

Schemata Monte Carlo Tree Optimization

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Background

- *MCTS methods have been taken an increasing attention in the last 15 years*
- *Originally hi gather a spectacular success in the the game of GO*
- *Later applied successfully in designing expert computer players for many others two players games:*
 - *Hex, Kriegspiel, Poker*
- *Outperform alphabeta search even where good heuristic evaluations are difficult to obtain*
- *Recently, some other domains have been addressed*

Binary Combinatorial Optimization

- *BCO consists in the finding of a binary string that represents the optimal combination of yes/no alternatives.*
- *The difficulty resides in the weakness of the binary representation.*
- *The GA tries to overcome it with an implicit parallel evaluation of schemata.*
- *However there is no explicit use of schemata to improve the search of better solutions.*

Binary schemata

- *In this work we try obtain binary schemata from whom good solutions could be generated*
- *Schemata must be generated being fitter and more specific in time*
- *Schemata are used to generate, randomly, solutions to the problem, and those solutions are used to estimate the efficacy of the schemata*

0011111001 0001111010
0111011001 0101011001
0101101010 0101001000
0111111011 0001001010
0011101001 0001001001

01**10****

S-MonteCarlo Network

- *Generating good schemata have many intrinsic problems.*
 - *The space of schemata is much bigger than those of the solutions (3^L vs. 2^L)*
 - *Schemata evaluation is a difficult task because its size and structure*
- *We propose the use of MCTS:*
 - *They could deal with incomplete information*
 - *They can improve the efficiency of accuracy estimations for schemata*
 - *They use a tree structure that fits very well the intrinsic nature of the schemata*

S-MonteCarlo Network

- *Nodes in the network are composed by schema*
- *The first node is the more general schema, don't care symbol in every position*
- *Each node is one level more specific than its parent*
- *Last level nodes contain schema of a fixed small specificity, allowing the generation of every possible individual*
- *The other nodes are evaluated by a sampling set of individuals generated randomly*

Procedure

- *In each iteration the most promising node is selected for expansion*
- *The network grows in a unstructured and unbalanced way*
- *All nodes not fully expanded could be considered for selection*
- *The procedure is performed in four phases:*
 - *Selection*
 - *Expansion*
 - *Simulation*
 - *Backpropagation*

Selection

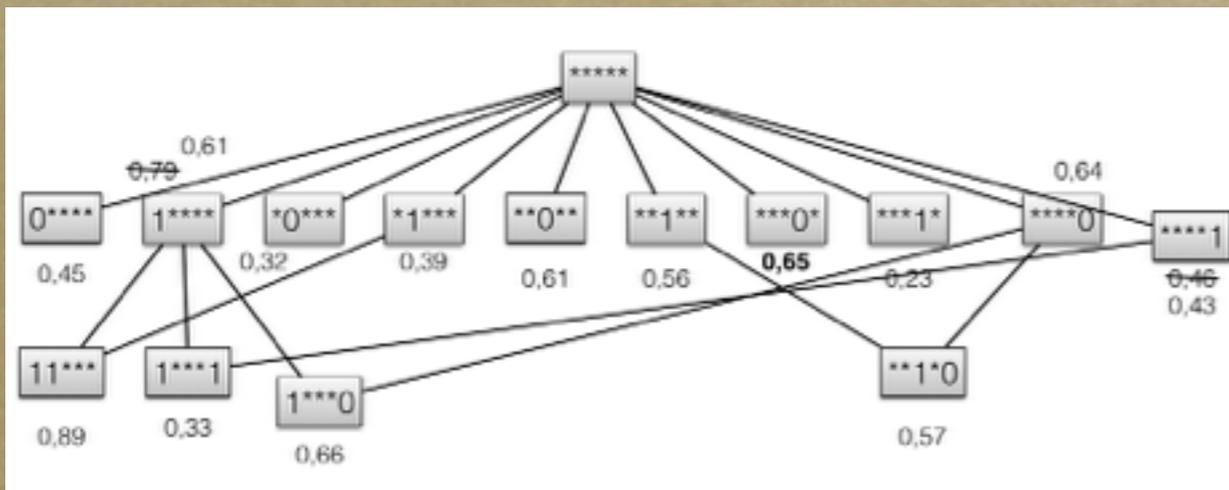
- *The more promising unexpanded node of the network must be selected*
- *A tree policy is designed to decide the meaning of being a promising node*
 - *There are many tree policy, in this work we propose the use of the Upper Confidence Policy (UCP)*

$$M(S_k) = f(S_k) + C \sqrt{\frac{\log N_k}{n_k}}$$

- *$M(S_k)$ -> Criteria for a node S_k to be selected*
- *$f(S_k)$ -> Evaluation of node S_k*
- *c is the exploration parameter*
- *N_k -> Size of the sampling set for node S_k*
- *n_k -> Number of examples used historically to evaluate node S_k*

Expansion

- *The selected node is expanded, generating one descendant, following random expansion policy*
- *Once a descendant is generated, it is liked with all their parents, those that are less general and matching the new one*



Simulation

- *The new generated node is from a sampling set of individuals represented by the schema of that node*
- *The solutions in the sampling set are generated randomly, fitting the rules of the schema, and are not stored*
- *The value assigned to the schema will be the average of the evaluation values of its sampling set*

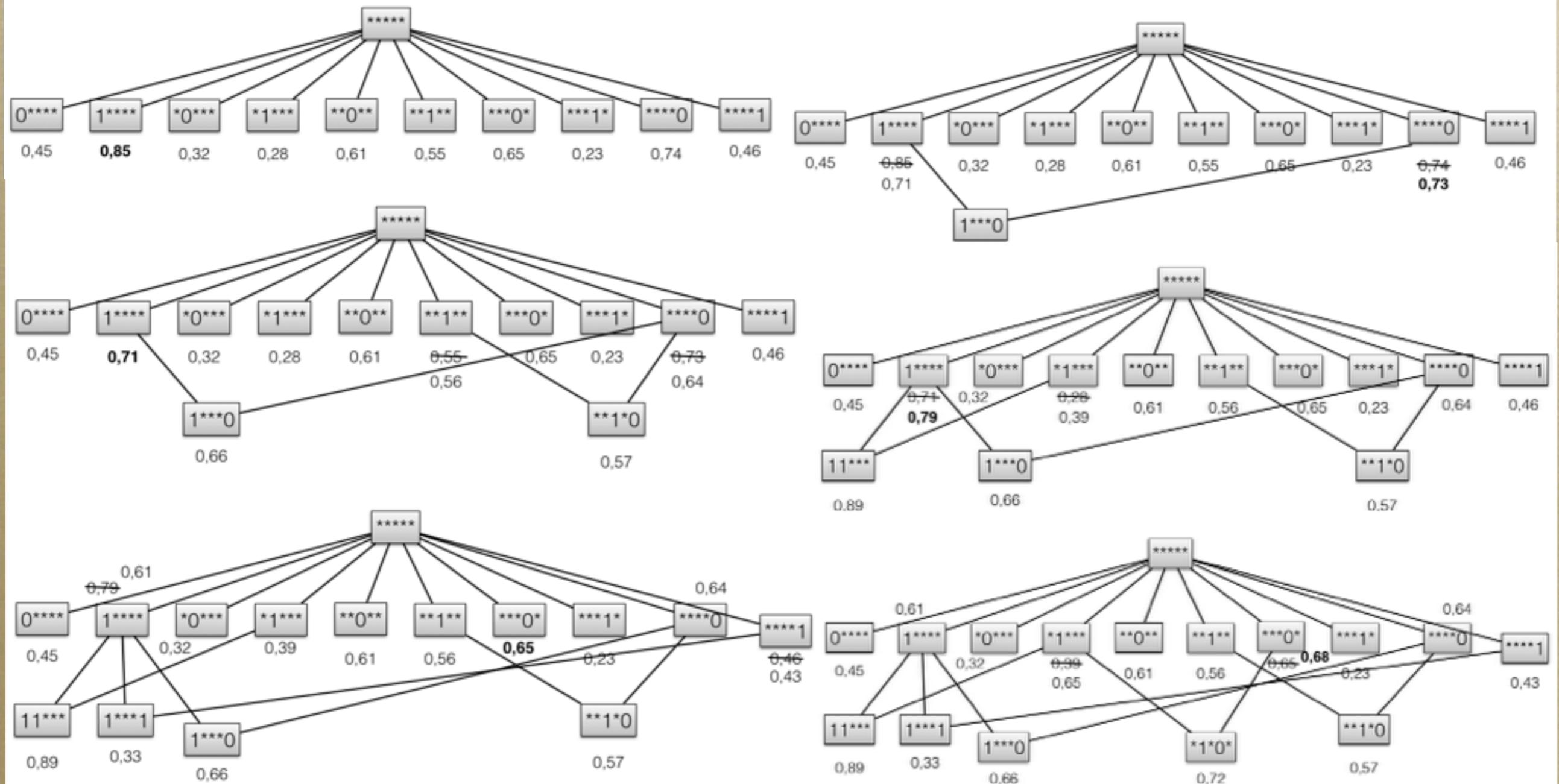
BackPropagation

- *All the evaluation values of all the nodes that are ancestors to the new created node are updated*

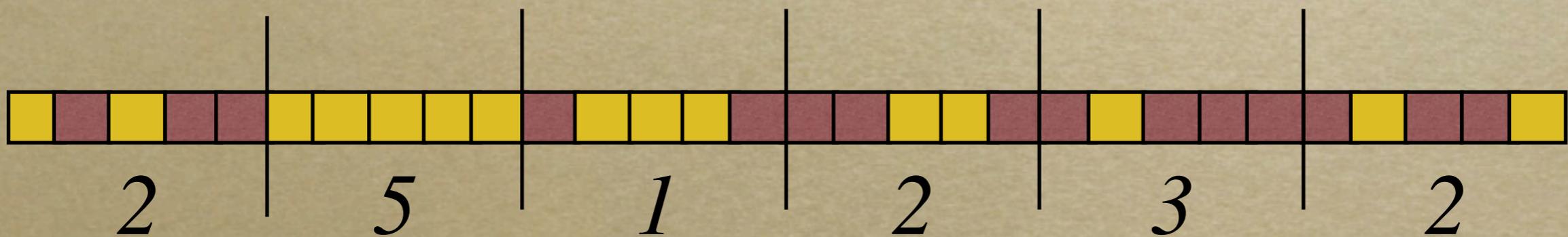
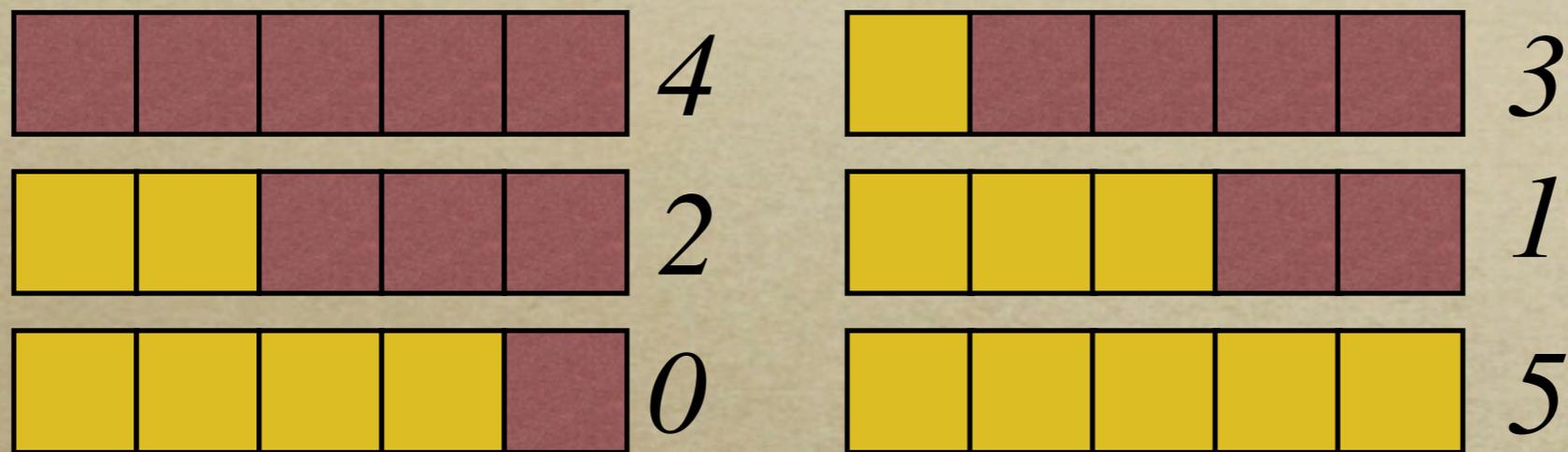
$$f(S_k) = \frac{(t \cdot f(S_k)) + v(S_k)}{t + 1}$$

$$v(S_k) = \frac{\sum_{I_i \in S_k} f(I_i)}{n}$$

Example of iterations



Deceptive trap function



$$f = 15/30 = 0,5$$

Knapsack problem



$$\sum_{i=1}^n w_i x_i$$

$$\sum_{i=1}^n w_i x_i \leq W$$

$$x \in \{0, 1\}$$

Results

Deceptive function			
Size	Best solution	Accuracy (mean, deviation)	Evaluations (mean, deviation)
20	0,96	0,94±0,02	154831±152774
25	0,96	0,92±0,01	282726±185339
30	0,91	0,89 ±0,01	404122±269166
35	0,91	0,88±0,01	526249±237347
40	0,9	0,87±0,01	623444±141584
45	0,89	0,86±0,01	754003±146172
50	0,88	0,85±0,008	890116±104346
Knapsack problem			
24	1,0	1,0±0,0	368562±93717