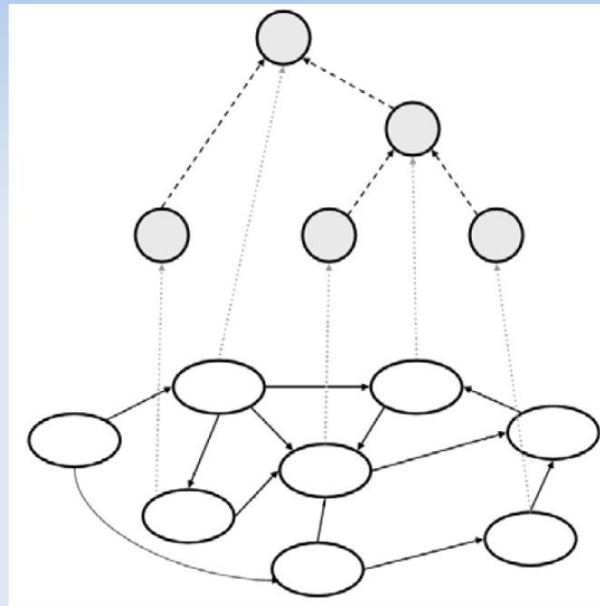
Exploit the graph structure of XML + the content between the tags

---

# We are working on Wikipedia

## The Nature of Wikipedia

- Wikipedia is a combination of two interconnected graphs
  - A directed graph with the regular pages as nodes and the links between pages as edges
  - An acyclic directed graph with the category pages as nodes and their connections as edges
- The main regular page graph consists of ~ 3 650 000 nodes and the category graph of ~ 700 000 nodes (last count)

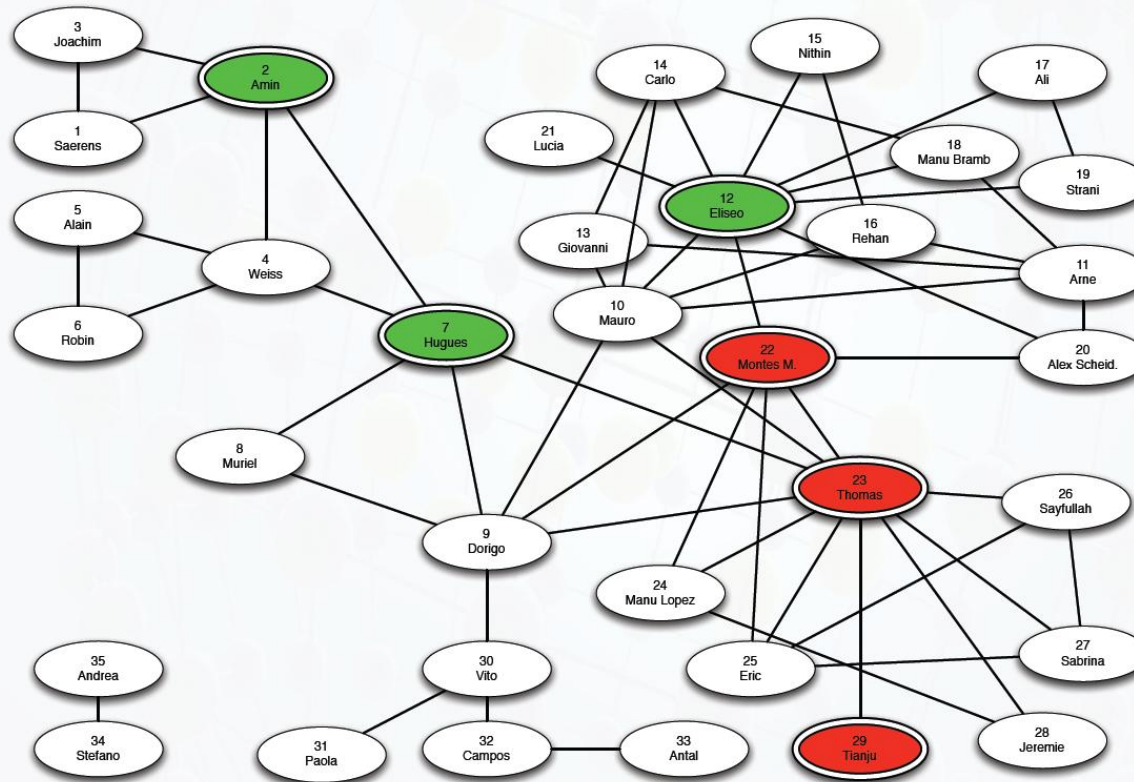


# Graph Mining

Introduction and Context  
Betweenness and Covariance  
Classification of Nodes  
Conclusion and Perspectives

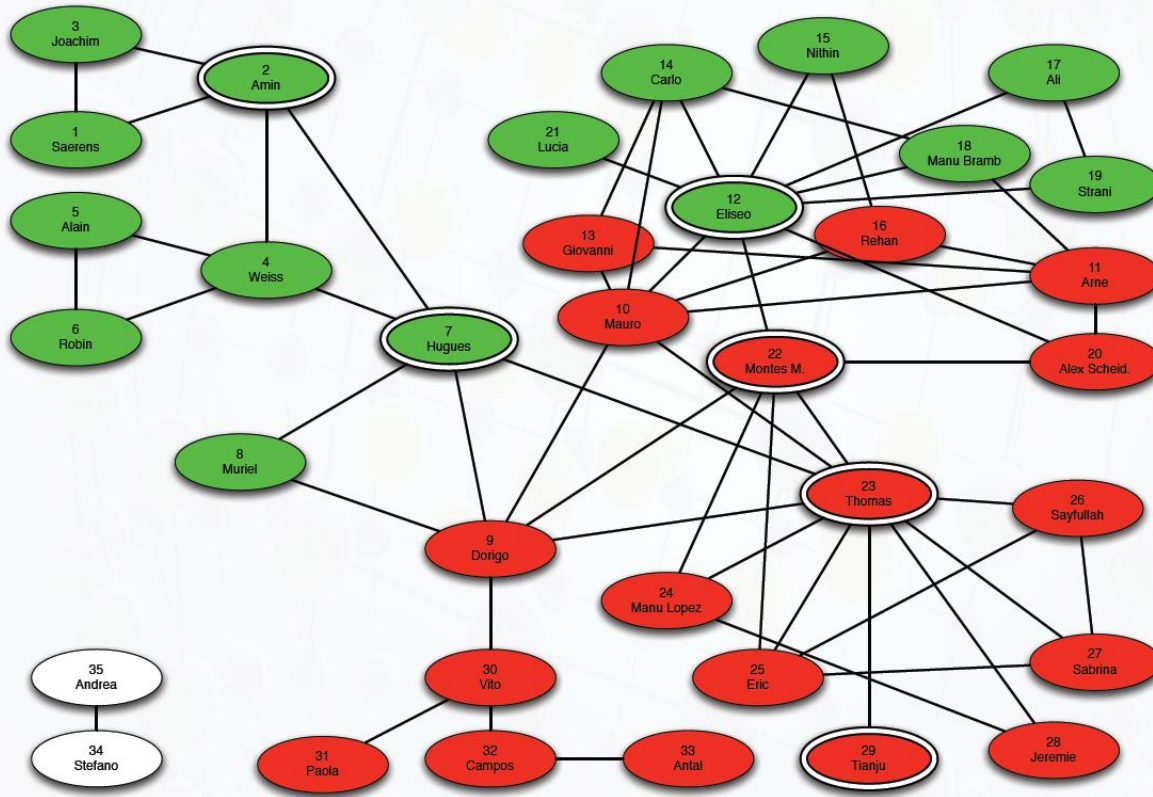
Introduction  
Algorithms  
Experiments

## Application to Classification



Let us classify all the nodes.

# Application to Classification



Let us classify all the nodes.

# Combine different types of information: graph and text

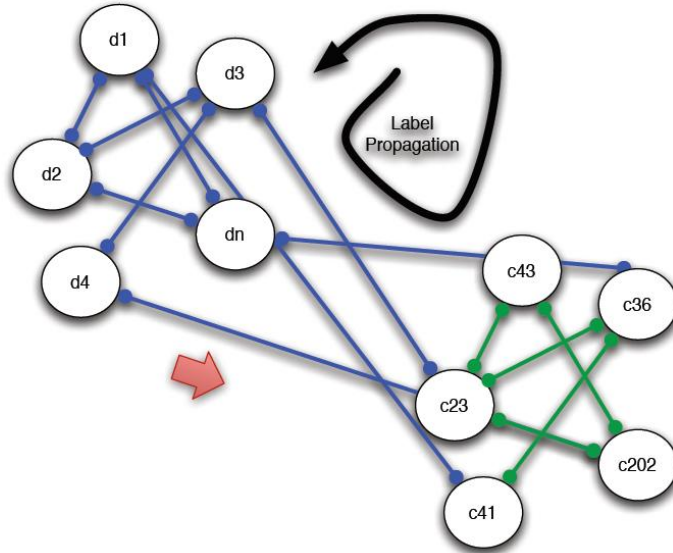
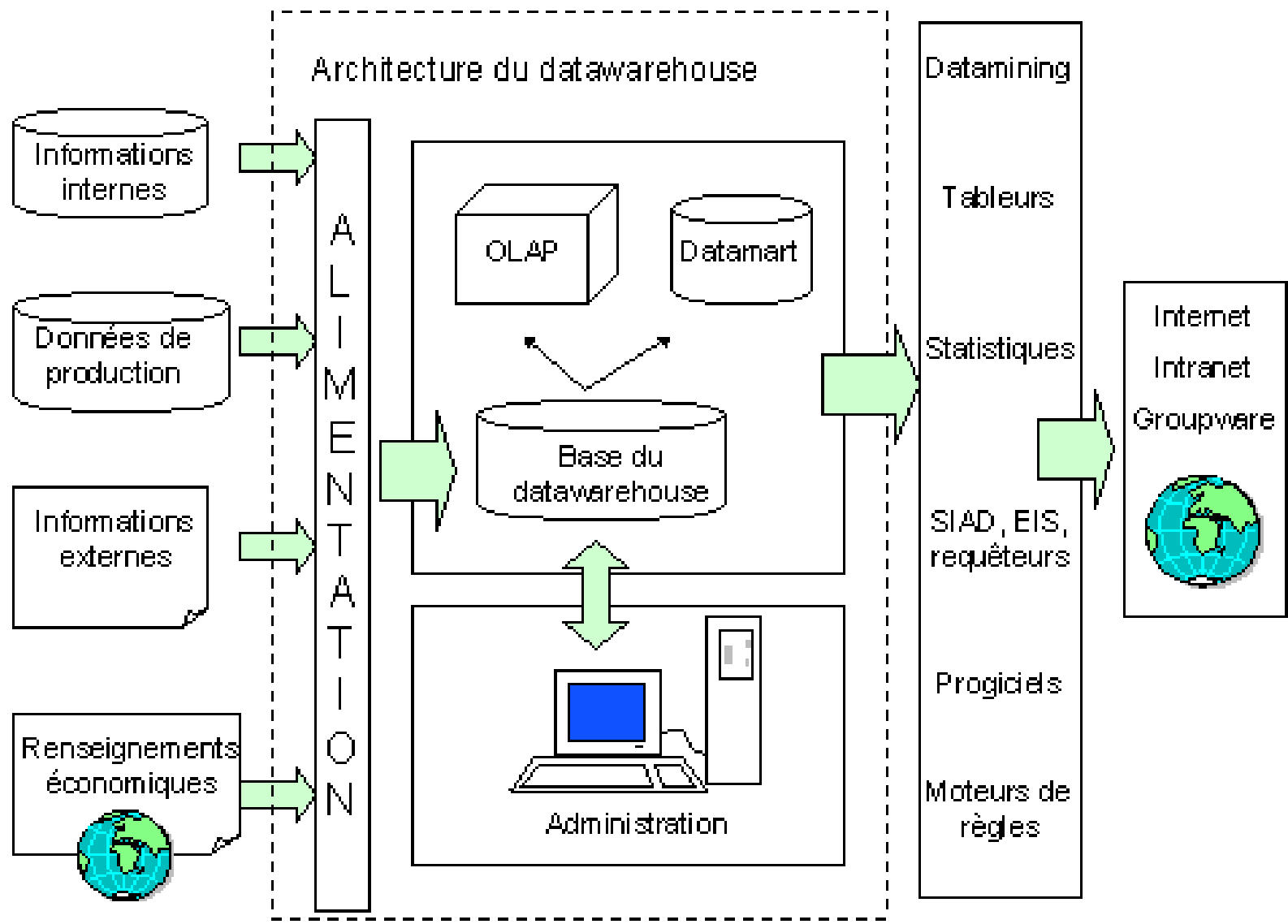


Figure 10: The document nodes has been connected to an external preexisting citation network through inferred  $k$  nearest neighbors links (i.e. in blue). The goal is to propagate labels from the citation graph to the just connected documents.

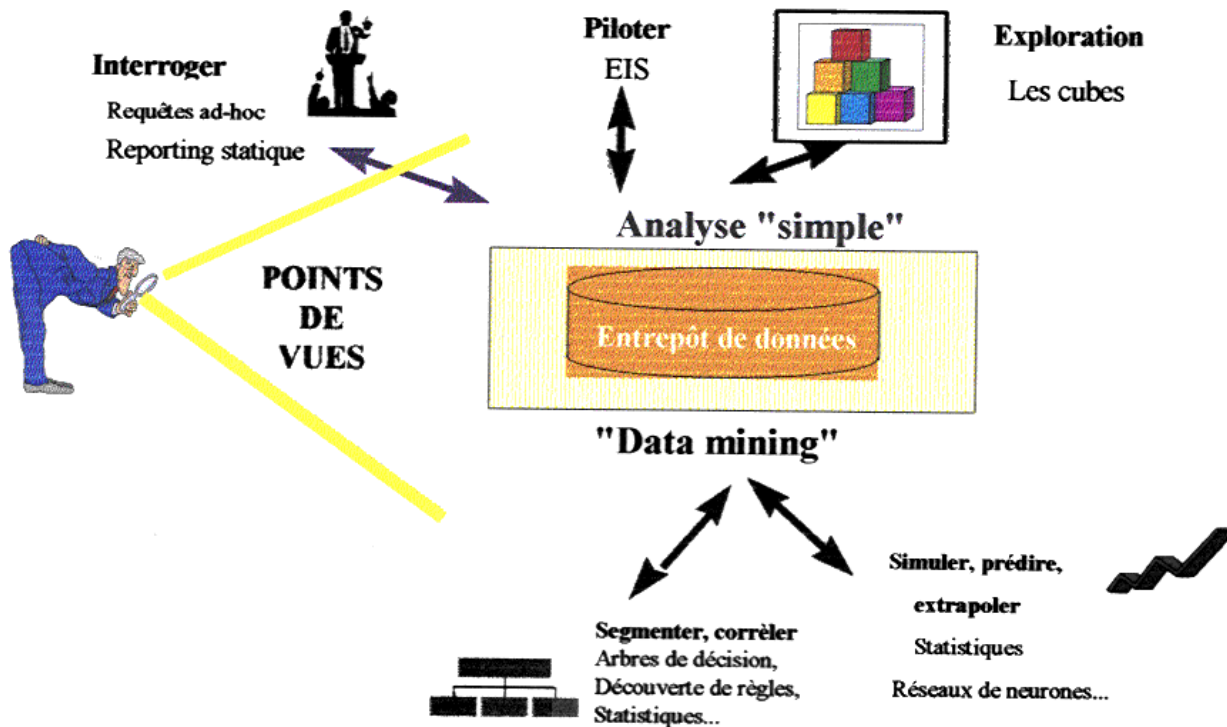
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# Data Warehousing

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Source : *Le Data Warehouse –Le Data Mining*, Eyrolles, Paris, p. 40

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# Réorganisation des données

- Orientées sujet
  - intégrées
  - transversales
  - historisées
  - non volatiles
  - Des données productions ---> données décision
-

	Environnement transactionnel	Data Warehouse
Type d'utilisateurs	Font tourner les roues de l'entreprise	Vérifient si les roues de l'entreprise tournent bien
Définition de système performant	Système performant = système rapide	Notion de performance est liée au degré de prévisibilité d'une requête
Volumes manipulés	Faible	Elevé
Type d'accès	Lecture/écriture : la donnée est modifiée en ligne	Chargement par batch, mises à jour interdites car les données sont des clichés issus des systèmes de production
Types de données stockées	Dynamiques : mises à jour fréquente	Statique, évolution par chargement
Gestion des redondances	Est évitée car elle pose des problèmes d'incohérence de données	Redondance peut être nécessaire pour optimiser les performances → pas de problème de cohérence car la donnée de base est déjà une copie
Domaine couvert	Modèle le plus souvent propre à une application	Rôle transversal dans l'entreprise et organisé par sujet
Mode d'accès et conséquence sur le modèle de données	Par l'intermédiaire d'application ; le modèle de données n'est visible que par l'utilisateur qui ne voit le système qu'à travers des applications qu'il utilise → le modèle de données peut être complexe	Directe ou légèrement masquée par un outil d'aide à la décision → le modèle doit être simple
Type de requête	Simple car prévisibles → le modèle de données est conçu pour éviter les requêtes trop complexes. La plupart des requêtes s'appuient sur un index, d'où des temps de réponses proportionnels au volume stocké. Les performances sont stables car toutes les requêtes sont prédéfinies	Complexe, surtout si l'utilisateur est autonome. Il est quasiment impossible de garantir que tous les accès passeront par les index : le temps de réponse peut dépendre du volume stocké et pas seulement du volume associé au résultat de la requête
Horizon temporel	Court	Long
Nombre et type d'accès	Réguliers et prévisibles	Très irréguliers et imprévisibles
Volume	Rarement supérieure à la dizaine de gigas	Supérieur car historisation

**TABLE DES METRIQUES (FAITS)**

<b>PRODUIT</b>
Id-prod
Nom
Gamme
Resp
Coût unitaire
Couleur

<b>FOURNISSEUR</b>
Id-fourn
Nom
Dept
Type
Nationalité
...

<b>PERIODE</b>
JJ MM YYYY
Jour-sem
semaine mois
semaine
trimestre
semaine année
mois

<b>Ventes</b>
Id-prod
Id-fourn
JJ MM YYYY
Id-client
<b>CA</b>
<b>Marges</b>
<b>Unités</b>
...

<b>CLIENT</b>
Id-client
Nom
tel
région
...

**DIMENSIONS**

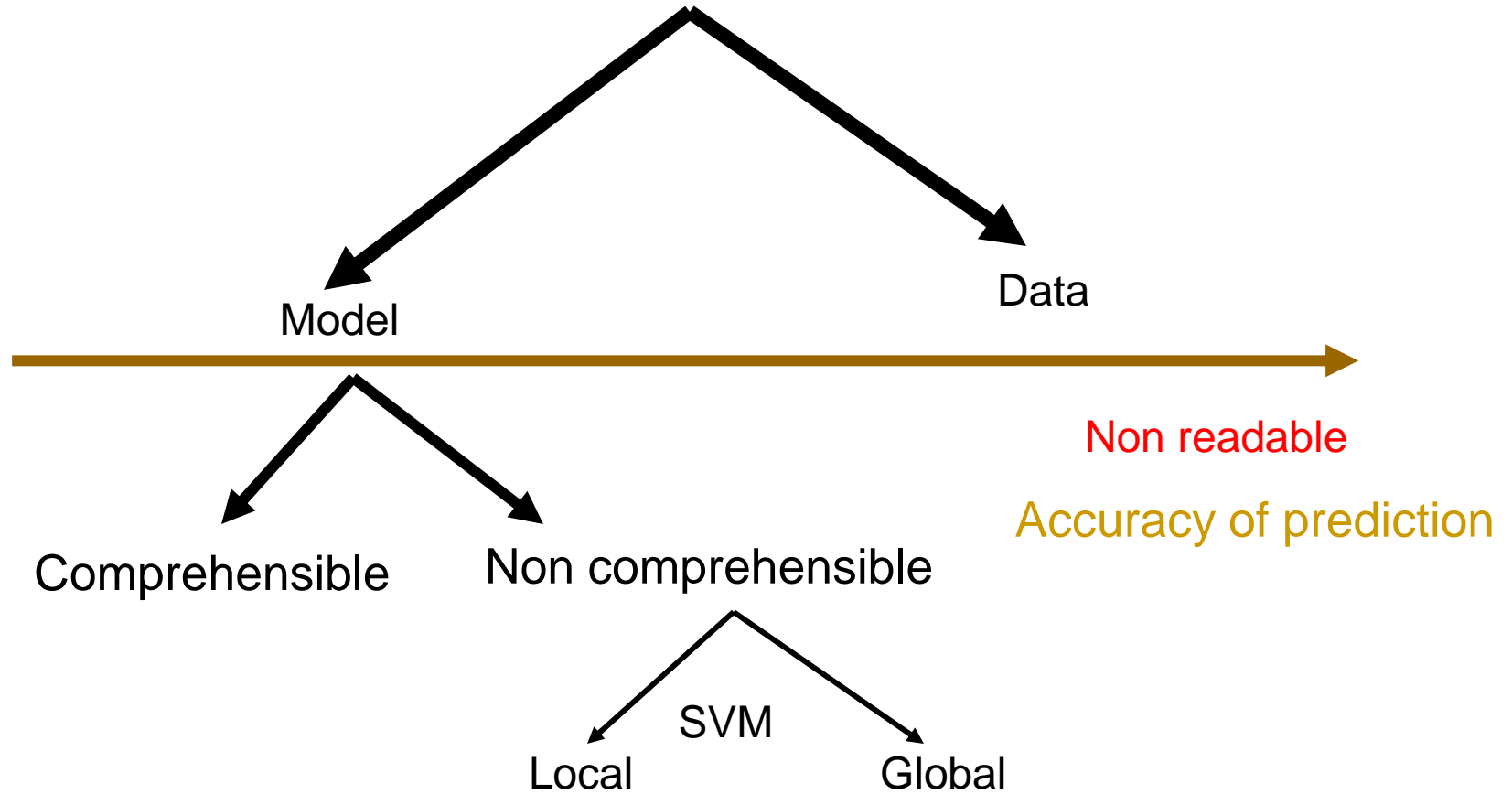
**Métriques**

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# Model-based vs Data-based

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# Different approaches

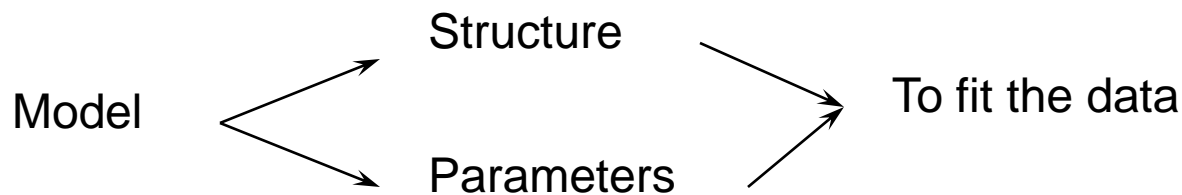


# Understanding and Predicting



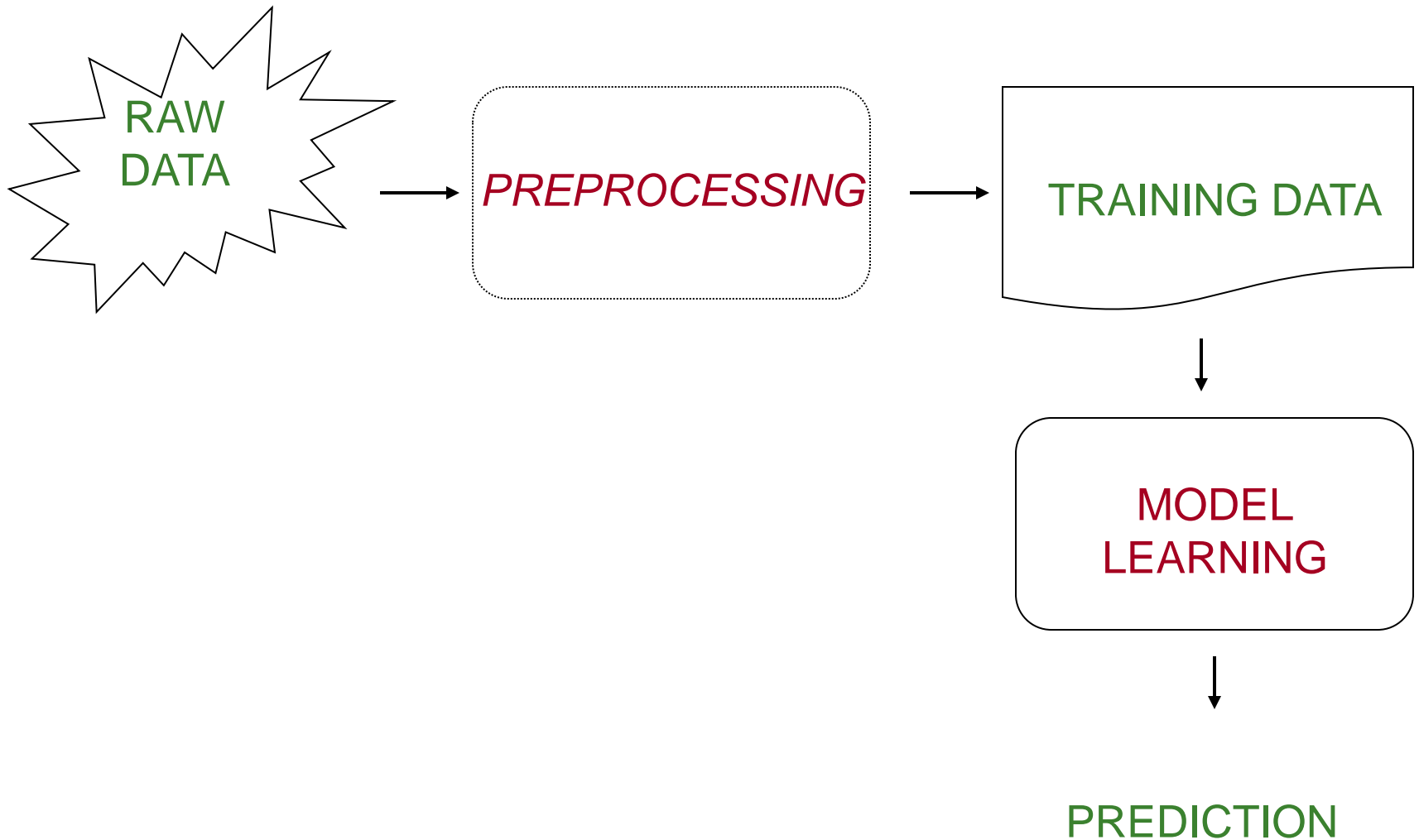
## Building Models

A model needs data to exist but, once it exists, it can exist without the data



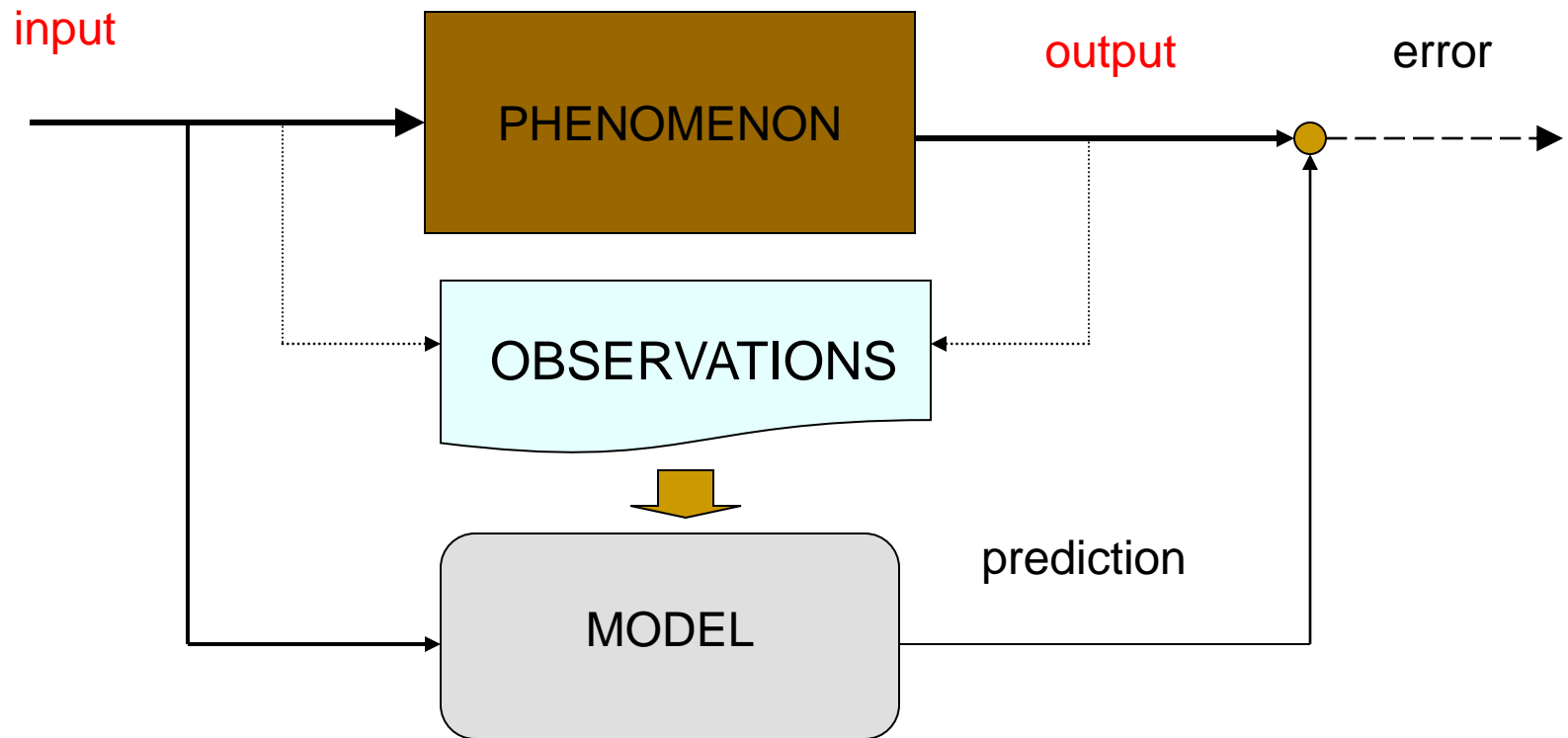
Linear, NN, Fuzzy, ID3, Wavelet, Fourier, Polynomes,...

# From data to prediction



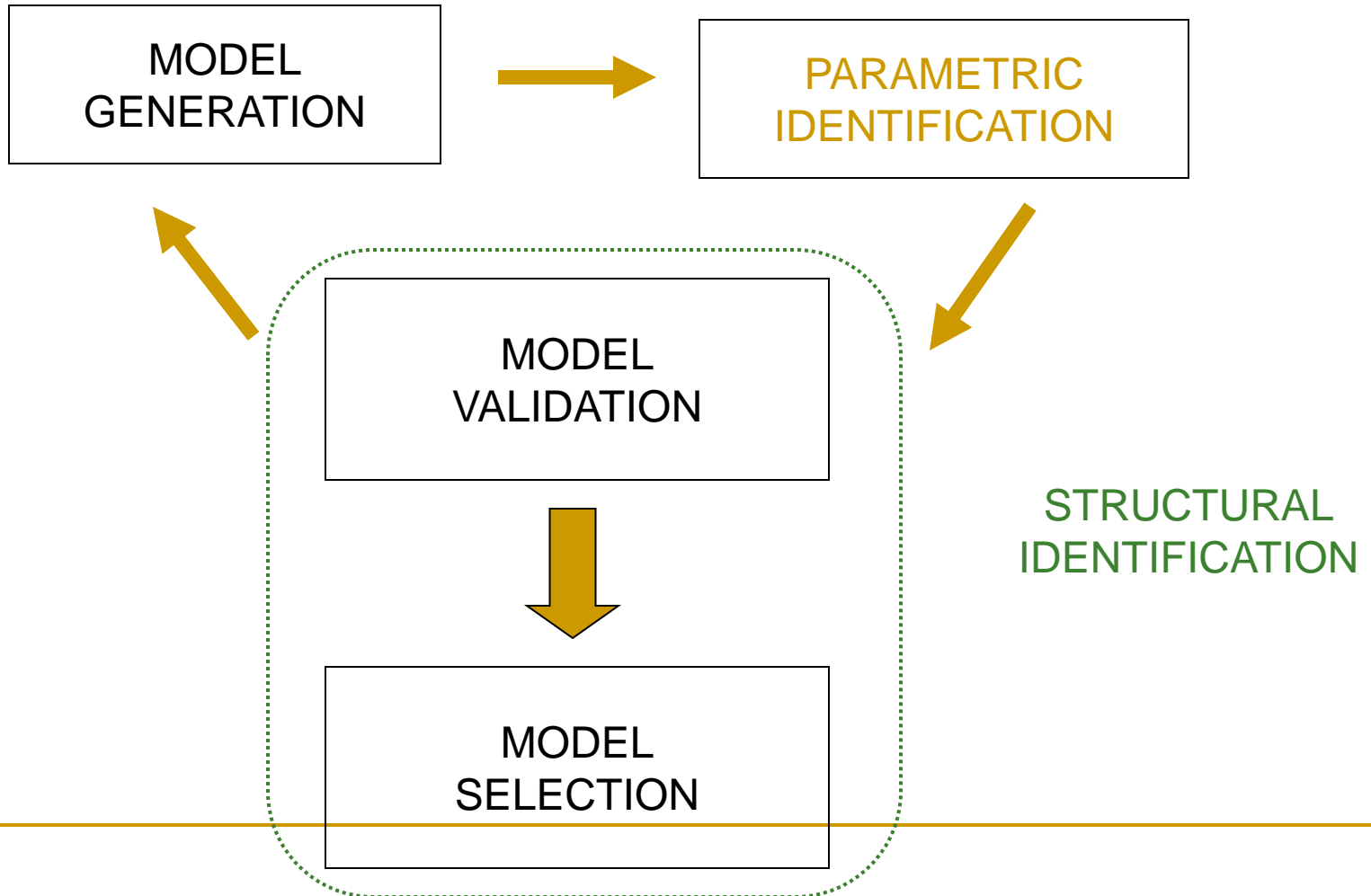


# Supervised learning

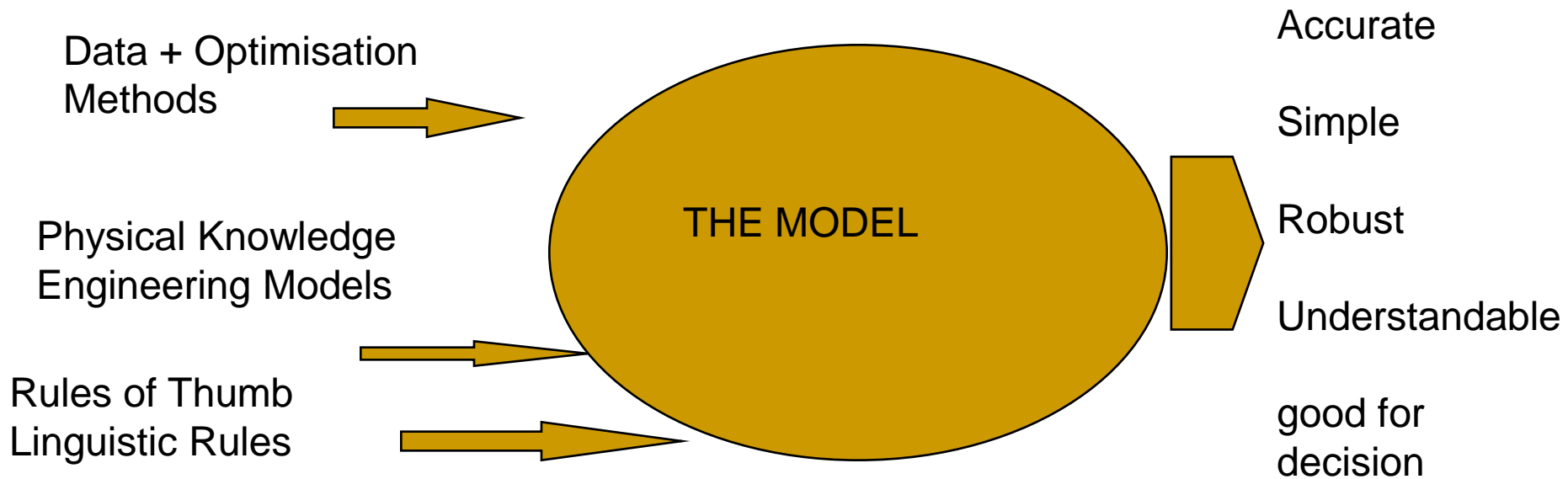


- **Finite** amount of **noisy** observations.
- **No a priori knowledge** of the phenomenon.

# Model learning



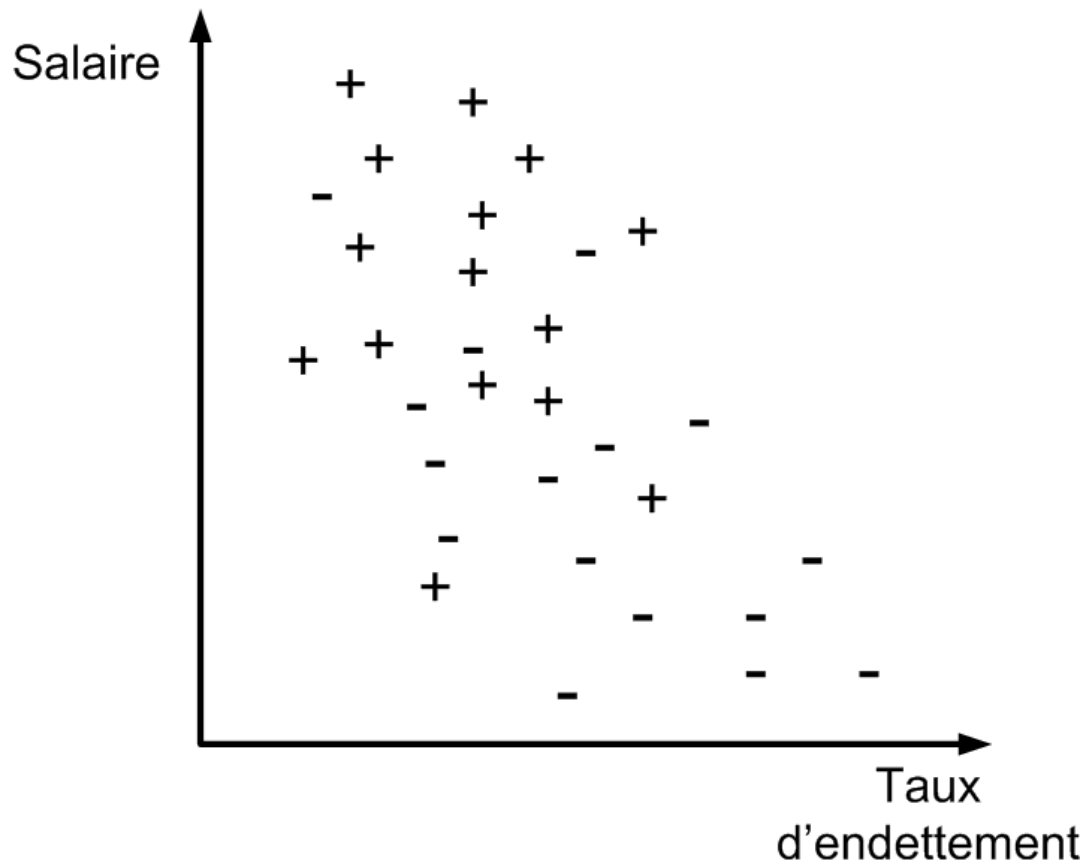
# The Practice of Modelling

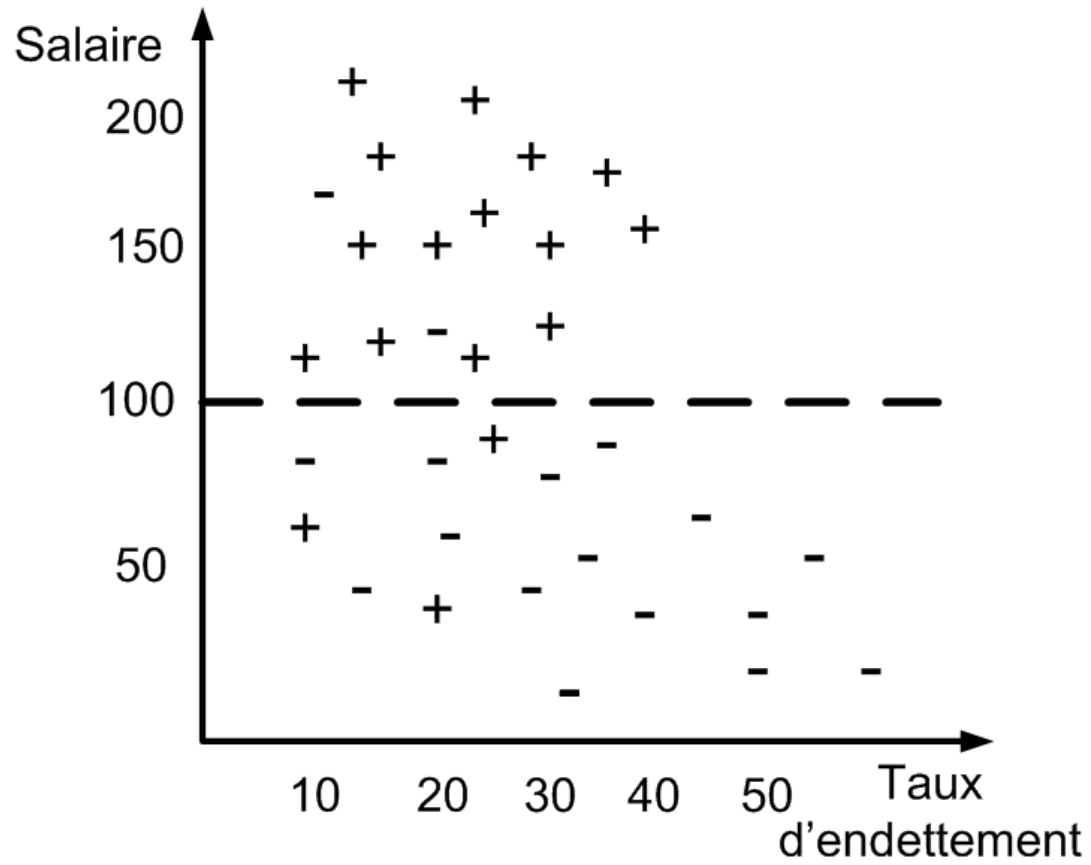


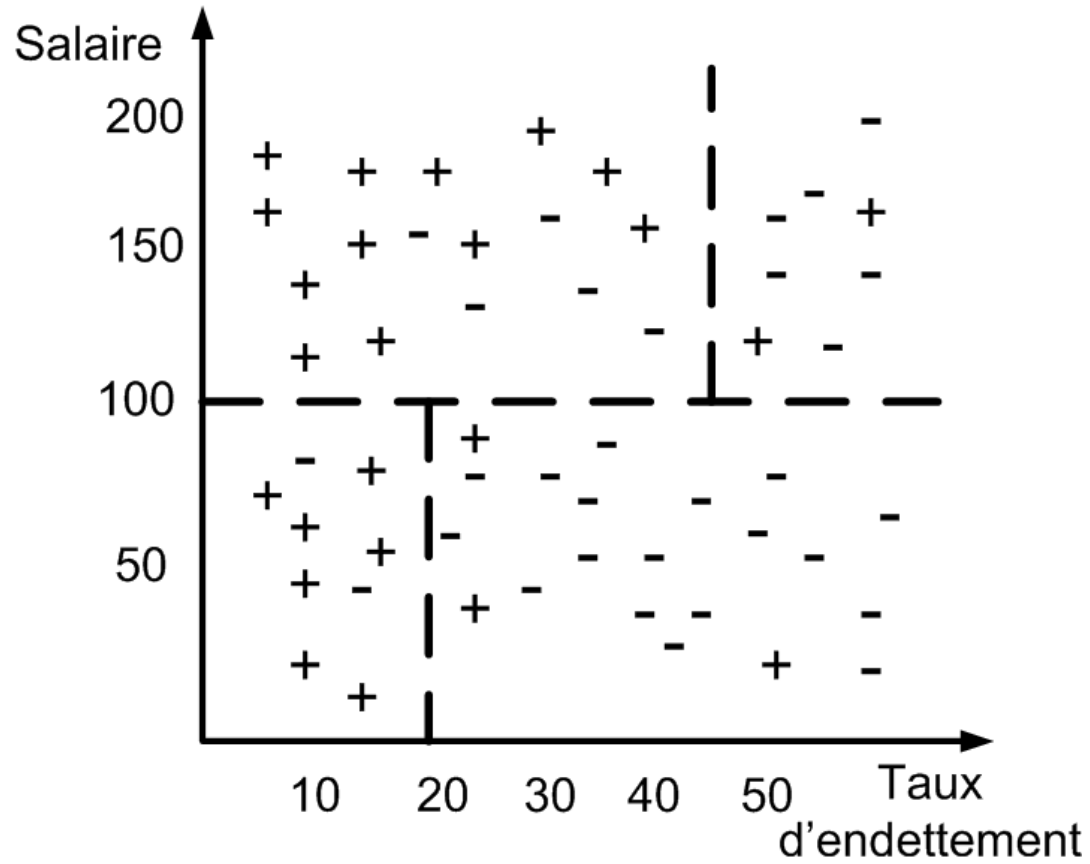
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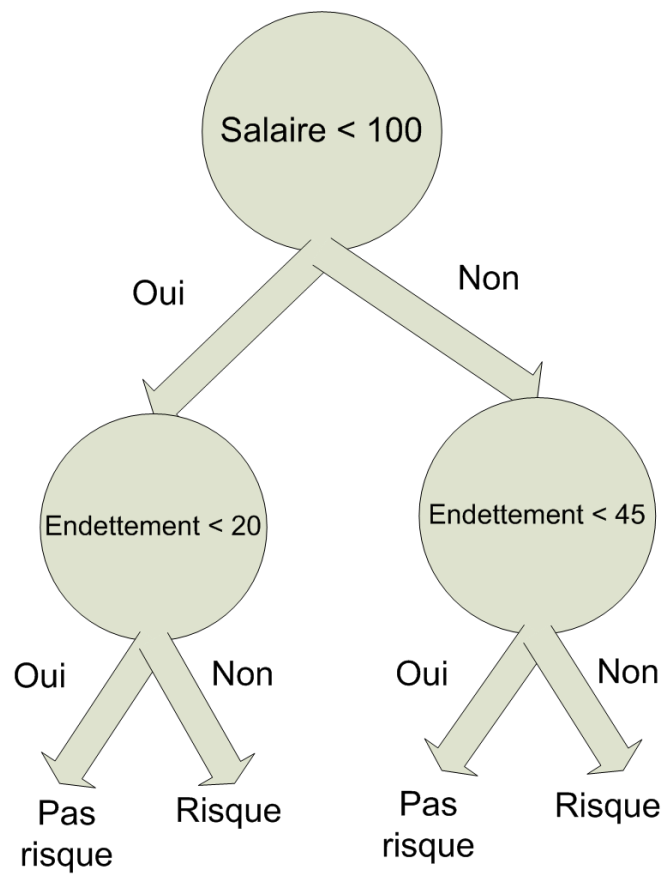
# Comprehensible models

- Decision trees
  - Qualitative attributes
  - Force the attributes to be treated separately
  - classification surfaces parallel to the axes
  - good for comprehension because they select and separate the variables
-











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# Decision trees

- Very used in practice. One of the favorite data mining methods
  - Work with noisy data (statistical approaches) can learn logical model out of data expressed by and/or rules
  - ID3, C4.5 ---> Quinlan
  - Favoring little trees --> simple models
-

- 
- At every stage the most discriminant attribute
  - The tree is being constructed top-down adding a new attribute at each level
  - The choice of the attribute is based on a statistical criteria called : “the information gain”
  - Entropie =  $-p_{oui} \log_2 p_{oui} - p_{non} \log_2 p_{non}$
  - Entropie = 0 if  $P_{oui/non} = 1$
  - Entropie = 1 if  $P_{oui/non} = 1/2$
-

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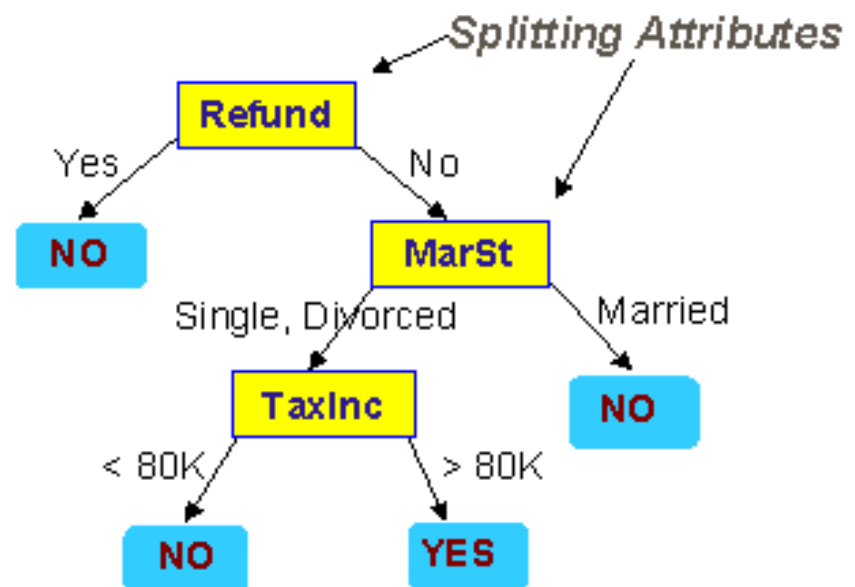
# Information gain

- $S$  = set of instances,  $A$  set of attributes and  $v$  set of values of attributes  $A$
  - $\text{Gain}(S,A) = \text{Entropie}(S) - \sum_v |S_v|/|S| * \text{Entropie}(S_v)$
  - the best  $A$  is the one that maximises the Gain
  - The algorithm runs in a recursive way
  - The same mechanism is reapplied at each level
-

# Example Decision Tree

categorical  
categorical  
continuous  
class

Tid	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

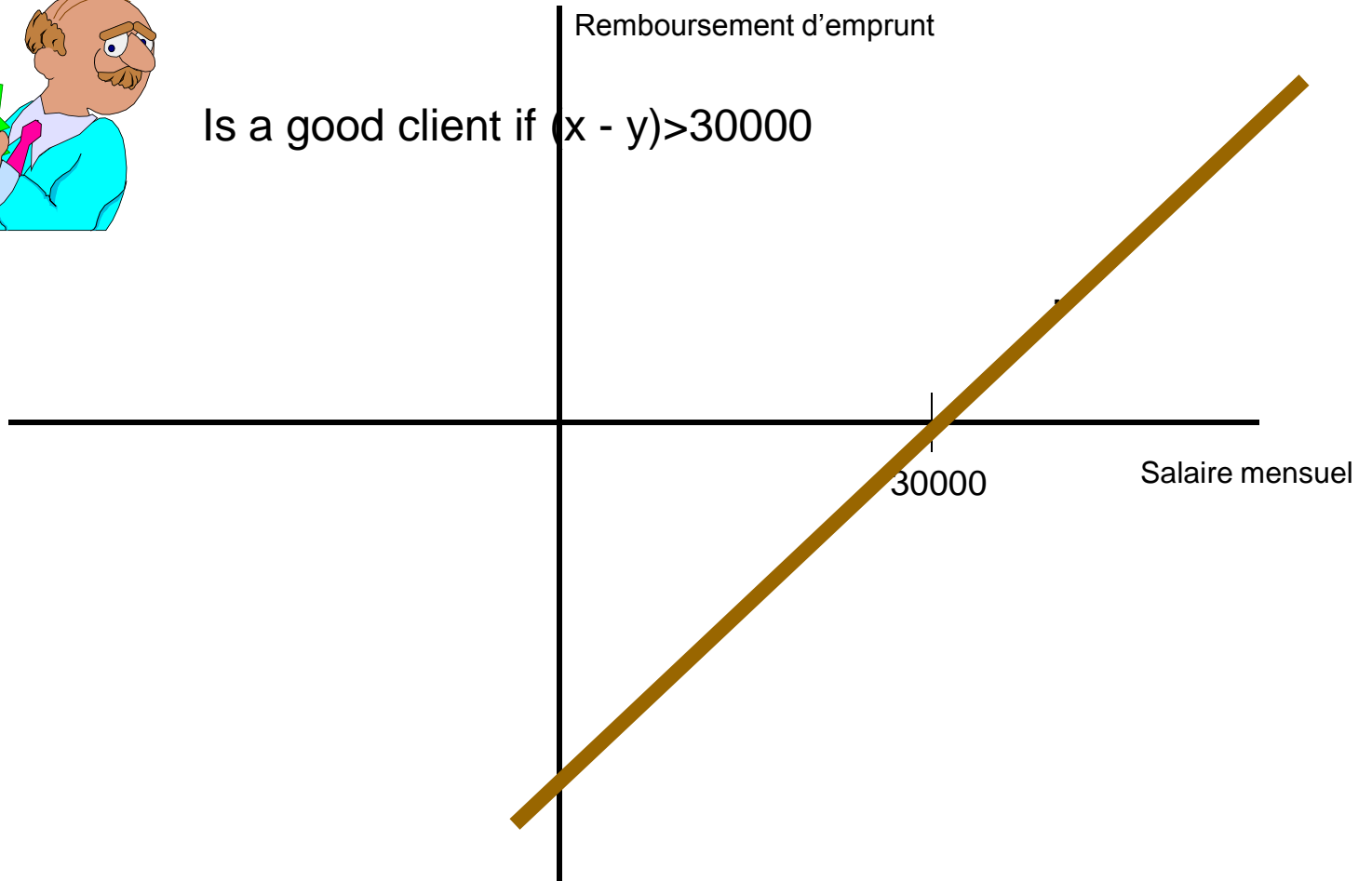


The splitting attribute at a node is determined based on the Gini index.

# BUT !!!!



Is a good client if  $(x - y) > 30000$

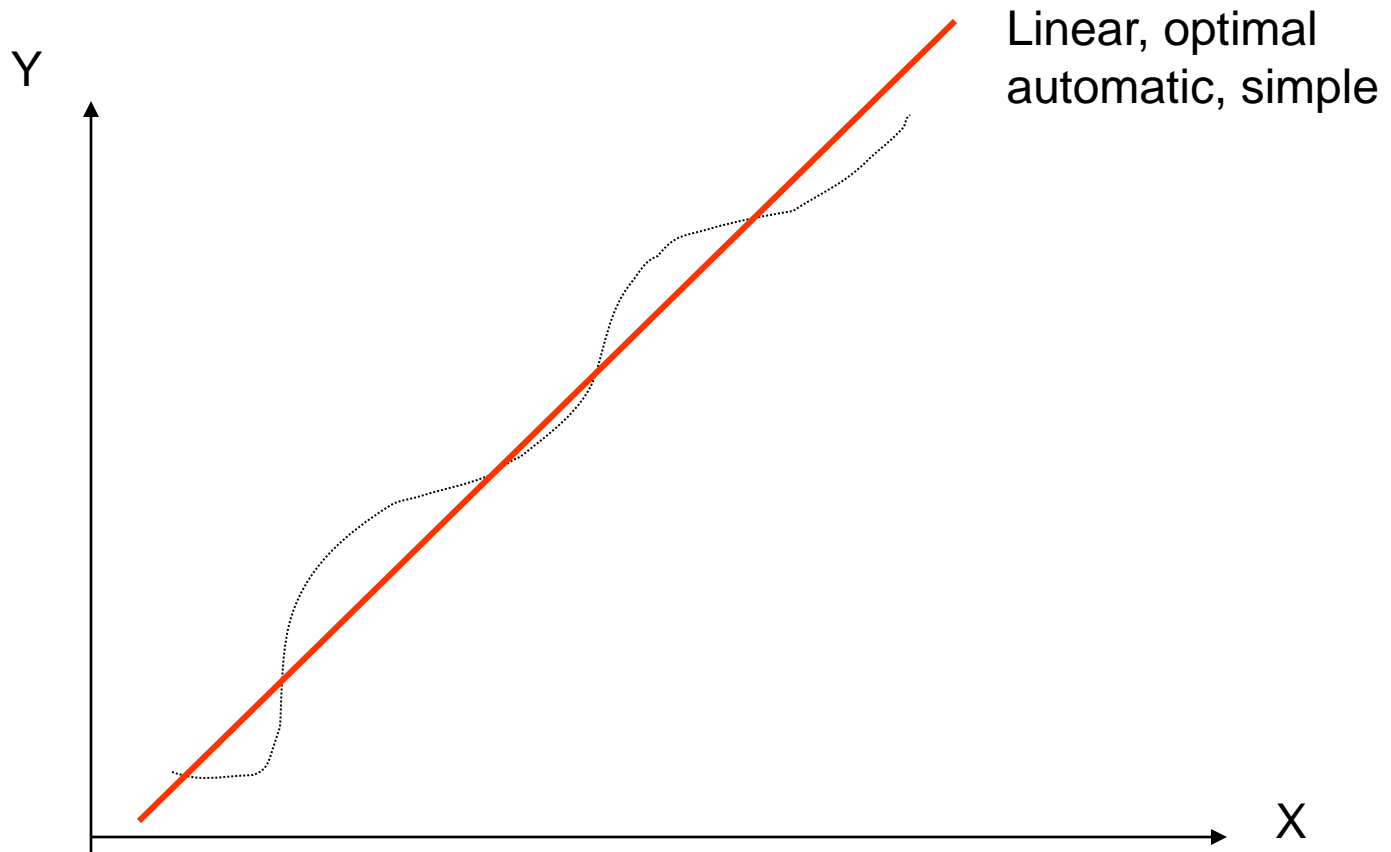


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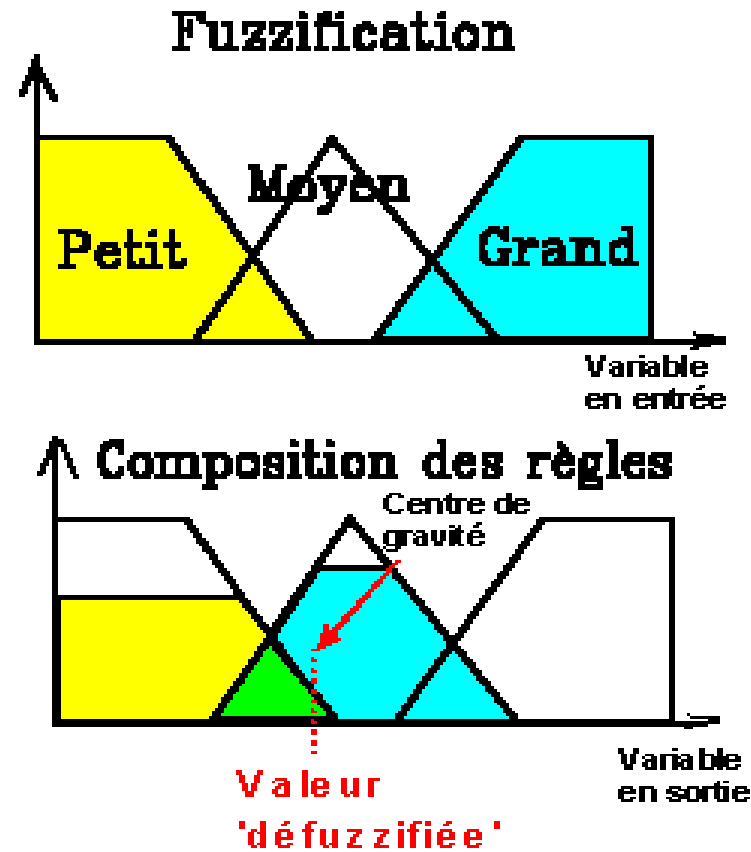
# Other comprehensible models

- Fuzzy logic
- Realize an I/O mapping with linguistic rules
- If I eat “a lot” then I take weight “a lot”

# Trivial example



# The fuzzy





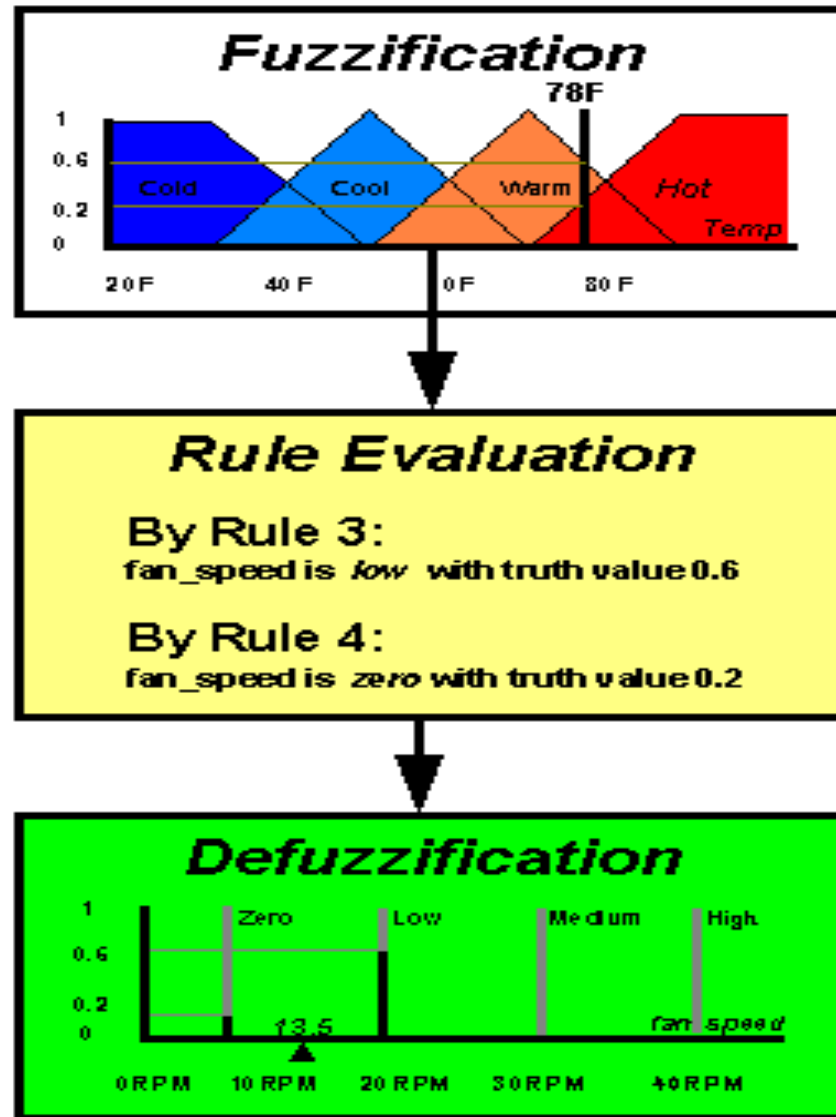
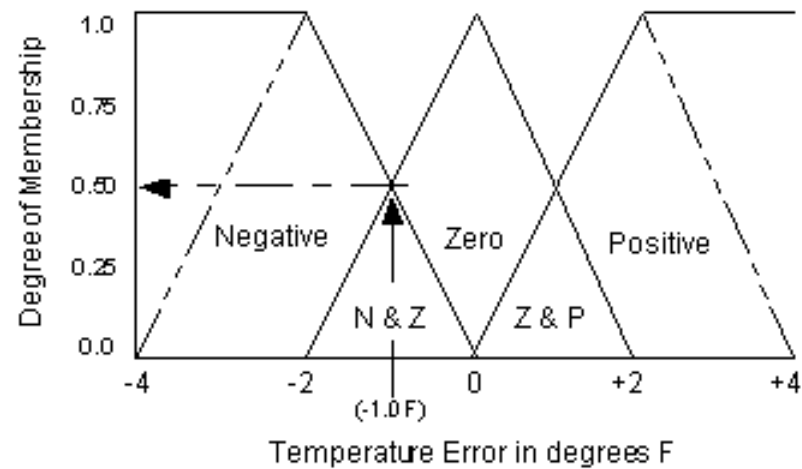
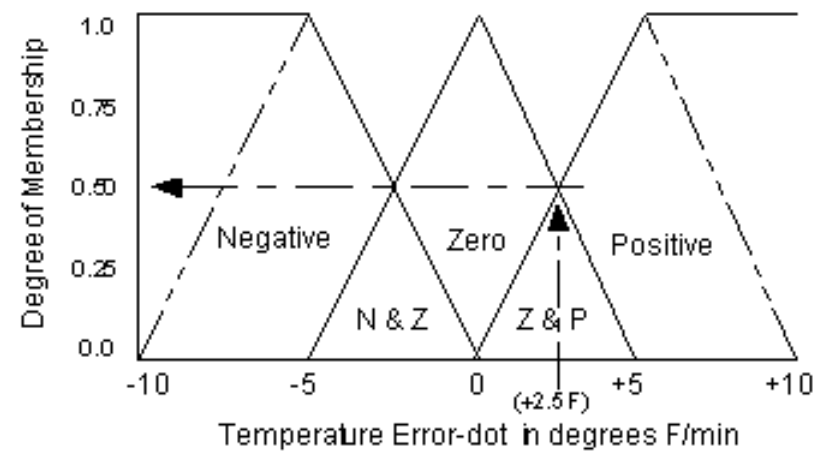


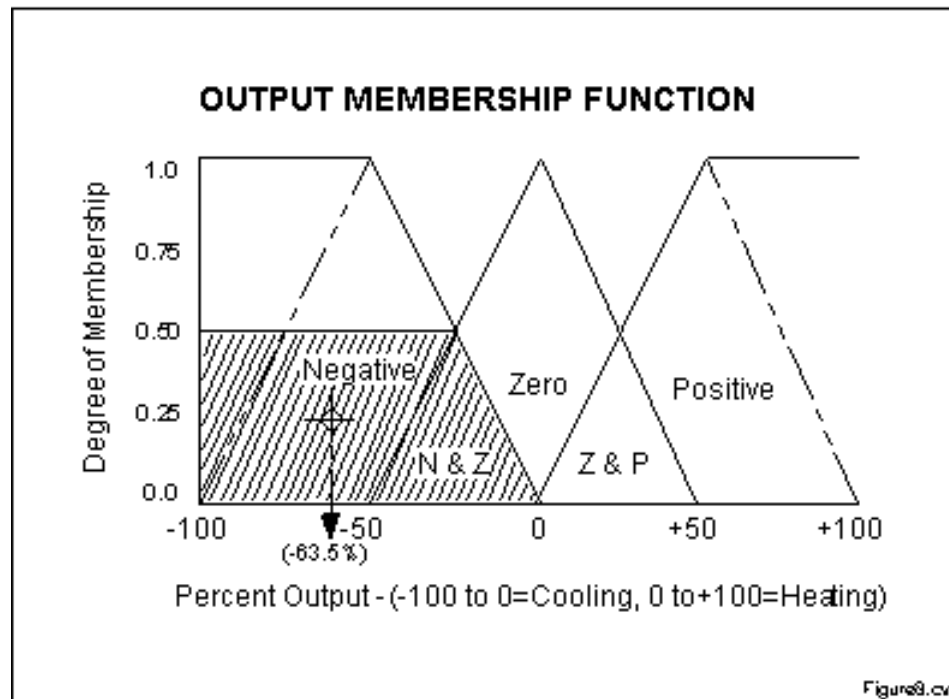
Figure 3 The Fuzzy Inference Process

### ERROR MEMBERSHIP FUNCTION



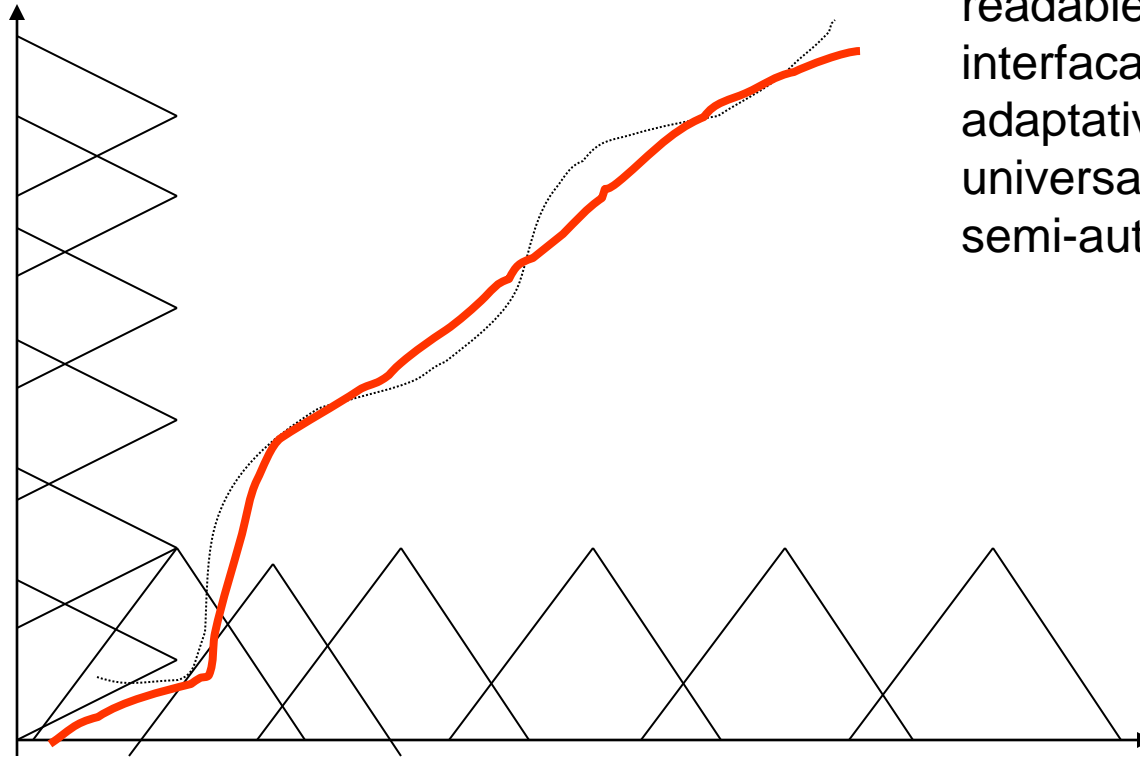
### ERROR-DOT MEMBERSHIP FUNCTION





IF x is very small THEN y is small  
IF x is small THEN y is medium  
IF x is medium THEN y is medium

Y



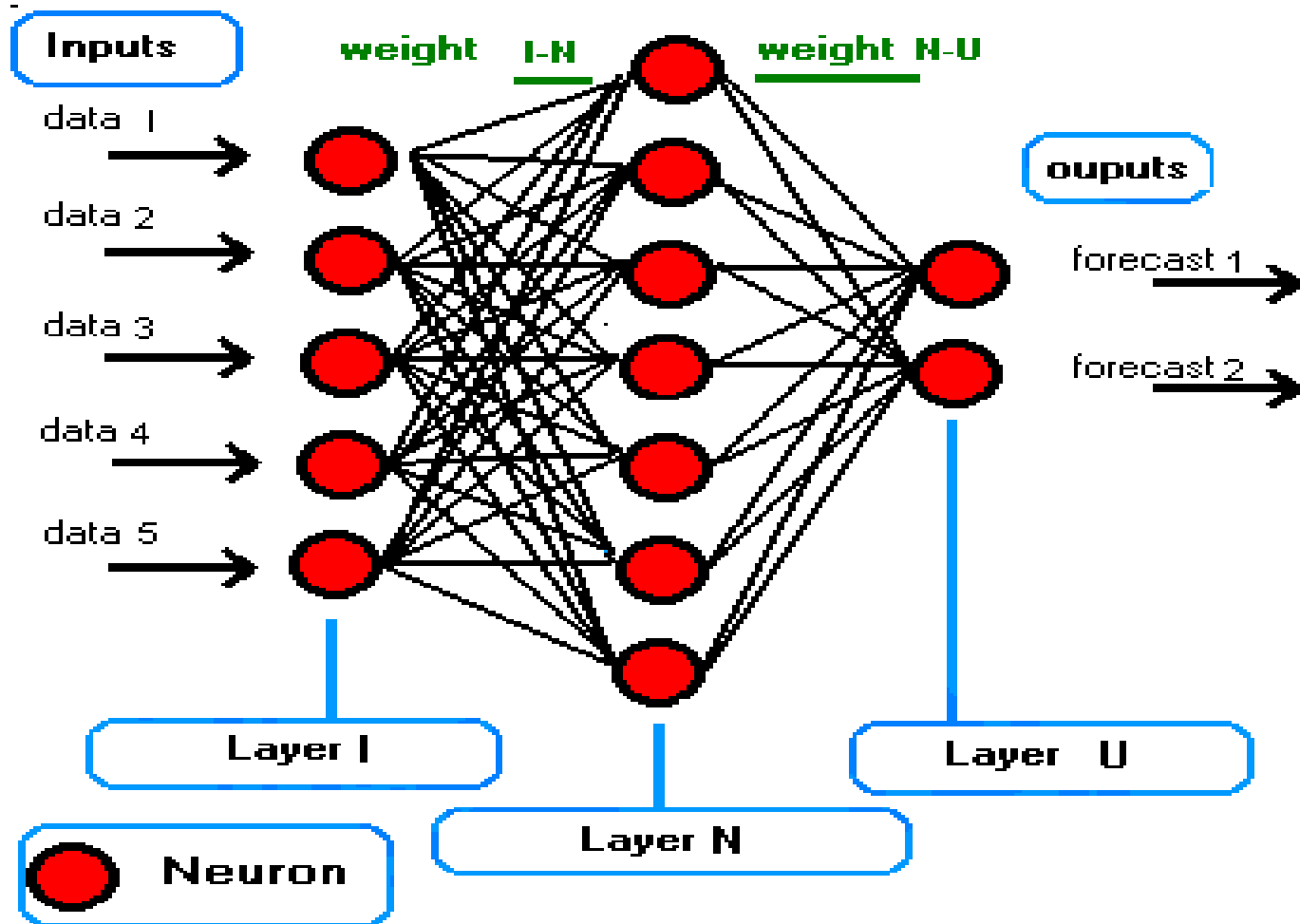
readable ?  
interfacable ?  
adaptative  
universal  
semi-automatic

---

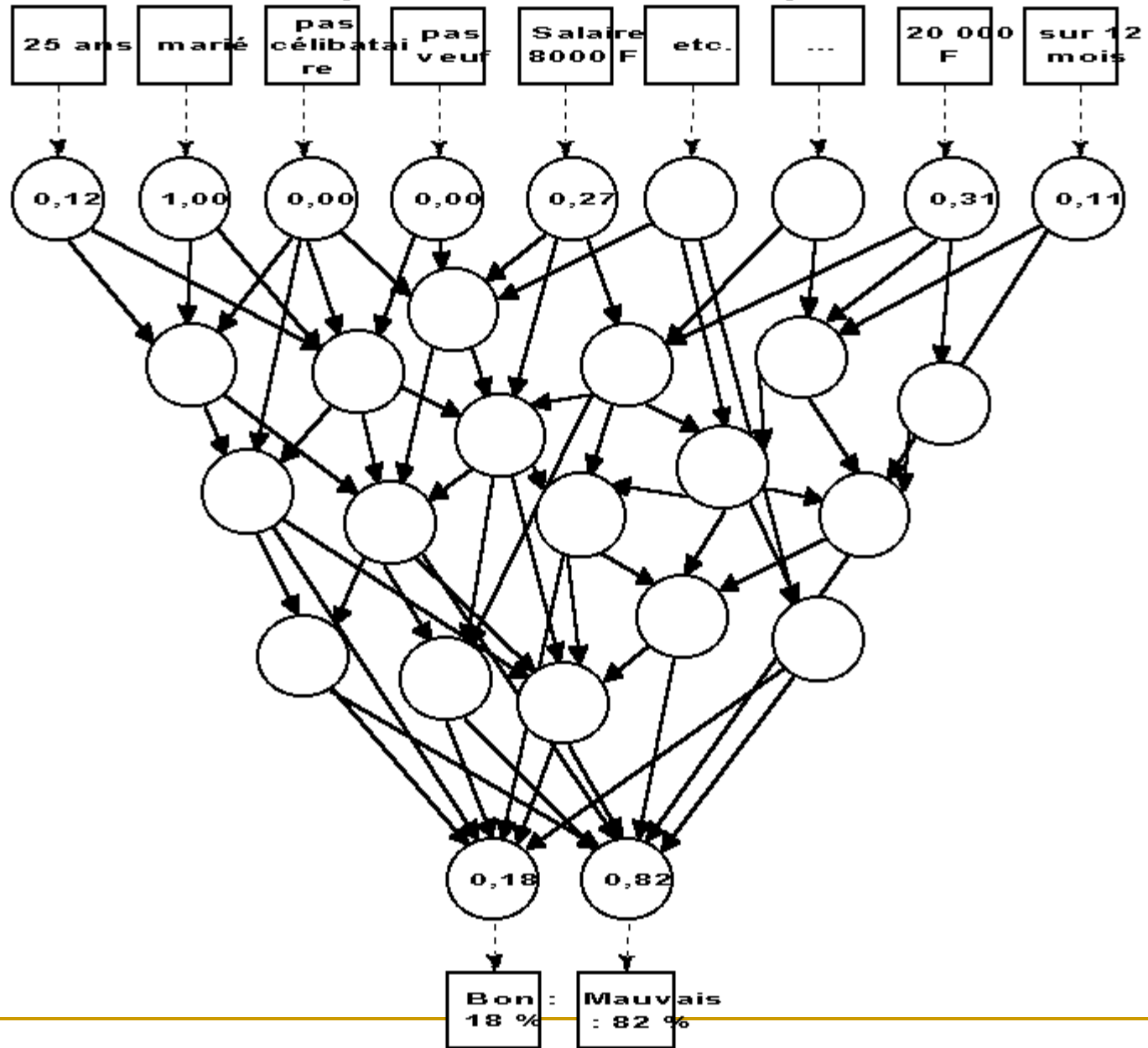
# Non comprehensible models

- From more to less
    - linear discriminant
    - local approaches
      - fuzzy rules
      - Support Vector Machine
      - RBF
    - global approaches
      - NN
      - polynômes, wavelet,...
      - Support Vector Machine
-

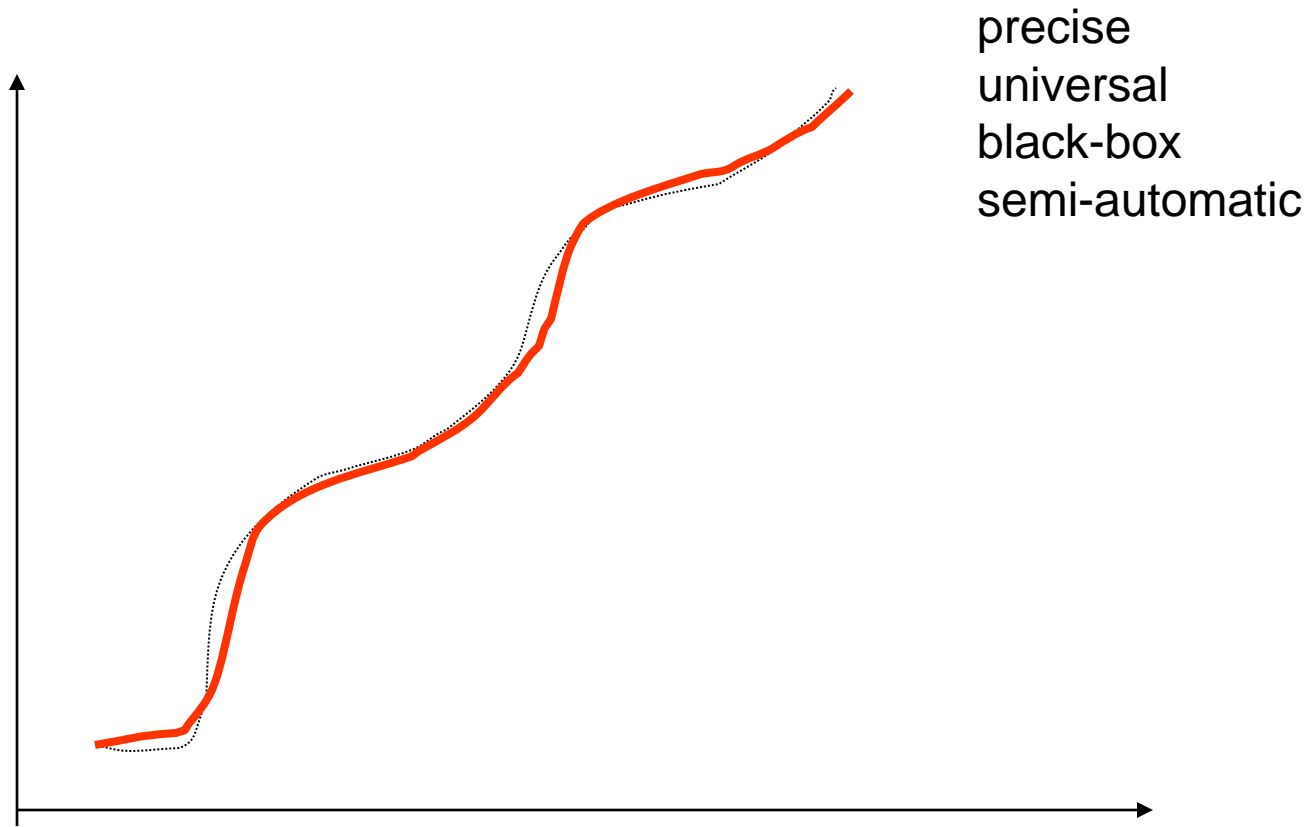
# The neural network



# description de dossier de prêt

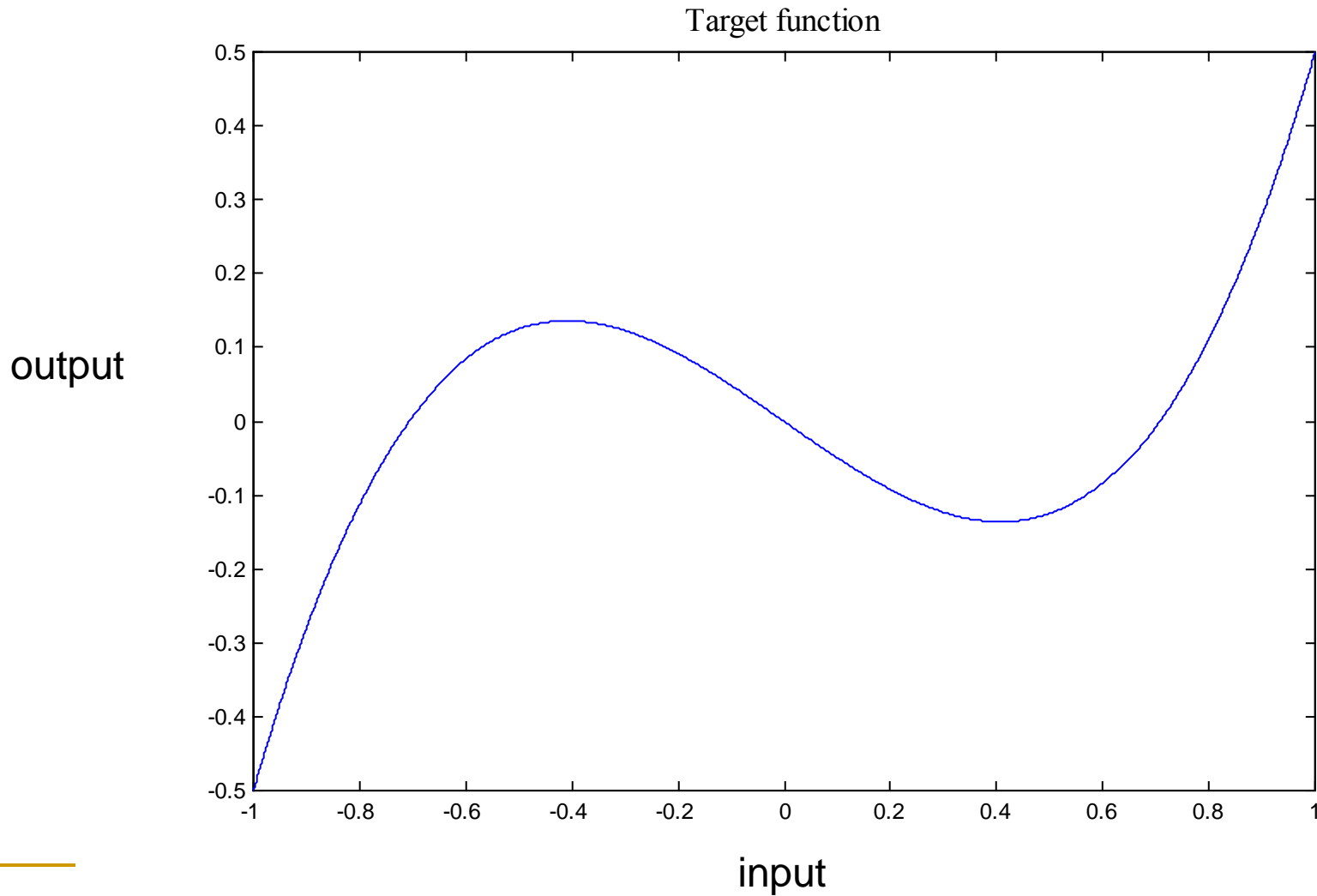


suggestion de décision

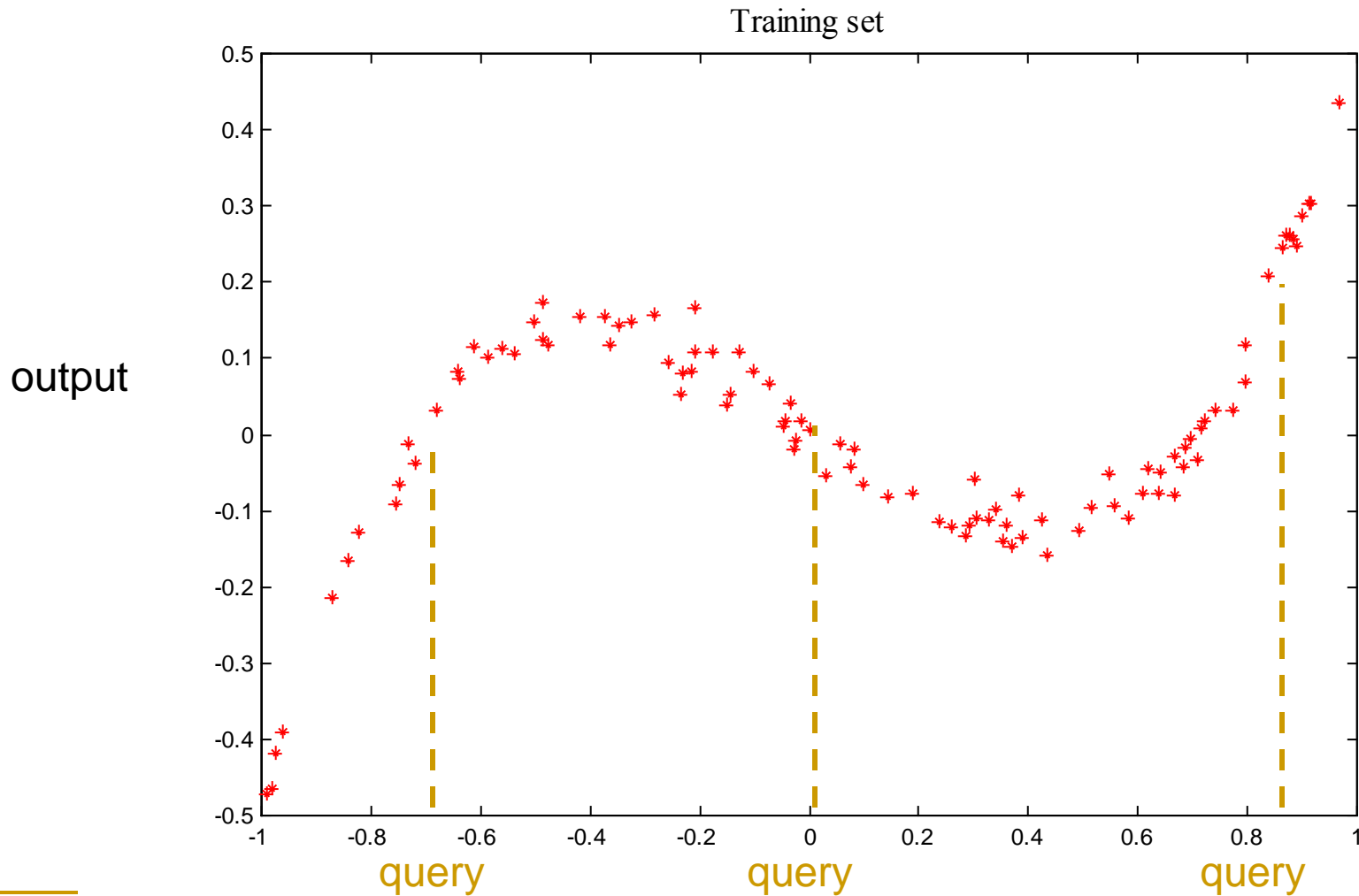




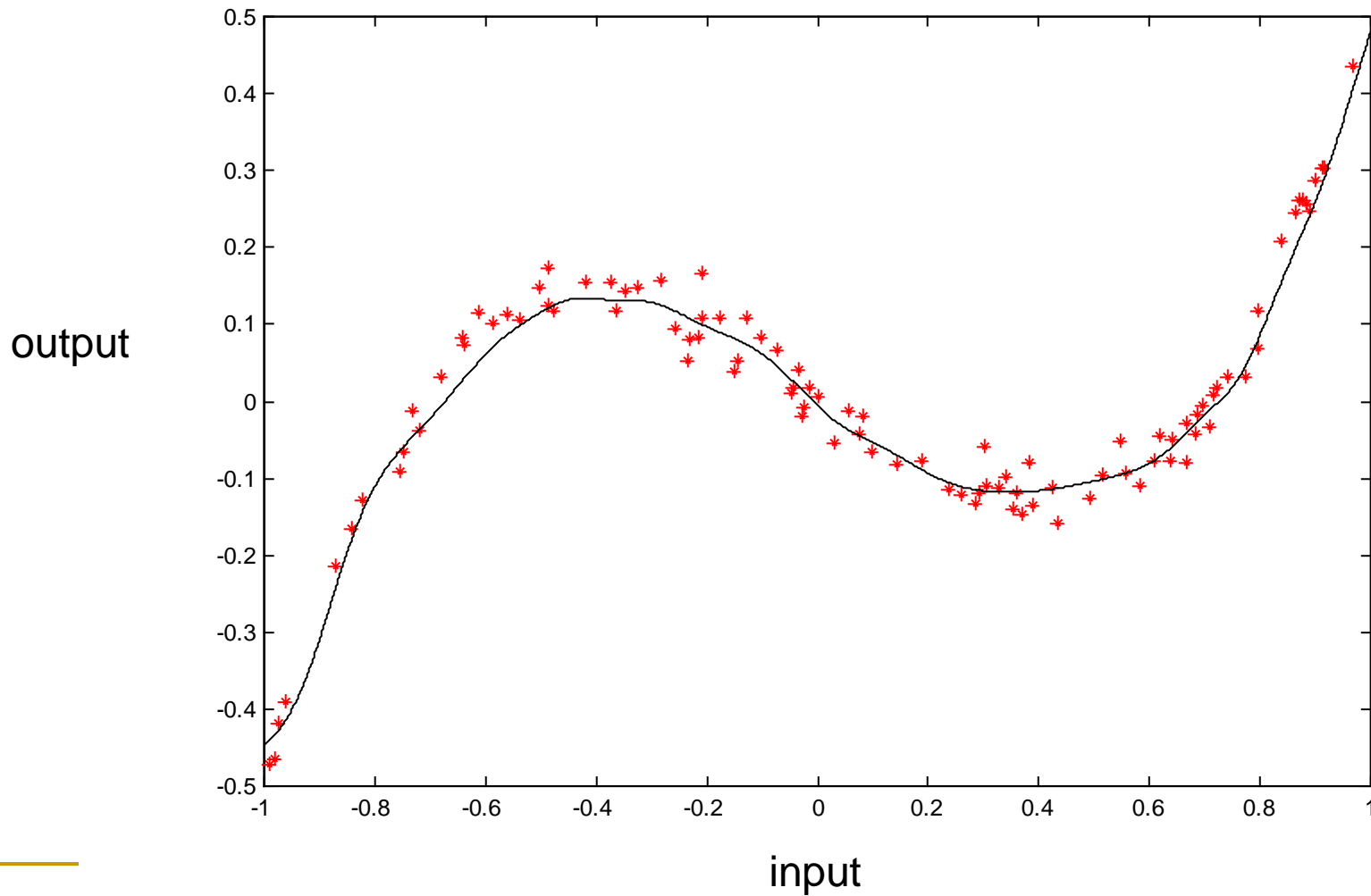
# Nonlinear relationship



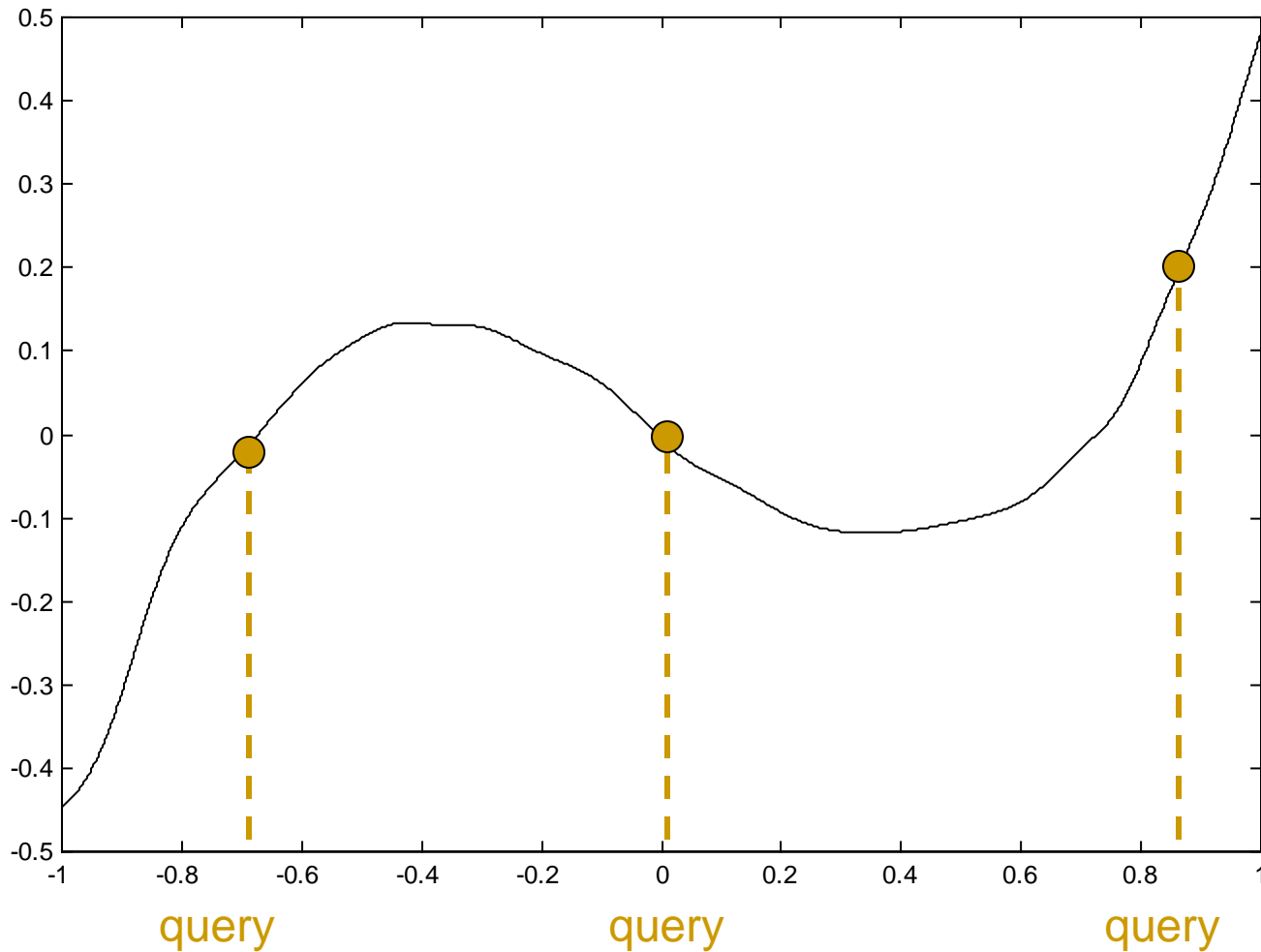
# Observations



# Global modeling



# Prediction with global models



---

# Advantages

- Exist without data
  - Information compression
    - Mainly SVM: mathématiques, pratiques, logique et génériques.
  - Detect a global structure in the data
  - Allow to test the sensitivity of the variables
  - Can easily incorporate prior knowledge
-

---

# Drawbacks

- Make assumption of uniformity
  - Have the bias of their structure
  - Are hardly adapting
  - Which one to choose.
-

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# BAGFS: ensemble method

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---

# 'Weak classifiers' ensembles

- Classifier capacity reduced in 2 ways :
    - simplified internal architecture
    - NOT all the available information
  - Better **generalisation**, reducing **overfitting**
  - Improving **accuracy**
    - ☞ by **decorrelating** classifiers errors
    - ☞ by increasing the **variability** in the learning space.
-



# `Bagging` : resampling the learning set

- Bootstraps aggregating (*Leo Breiman*)
  - random and independant perturbation of the learning set.
  - vital element : **instability** of the inducer\*.
    - e.g. **C4.5**, **neural network** but not **kNN** !
  - increase **accuracy** by reducing **variance**

\* inducer = base learning algorithm : c4.5, kNN, ...

---

# Learning set resampling : `Arcing`

- **Adaptive** resampling or reweighting of the learning set (*Leo Breiman* terminology).
  - ☞ **Boosting** (*Freund & Schapire*)
    - sequential reweighting based on the description accuracy.
      - ☞ e.g. **AdaBoost.M1** for multi-class problems.
    - needs instability so as bagging
    - better variability than bagging.
    - sensible to noisy databases.
    - better than *bagging* on non-noisy databases
-

---

# Multiple Feature Subsets :

Stephen D. Bay (1/2)

- problem ?
  - **kNN is stable vertically** so Bagging doesn't work.
- ☞ **horizontally : MFS** - combining random selections of features with or without replacement.
- question ?
  - what about other inducers such C4.5 ??



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# Multiple Feature Subsets :

## Stephen D. Bay (2/2)

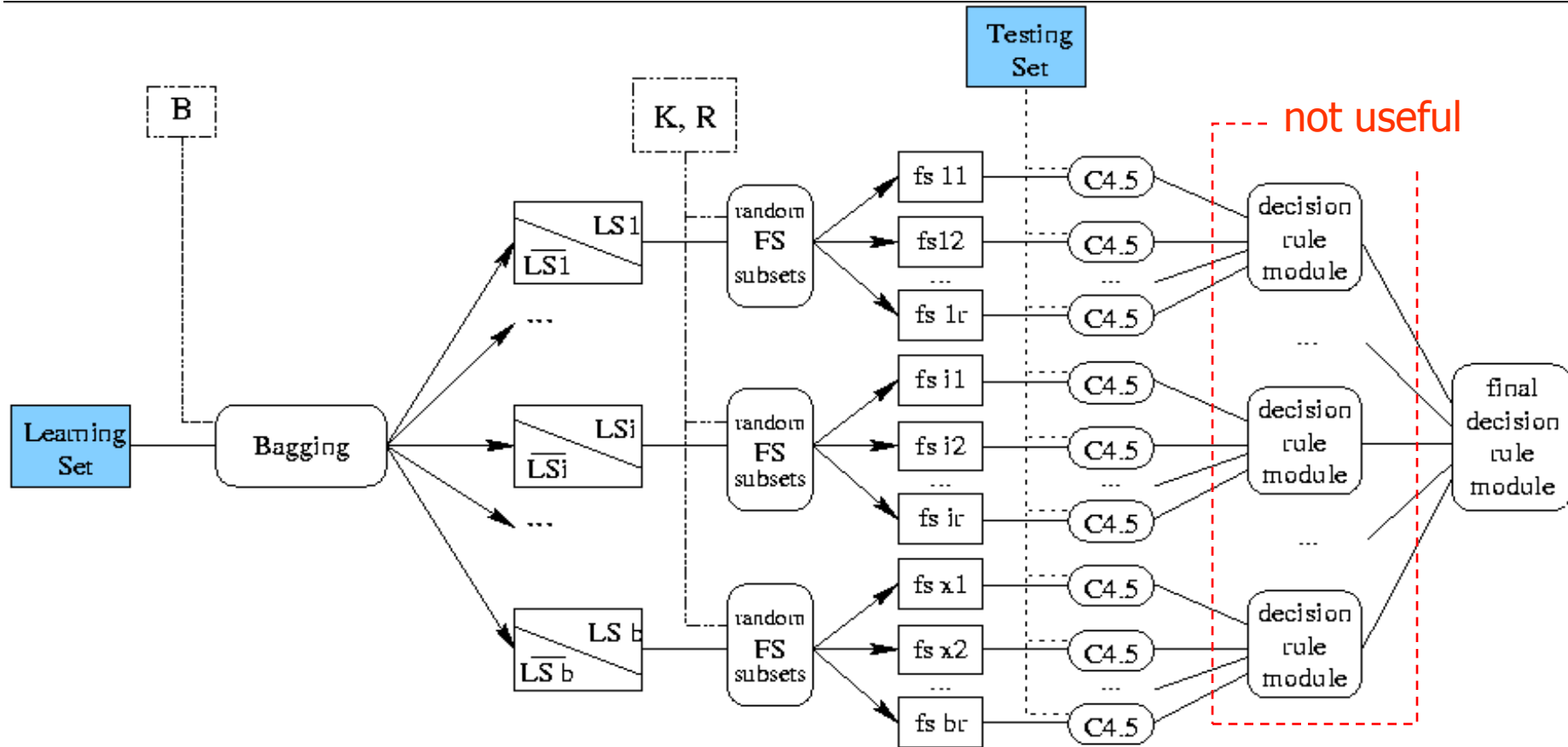
- **Hypo** : kNN uses its ' horizontal ' instability.
  - Two parameters :
    - $K=n/N$ , proportion of features in subsets.
    - $R$ , number of subsets to combine.
  - ☺ MFS is better than single kNN with FSS and BSS, feature selections techniques.
  - ☺ MFS is **more stable** than kNN on added irrelevant features.
  - ☺ MFS **decreases** variance and bias through randomness.
-

---

# BAGFS : a multiple classifier system

- BAGFS = MFS inside each Bagging.
  - BAGMFS = MFS & Bagging together.
  - 3 parameters
    - **B**, number of bootstraps
    - **K**= $n/N$ , proportion of features in subsets
    - **R**, number of feature subsets
  - decision rule : majority vote
-

# BAGFS architecture around C4.5



---

# Experiments

- Testing parametrization
    - optimizing  $K$  between 0.1 and 1 by means of a nested 10-fold cross-validation
    - $R=7, B=7$  for two-level method : Bagfs 7x7
    - set of 50 classifiers otherwise : Bag 50, BagMfs 50, MFS 50, Boosting 50
-

# Experimental Results

	c45	bagmfs 50	bagfs 7x7	boosting 50	bag 50	mfs 50
hepatitis	77.6	82.7	<b>84.1</b>	82.1	81.0	83.2
glass	64.8	<b>77.3</b>	76.6	74.4	74.8	75.2
iris	92.7	<b>93.4</b>	93.2	92.4	92.3	<b>93.5</b>
ionosphere	90.9	93.7	93.5	93.2	92.8	93.6
<b>liver disorders</b>	64.1	<b>73.5</b>	70.5	72.3	72.8	65.6
new-thyroid	92.0	<b>94.9</b>	94.5	93.5	93.8	92.7
<b>ringnorm</b>	91.9	<b>97.9</b>	97.7	95.3	95.6	97.6
twonorm	85.4	<b>96.9</b>	96.7	96.4	96.6	96.6
<b>satimage</b>	86.8	<b>91.4</b>	<b>91.3</b>	90.0	90.8	92.1
waveform	76.2	<b>84.6</b>	83.9	84.0	83.2	83.9
breast-cancer-w	94.7	<b>96.9</b>	<b>96.8</b>	95.5	95.3	<b>96.8</b>
<b>wine</b>	85.7	<b>92.3</b>	90.8	91.3	91.3	89.6
<b>segmentation</b>	93.4	<b>98.2</b>	<b>98.4</b>	95.1	96.6	<b>98.7</b>
Image	96.5	97.3	<b>97.8</b>	96.7	<b>97.6</b>	<b>97.6</b>
car	92.1	<b>93.2</b>	92.5	92.1	<b>93.2</b>	92.2
diabetes	72.4	75.7	75.7	<b>76.2</b>	75.7	74.0
	84.8	90.0	89.6	88.8	89.0	88.9

- McNemar test of significance (95%) : Bagfs performs never signif. worse and even sign. better on at least 4 databases (see red databases).



---

# BAGFS : discussions

- **How adjusting the parameters B, K, R**
    - internal cross validation ?
    - dimensionality and variability measures *hypothesis*
  - **Interest of a second level ?**
    - About irrelevant and (un)informative features ?
    - Does bagging + feature selections work better ?
    - How proving the interest of MFS randomness ?
  - **How using bootstraps complementary ?**
    - Can we ?
    - What to do ?
  - **How proving horizontal unstability of C4.5 ?**
  - **Comparison with 1-level bagging and MFS**
    - Same number of classifiers ?
    - Advantage of tuning parameters ?
-

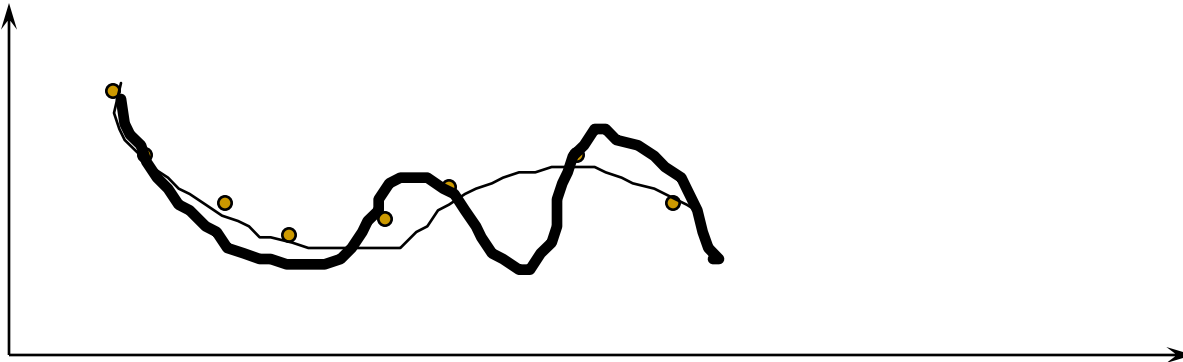
# Which best model ??

when they all can perfectly fit the data

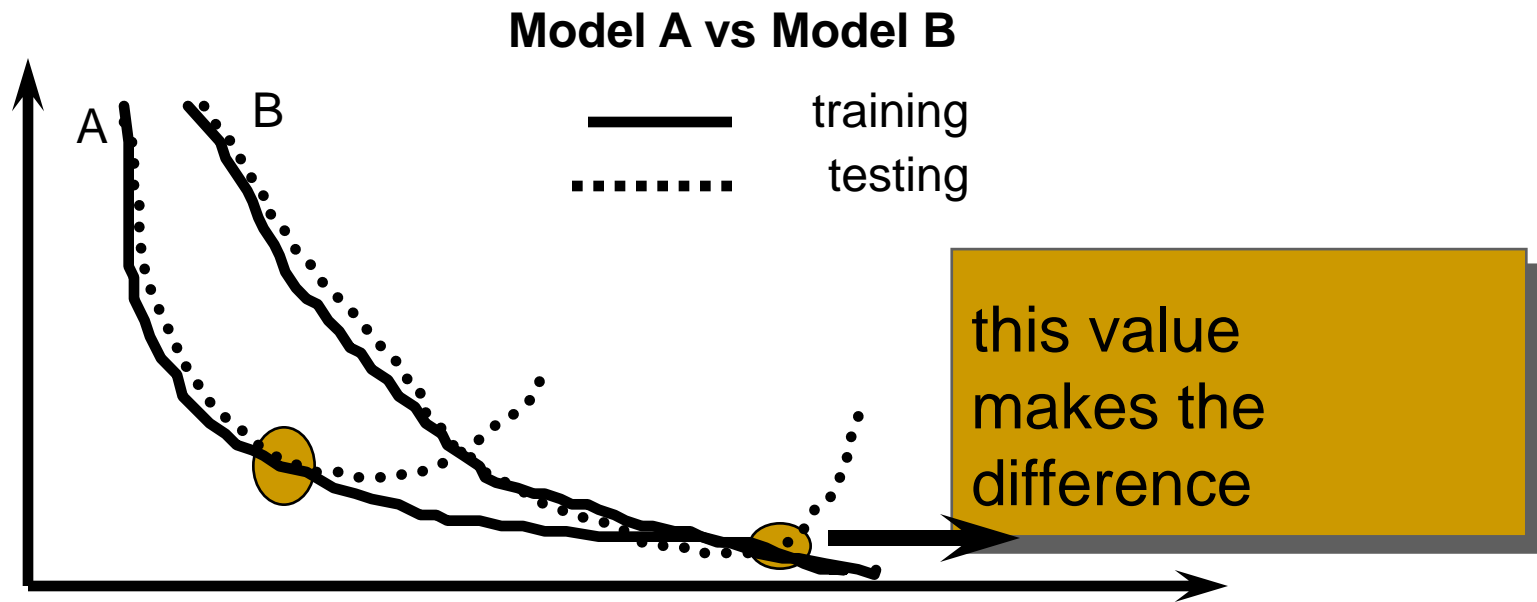
They all can perfectly fit the data but



they don't approach the data in the same way. This approach depends on their structure



# This explains the importance of Cross-validation



# Which one to choose

- Capital role of crossvalidation.
- Hard to run
- One possible response



- 
- Lazy methods
  - Coming from fuzzy
-

---

# Model or Examples ??

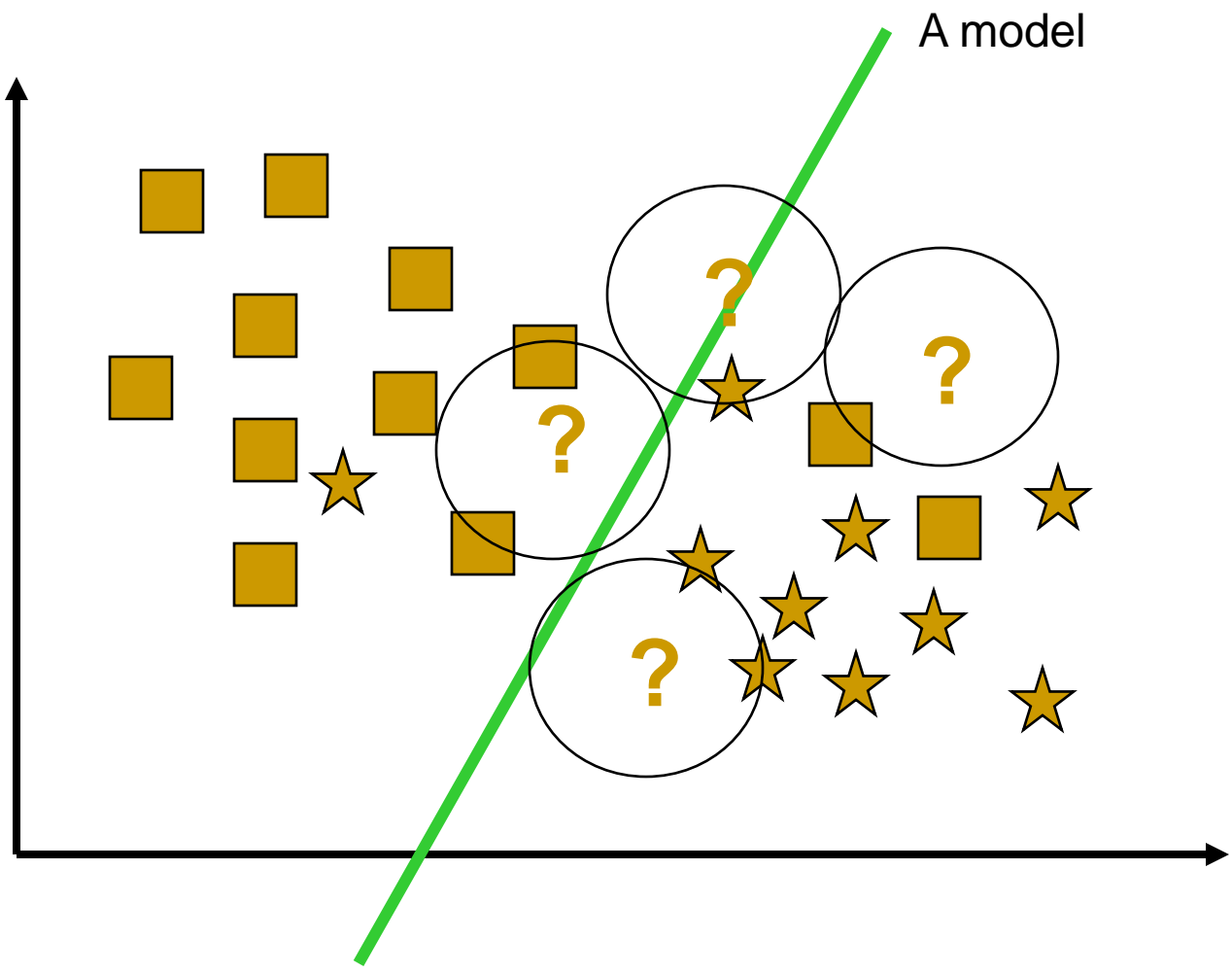
Build a Model



Prediction  
based on the model

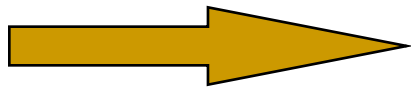
Prediction based  
on the examples

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# Lazy Methods

- Accuracy entails to keep the data and don't use any intermediary model: the best model is the data
- Accuracy requires powerful **local** models with **powerful cross-validation methods**



lazy methods is a new trend which is a revival of an old trend

- Made possible again due to the computer power

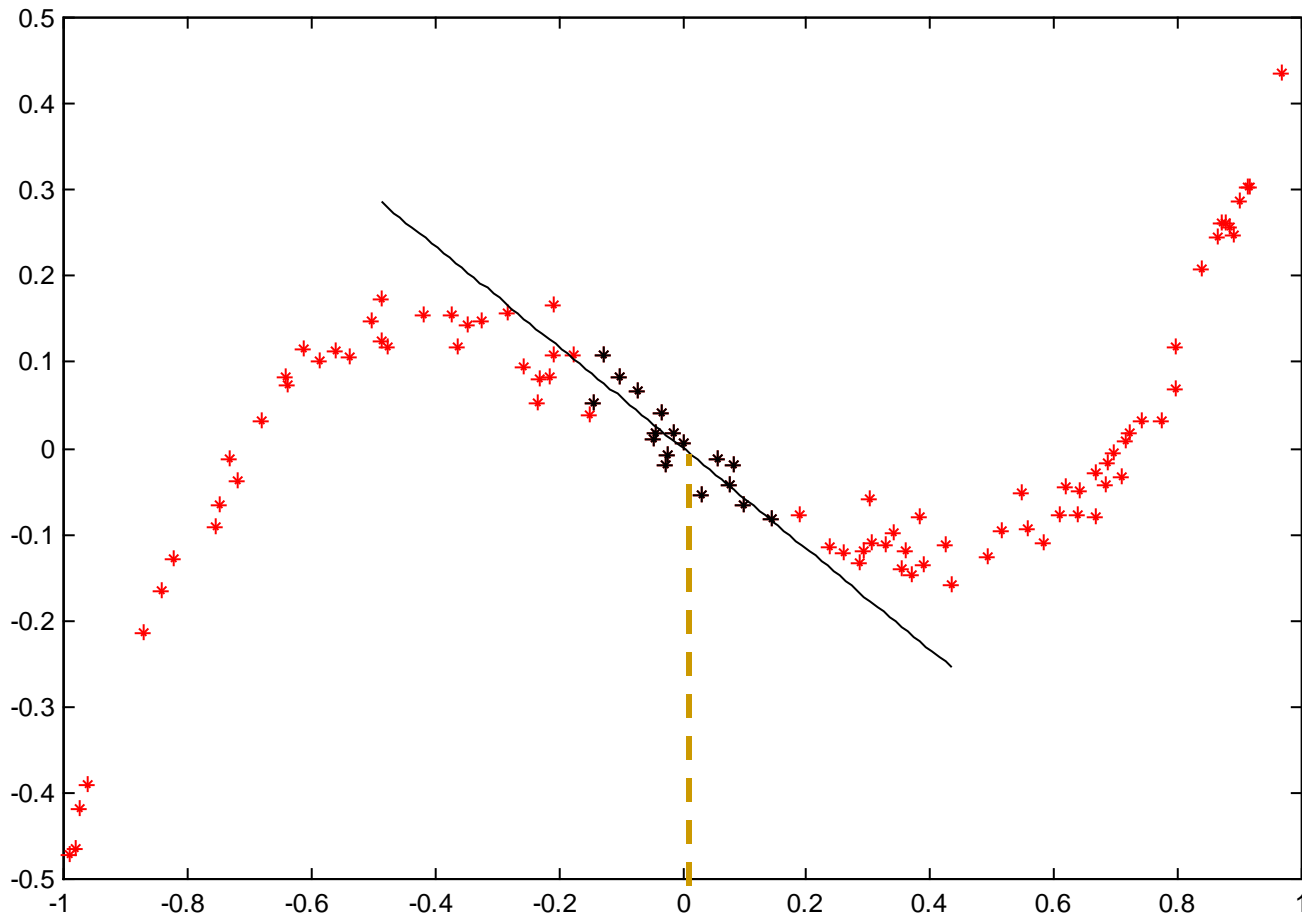


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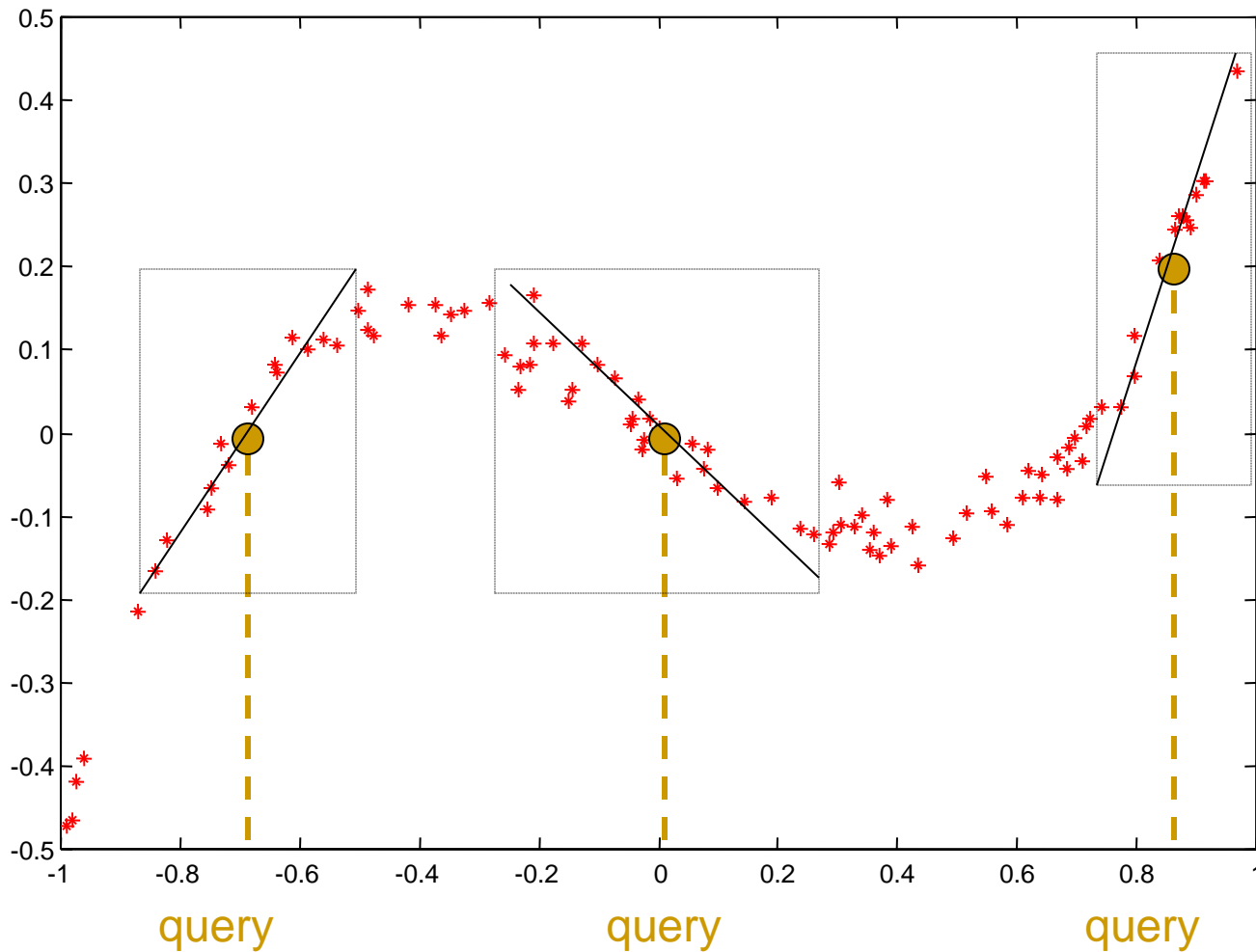
# Lazy methods

- A lot of expressions for the same thing:
    - memory-based, instance-based, examples-based, distance-based
    - nearest-neighbour
  - lazy for regression, classification and time series prediction
  - lazy for quantitative and qualitative features
-

# Local modeling



# Prediction with local models



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# Local modeling procedure

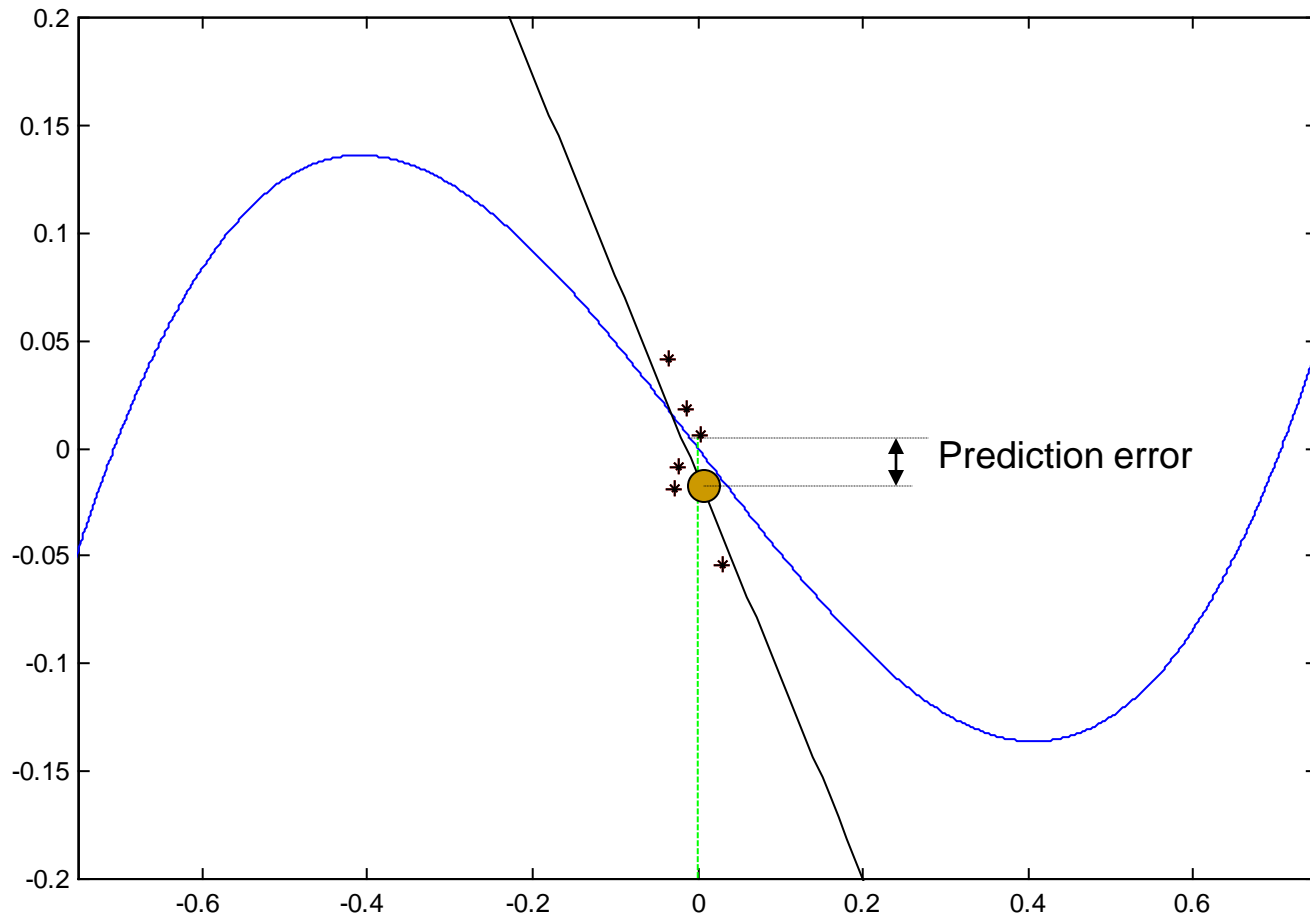
The identification of a local model can be summarized in these steps:

- ◆ **Compute the distance** between the query and the training samples according to a predefined **metric**.
- ◆ **Rank the neighbors** on the basis of their distance to the query.
- ◆ **Select a subset** of the nearest neighbors according to the **bandwidth** which measures the size of the neighborhood.
- ◆ **Fit a local model** (e.g. constant, linear,...).

The work focused on the **bandwidth selection problem**.

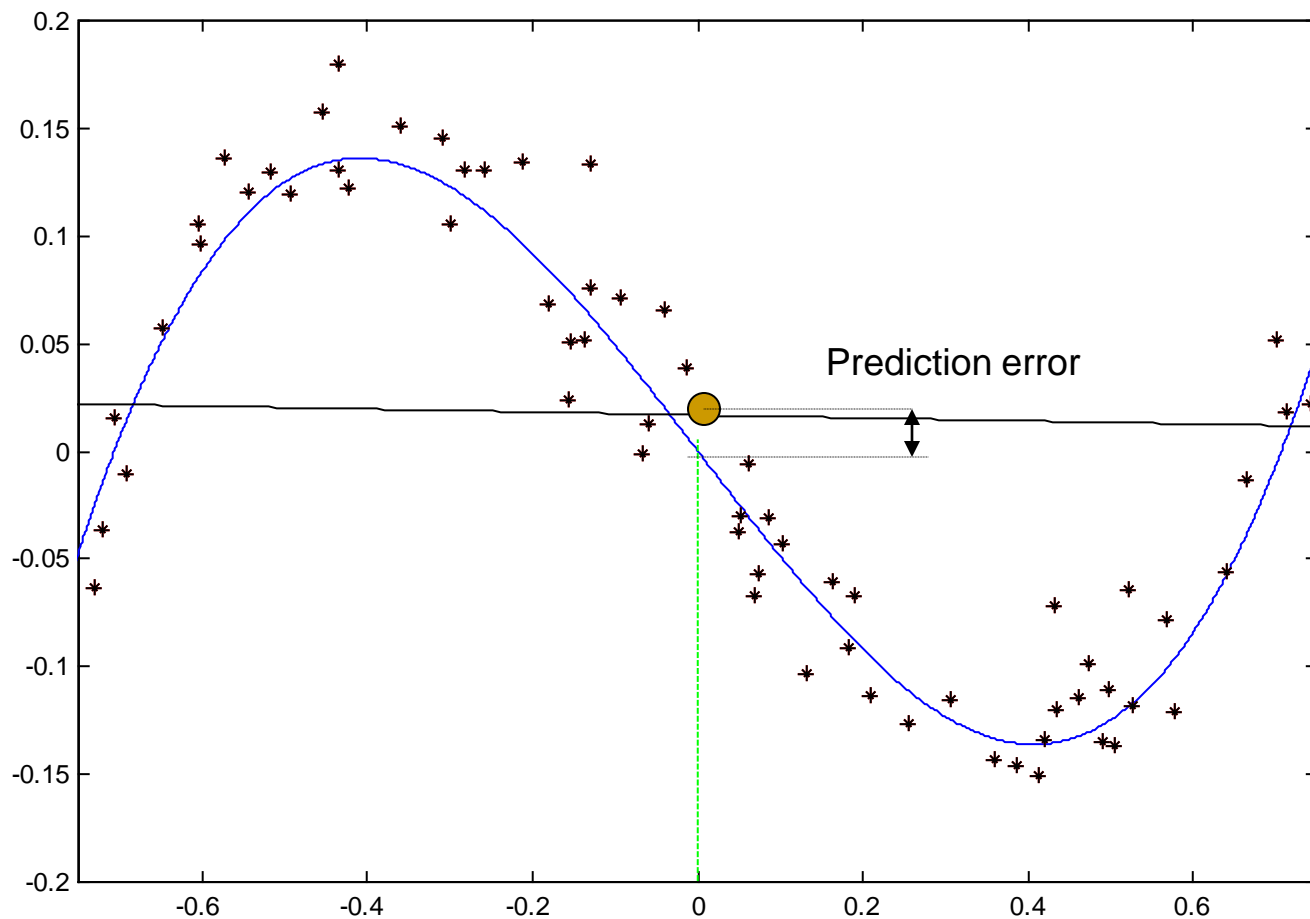
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# Bias/variance trade-off: overfitting



too few neighbors  $\Rightarrow$  **overfitting**  $\Rightarrow$  large prediction error

# Bias/variance trade off: underfitting



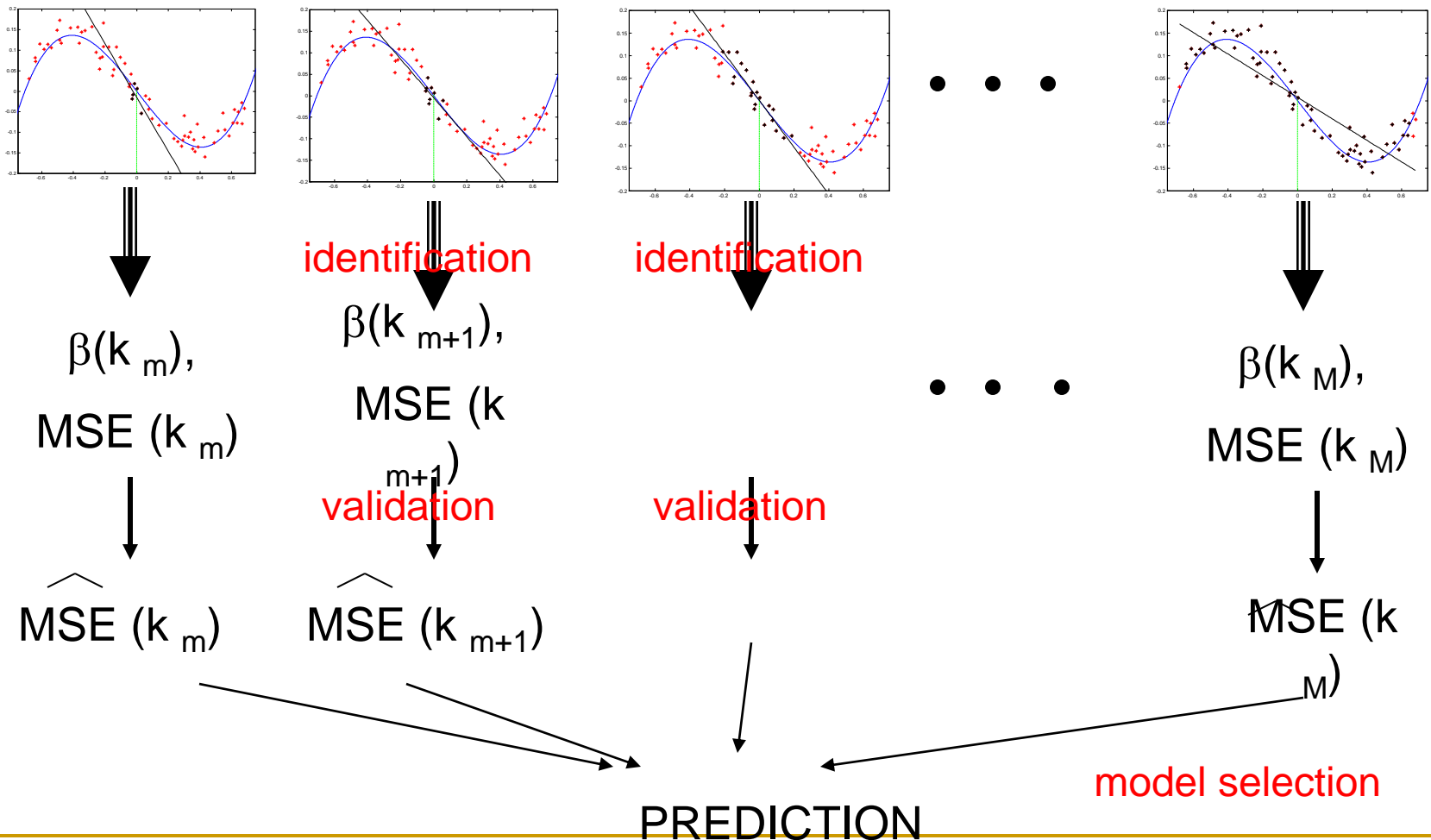
too many neighbors  $\Rightarrow$  **underfitting**  $\Rightarrow$  large prediction error

---

# Validation croisée: Press

- Fait un leave-one-out sans le faire pour les modèles linéaires
  - Un gain computationnel énorme
  - Rend possible une des validations croisées les plus puissantes à un prix computationnel infime.
-

# Data-driven bandwidth selection





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# Advantages

- No assumption of uniformity
  - Justified in real life
  - Adaptive
  - Simple
-

---

# From local learning to Lazy Learning (LL)

- By speeding up the local learning procedure, we can delay the learning procedure to the moment when a prediction in a query point is required (**query-by-query learning**).
  - This method is called **lazy** since the whole learning procedure is deferred until a prediction is required.
  - Example of non lazy methods (**eager**) are **neural networks** where learning is performed in advance, the fitted model is stored and data are discarded.
-

---

# Static benchmarks

- **Datasets:** 15 **real** and 8 **artificial** datasets from the ML repository.
  - ◆ **Methods:** Lazy Learning, Local modeling, Feed Forward Neural Networks, Mixtures of Experts, Neuro Fuzzy, Regression Trees (Cubist).
  - ◆ **Experimental methodology:** 10-fold cross-validation.
  - ◆ **Results:** Mean absolute error, relative error, **paired t-test**.
-

## Observed data

Dataset	No. examples	No. inputs
Housing	330	8
Cpu	506	13
Prices	209	6
Mpg	159	16
Servo	392	7
Ozone	167	8
Bodyfat	252	13
Pool	253	3
Energy	2444	5
Breast	699	9
Abalone	4177	10
Sonar	208	60
Bupa	345	6
Iono	351	34
Pima	768	8

## Artificial data

Dataset	No. examples	No. inputs
Kin_8nh	8192	8
Kin_8fm	8192	8
Kin_8nm	8192	8
Kin_32fh	8192	32
Kin_32nh	8192	32
Kin_32fm	8192	32
Kin_32	8192	32



# Experimental results: paired comparison (I)

Each method compared with all the others ( $9 \times 23 = 207$  comparisons)

Method	No. times significantly worse
LL linear	74
LL constant	96
<b>LL combination</b>	<b>23</b>
Local modeling linear	58
Local modeling constant	81
Cubist	40
Feed Forward NN	53
Mixtures of experts	80
Local Model Network (fuzzy)	132
Local Model Network (k-mean)	145

The lower, the better !!

# Experimental results: paired comparison (II)

Each method compared with all the others ( $9 \times 23 = 207$  comparisons)

Method	No. times significantly better
<b>LL linear</b>	80
<b>LL constant</b>	59
<b>LL combination</b>	<b>129</b>
<b>Local modeling linear</b>	89
<b>Local modeling constant</b>	74
<b>Cubist</b>	110
<b>Feed Forward NN</b>	116
<b>Mixtures of experts</b>	72
<b>Local Model Network (fuzzy)</b>	32
<b>Local Model Network (k-mean)</b>	21

The larger, the better !!

---

# Lazy Learning for dynamic tasks

- long horizon forecasting based on the iteration of a LL one-step-ahead predictor.
  - Nonlinear control
    - Lazy Learning inverse/forward control.
    - Lazy Learning self-tuning control.
    - Lazy Learning optimal control.
-

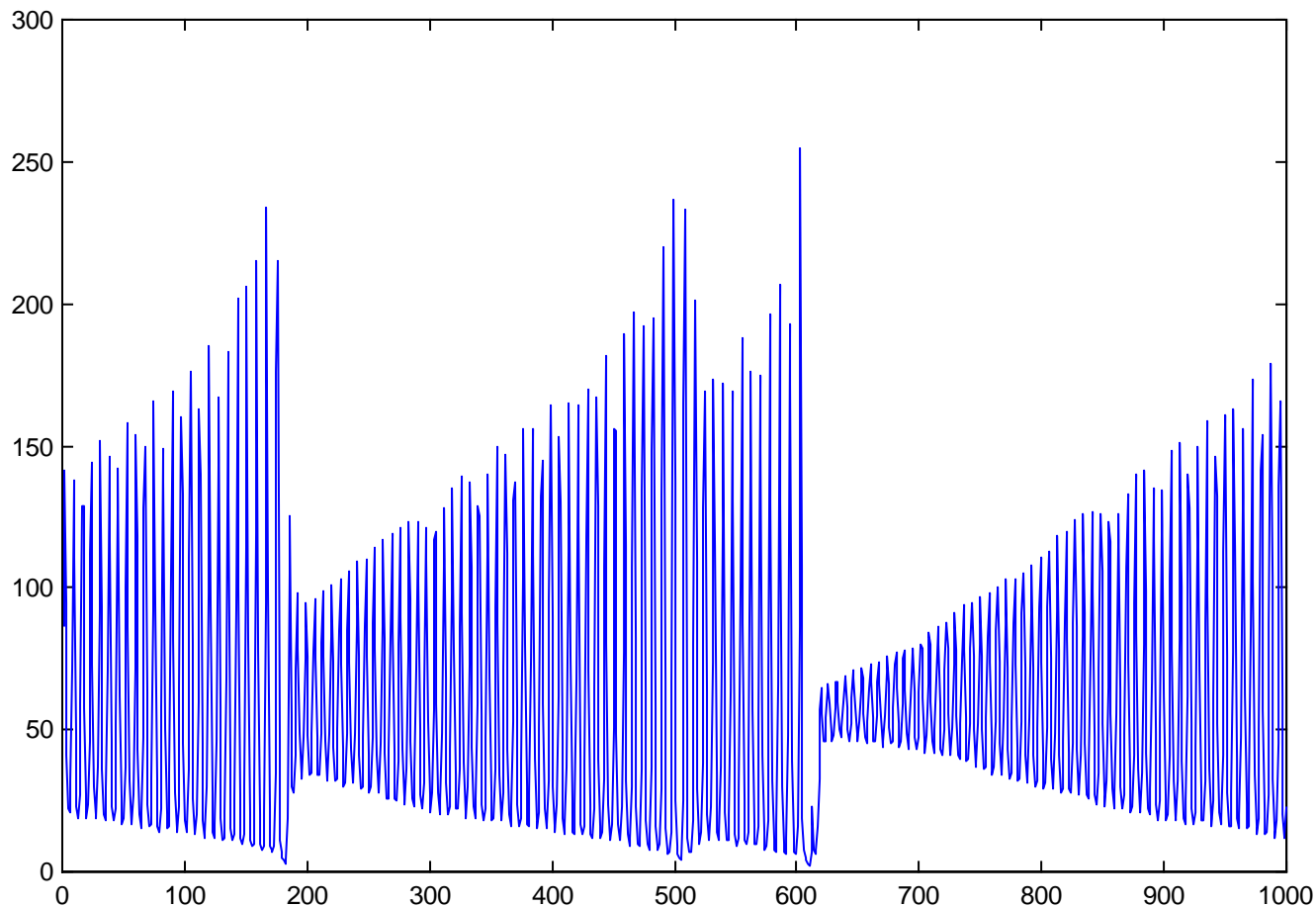
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# Dynamic benchmarks

- Multi-step-ahead prediction:
    - Benchmarks: Mackey Glass and 2 Santa Fe time series
    - Referential methods: recurrent neural networks.
  - Nonlinear identification and adaptive control:
    - Benchmarks: Narendra nonlinear plants and bioreactor.
    - Referential methods: neuro-fuzzy controller, neural controller, linear controller.
-

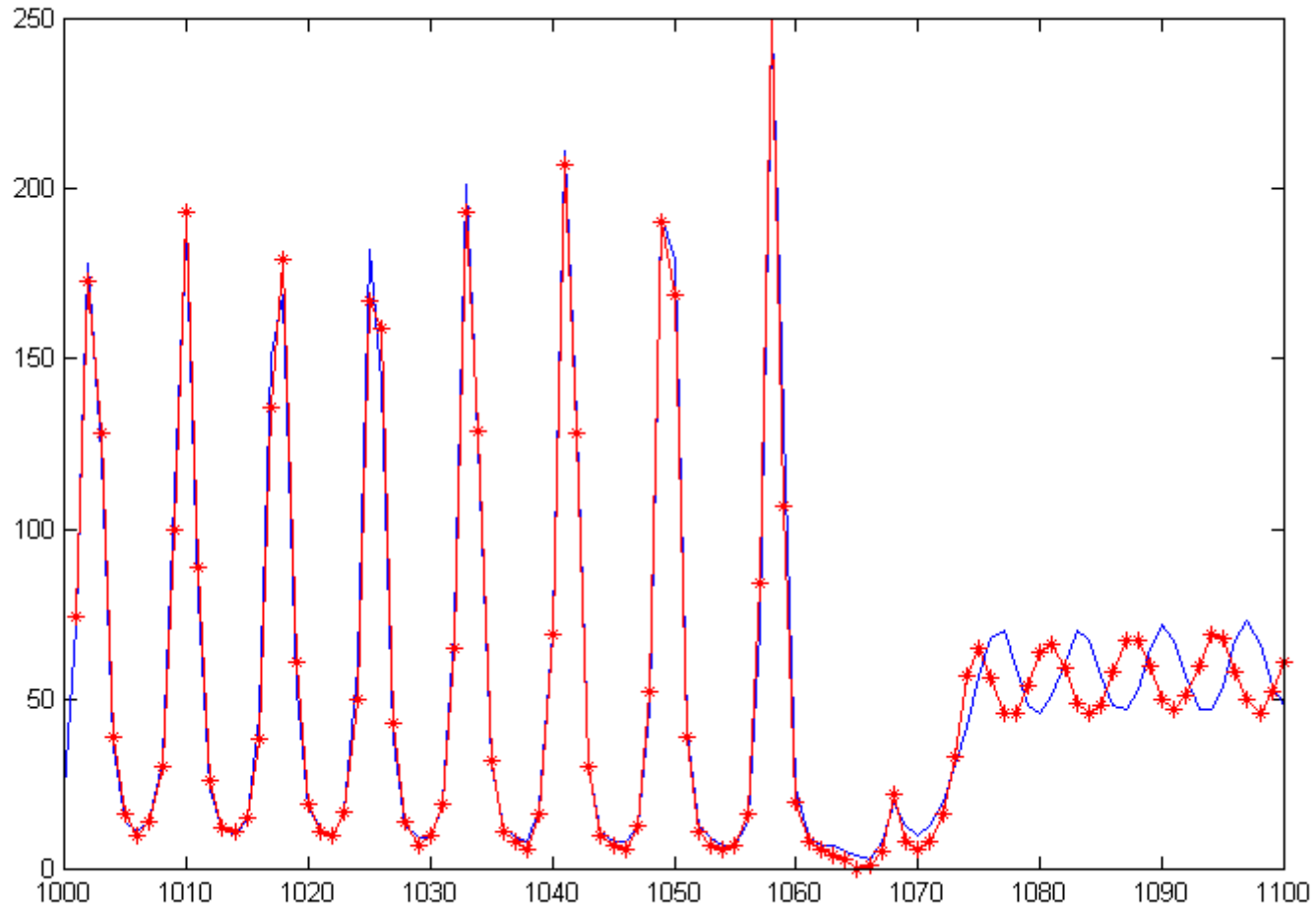


# Santa Fe time series



**Task:** predict the continuation of the series for the next 100 steps.

# Lazy Learning prediction



LL is able to predict the abrupt change around  $t = 1060$  !



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# Awards in international competitions

- **Data analysis competition:** awarded as a runner-up among 21 participants at the 1999 *CoIL International Competition* on *Protecting rivers and streams by monitoring chemical concentrations and algae communities*.
  - **Time series competition:** ranked second among 17 participants to the *International Competition on Time Series* organized by the *International Workshop on Advanced Black-box techniques for nonlinear modeling* in Leuven, Belgium
-